

Bounds on Long-Lived Dark Matter Mediators from Neutron Stars

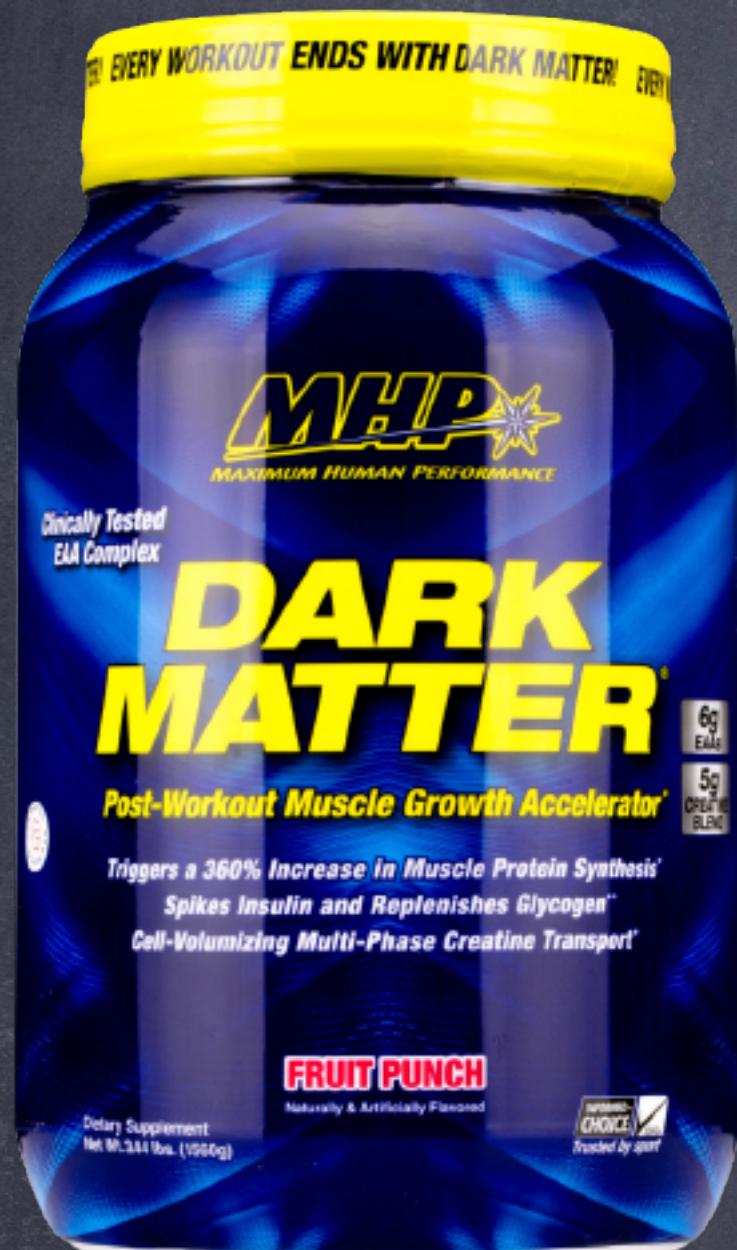
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in collaboration with Tim. M.P. Tait³
(In preparation)

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2. Sorbonne University, Jussieu, Paris, France.
3. Department of Physics and Astronomy, University of California, Irvine, CA, USA.



Outline

Preview: Dark Matter
Detections

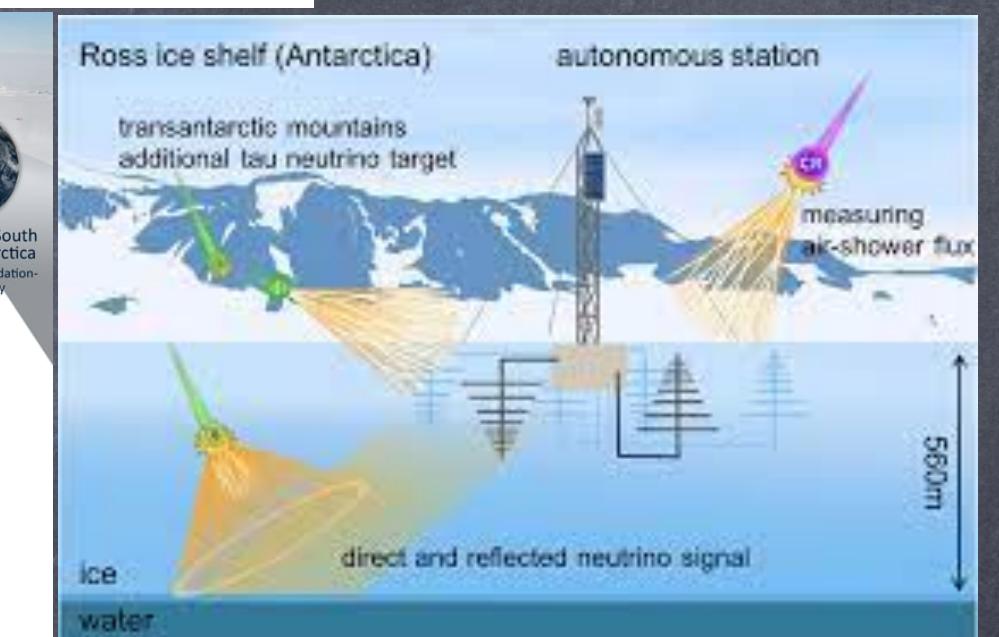
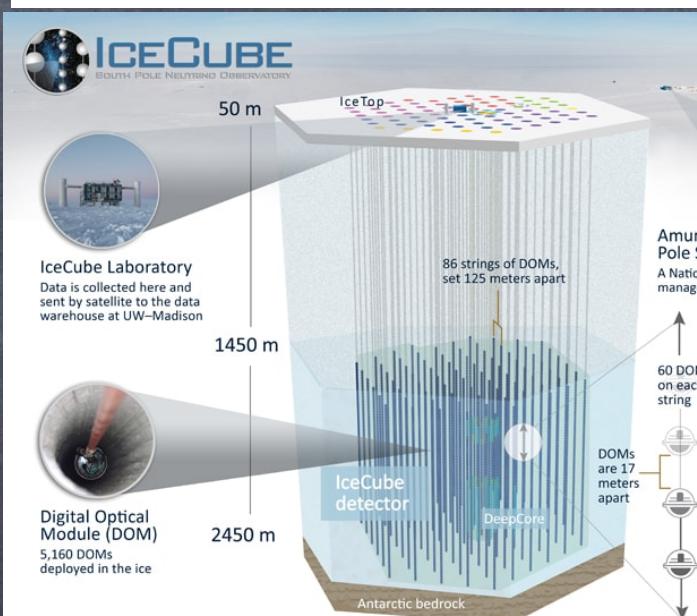
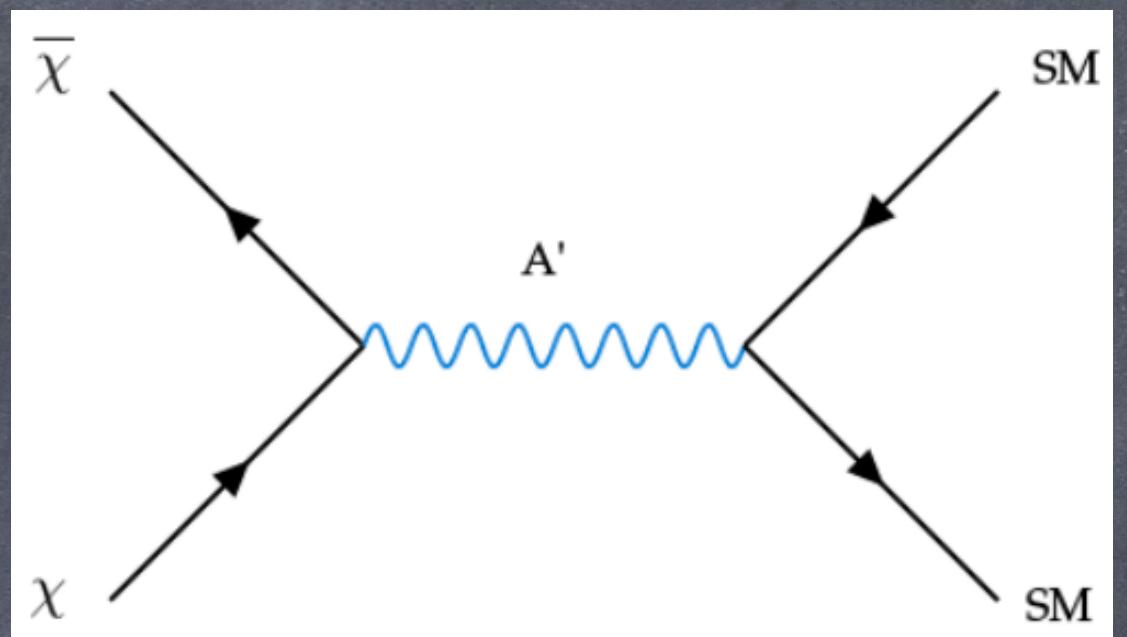


Available on Amazon,
Come with different flavors.

Free High Energy Colliders!!

Neutron Stars in
Galactic Center.

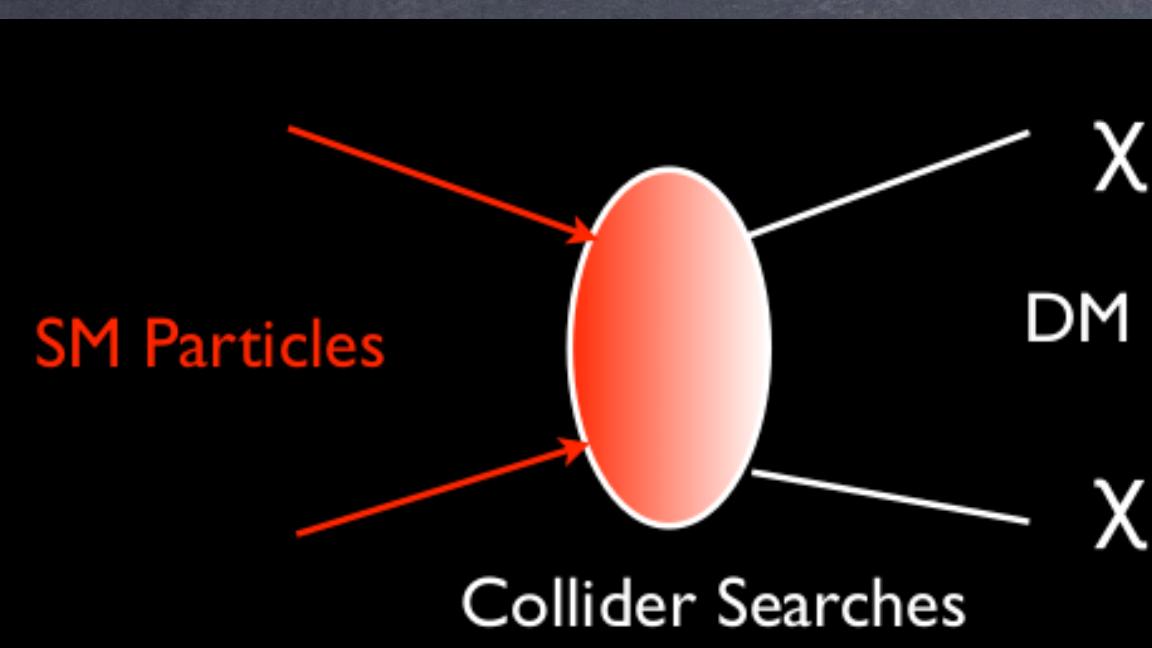
The DM model.



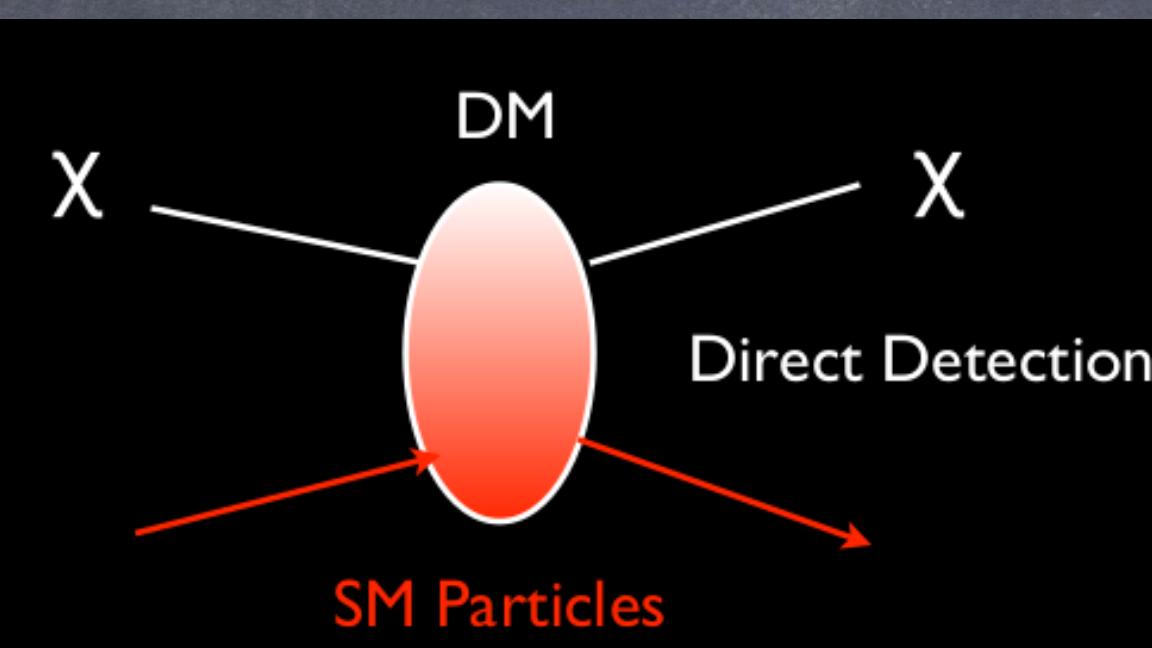
IceCube.
ARIANNA
(Projections).
Experimental results

Dark matter Detection methods

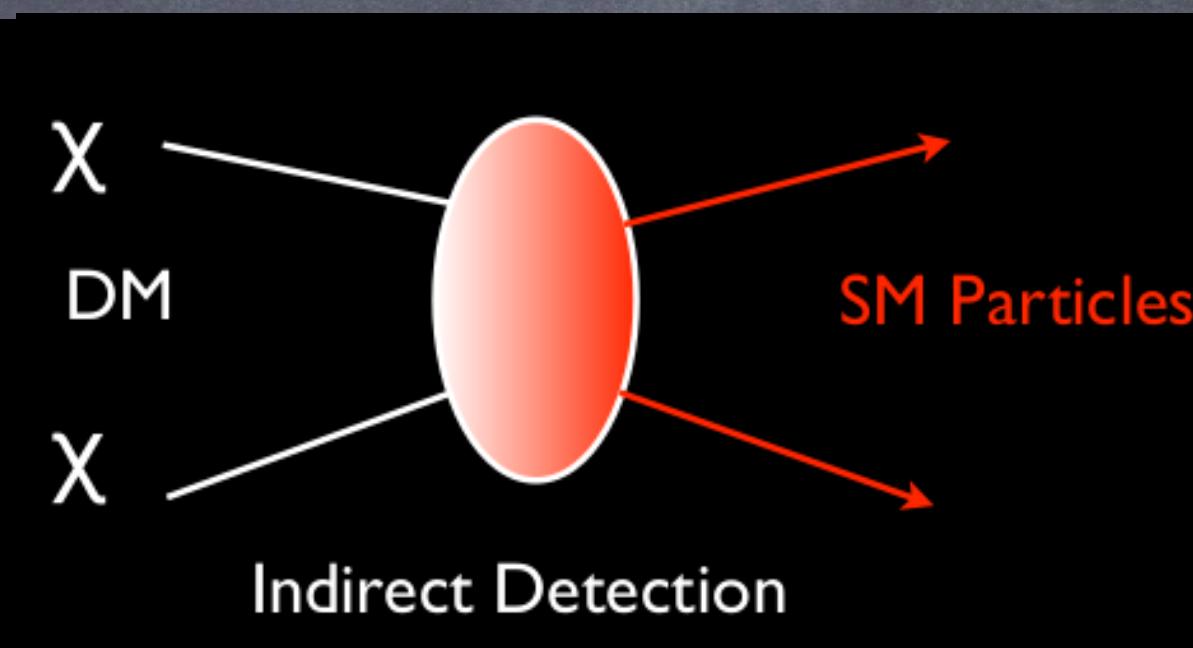
Signature: radiations.



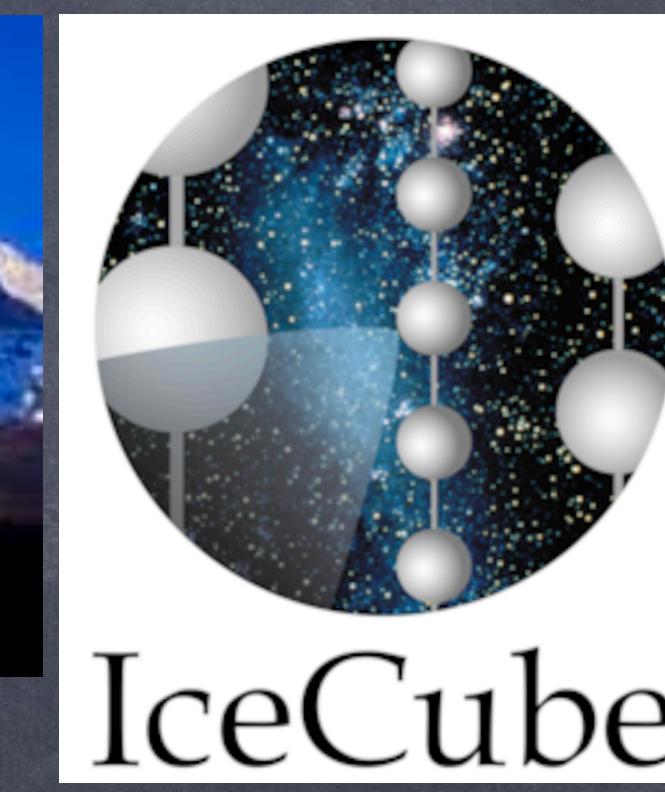
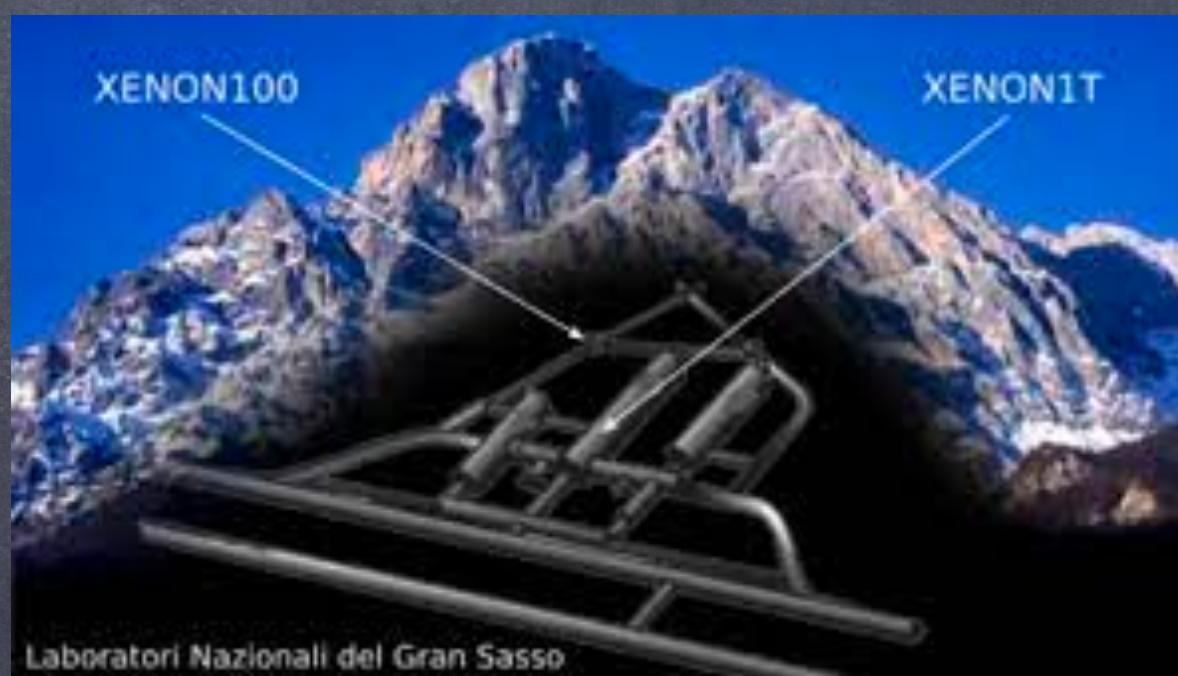
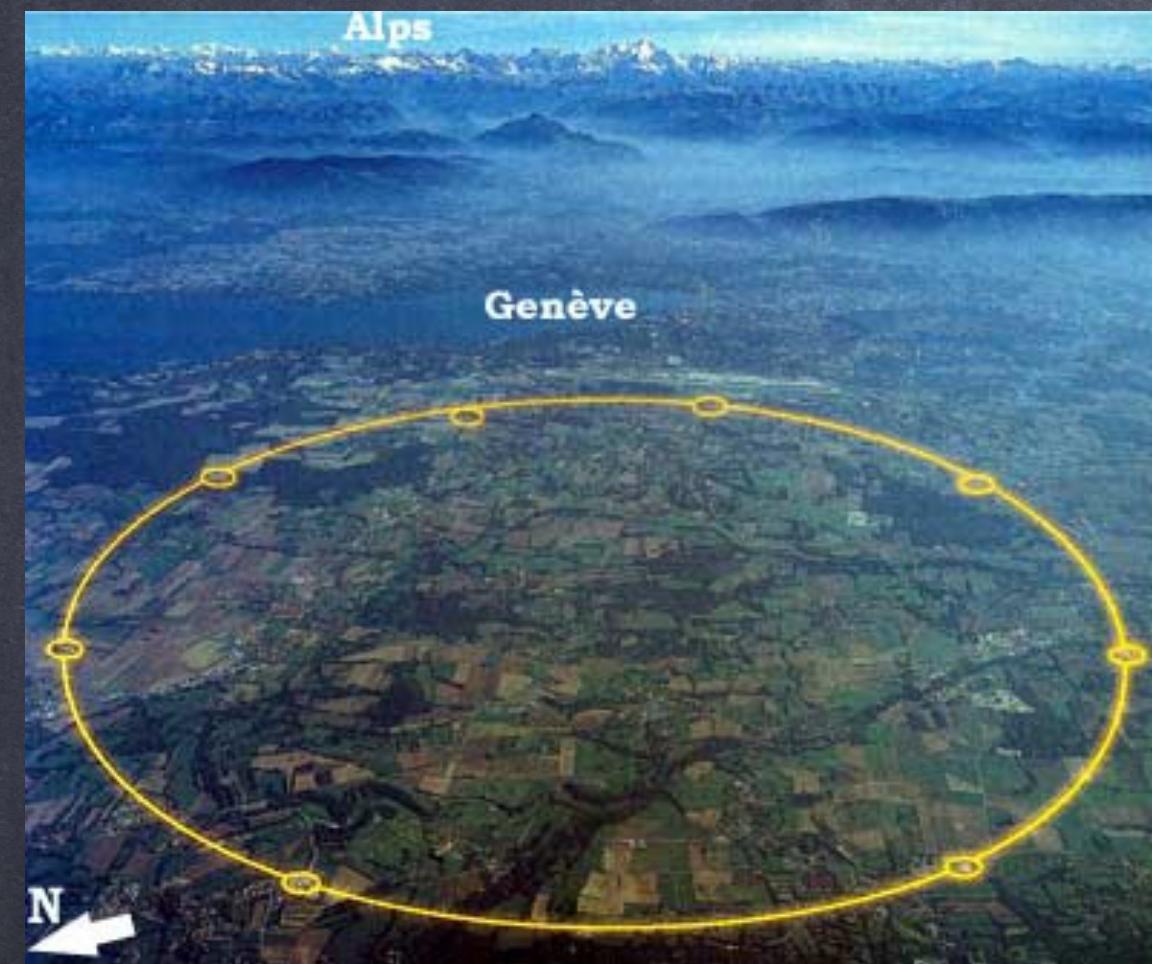
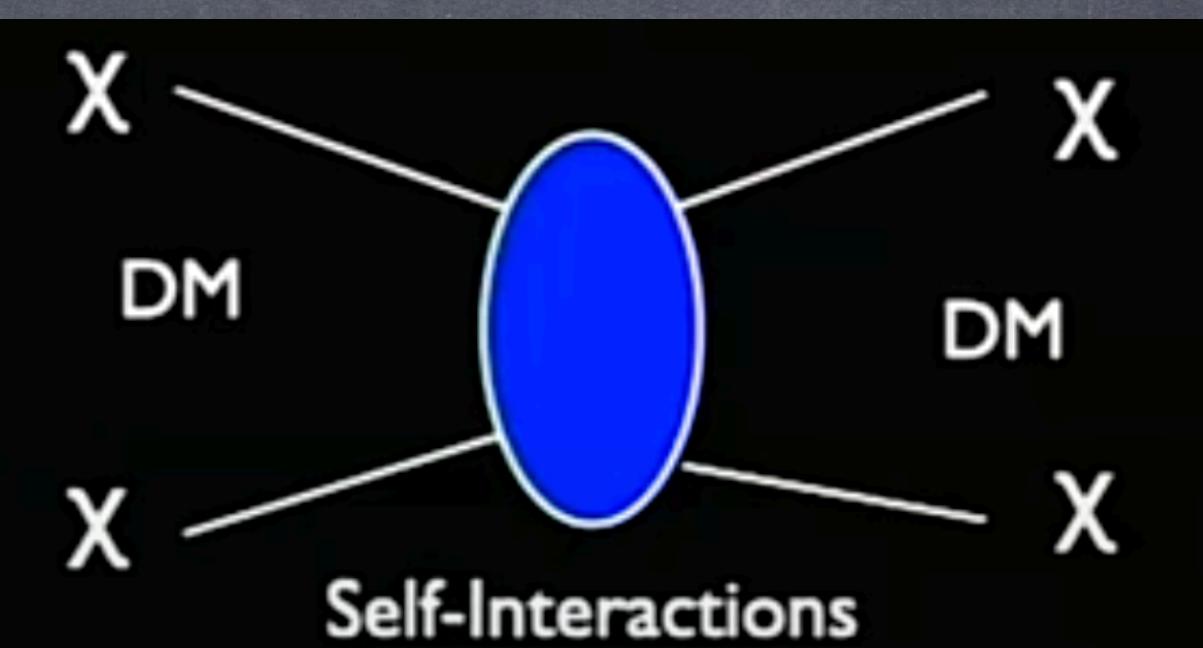
Signature: recoiled energies.



Signature: stable SM
($e^+, p, \gamma, \nu, \dots$).



Astrophysical structure
of the Universe.



This project!

Pictures for the processes are taken from Tim Tait's slide of KITP Snowmass2022.

Neutron Stars in Galactic Center



- Make from neutrons: $m_n = 1.0 \text{ GeV}$.
- Mass: $M_{\text{ns}} \approx 1.5 M_{\odot}$, Radius: $R_{\text{ns}} \approx 10 \text{ km}$.
- (Blueshift) Escape velocity:

$$v_{\text{esc}} = \sqrt{2\chi} \approx 2.1 \times 10^5 \text{ km/s}, \quad (1)$$

$$\text{with } \chi = 1 - \sqrt{1 - 2G_N M_{\text{ns}} / R_{\text{ns}}}. \quad (2)$$

- Saturation Cross Section:

$$\sigma_{\text{sat}} = \pi R_{\text{n}}^2 / N_n \approx 1.87 \times 10^{-45} \text{ cm}^2. \quad (3)$$

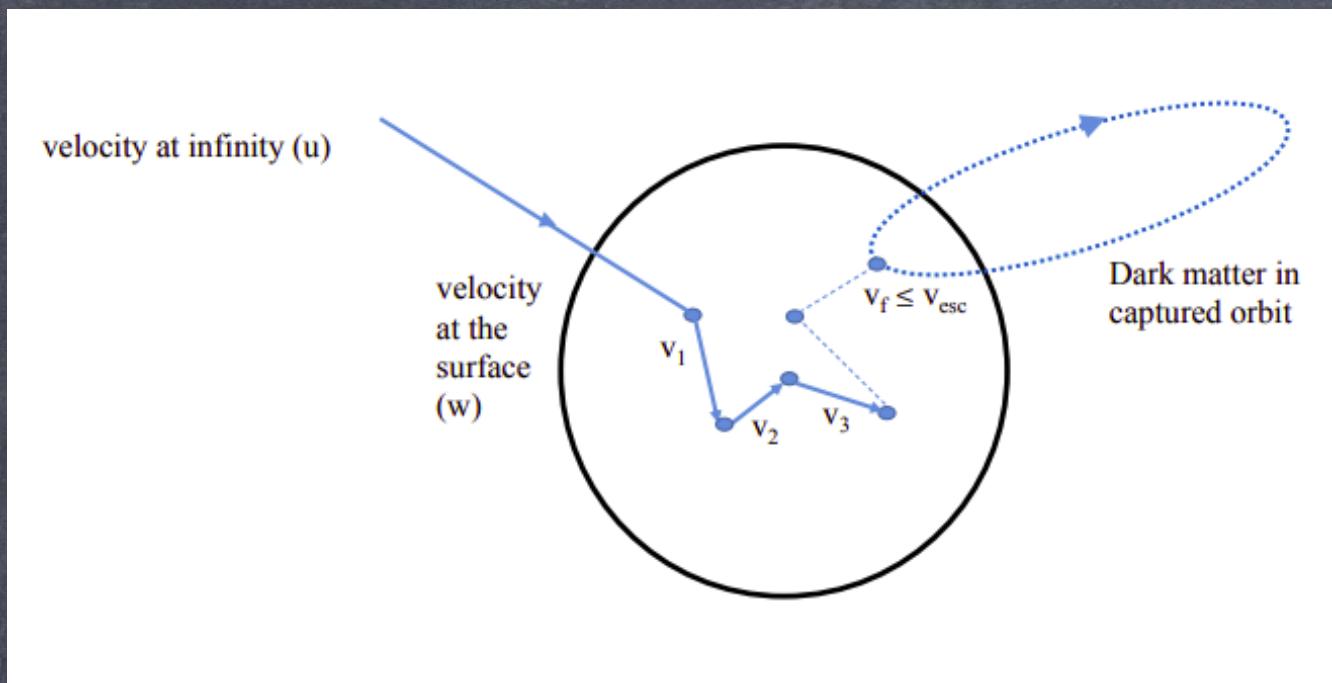
Neutron Star's number density¹ in Galactic Center:

$$\begin{aligned} n_{\text{ns}}(r) &= 5.98 \times 10^3 \left(\frac{r}{1 \text{ pc}} \right)^{-1.7} \text{ pc}^{-3} \quad (0.1 \text{ pc} < r < 2 \text{ pc}) \\ &= 2.08 \times 10^4 \left(\frac{r}{1 \text{ pc}} \right)^{-3.5} \text{ pc}^{-3} \quad (r > 2 \text{ pc}). \end{aligned} \quad (4)$$

1. This density is extracted from Fig. 2 of arXiv:1804.01543.

Dark Matter capture by neutron stars

Figure from arXiv:1906.04204



$v_f \leq v_{\text{esc}} \Rightarrow \text{Captured!}$

- DM velocity dispersion: \bar{v} .
- DM velocity (Nth-time scattering): v_N .
- DM density profile: n_χ .

Dark Matter Capture Rate after Nth times [GeV]:

$$C_N = \frac{\pi R_\star p_N(\tau)}{1 - 2G_N M_\star / R_\star} \frac{\sqrt{6} n_\chi}{3\sqrt{\pi}\bar{v}} \times \left[2\bar{v}^2 + 3v_{\text{esc}}^2 - (2\bar{v}^2 + 3v_N^2) \exp\left(-\frac{3(v_N^2 - v_{\text{esc}}^2)}{2\bar{v}^2}\right) \right]. \quad (5)$$

- Capture rate (1 NS): $C = \sum_{N=1}^{\infty} C_N$. (6)

- Total capture rate (ALL NSS): $C_{\text{tot}} = 4\pi \int_{r_1=0.1\text{pc}}^{r_2=100\text{pc}} r^2 n_{\text{ns}} C dr$. (7)

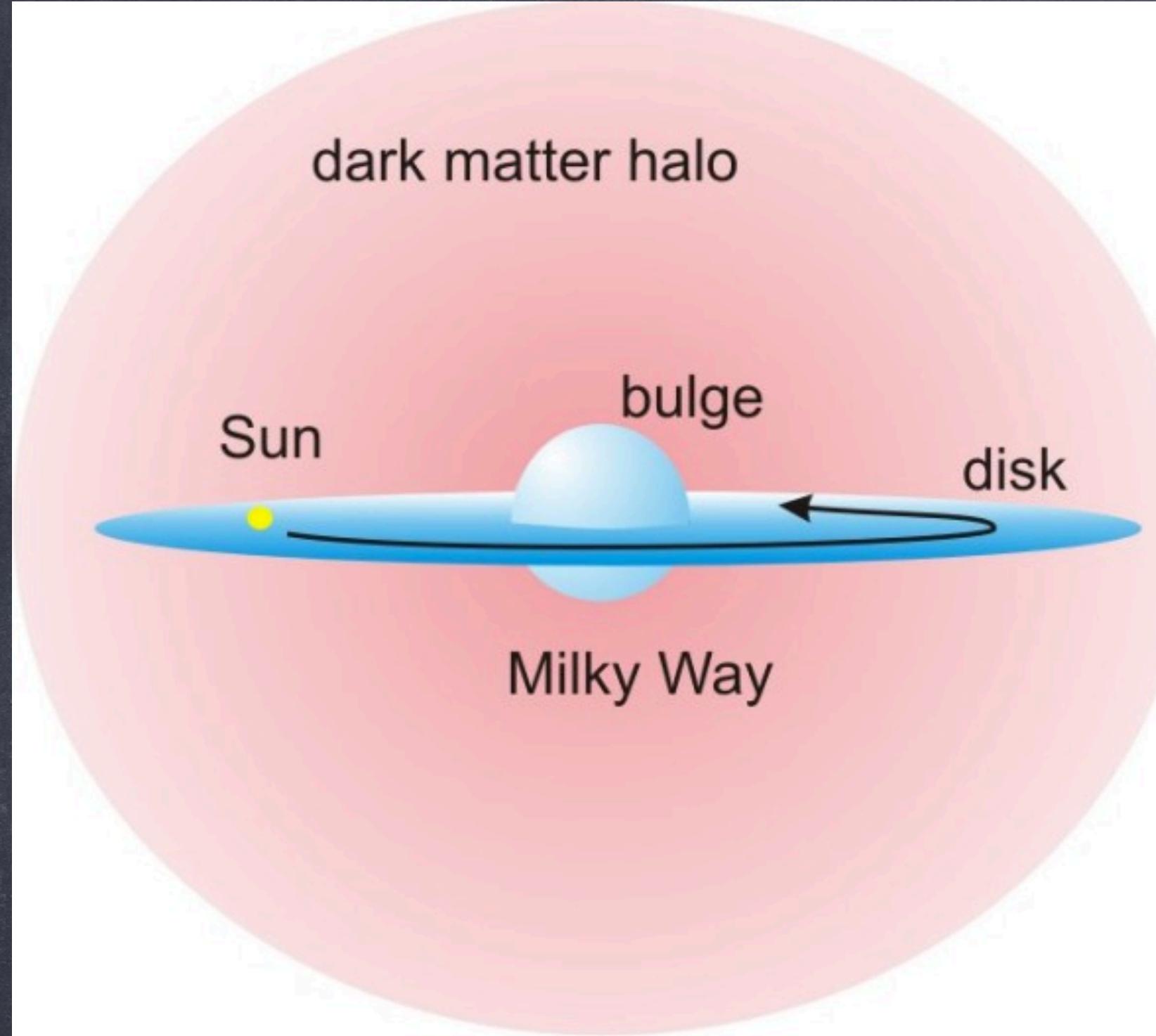
- Probability scattering N-time:

$$p_N(\tau) = 2 \int_0^\infty dy \frac{ye^{-y\tau}(y\tau)^N}{N!}$$

Optical Depth: $\tau = 1.5 \frac{\sigma_{\chi n}}{\sigma_{\text{sat}}} \rightarrow \text{DM model.}$
 $\tau = 1.5 \frac{\sigma_{\chi n}}{\sigma_{\text{sat}}} \rightarrow \text{Celestial object.}$

Milky Way Galaxy

(Credit: <https://scienceblogs.com>)



$$\rho_\chi(r) = \rho_{\text{NFW}}(r) = m_\chi n_\chi(r) = \frac{\rho_0}{(r/r_s)^\gamma (1+r/r_s)^{3-\gamma}}.$$

(arXiv:9508025)

(arXiv:1301.8241)

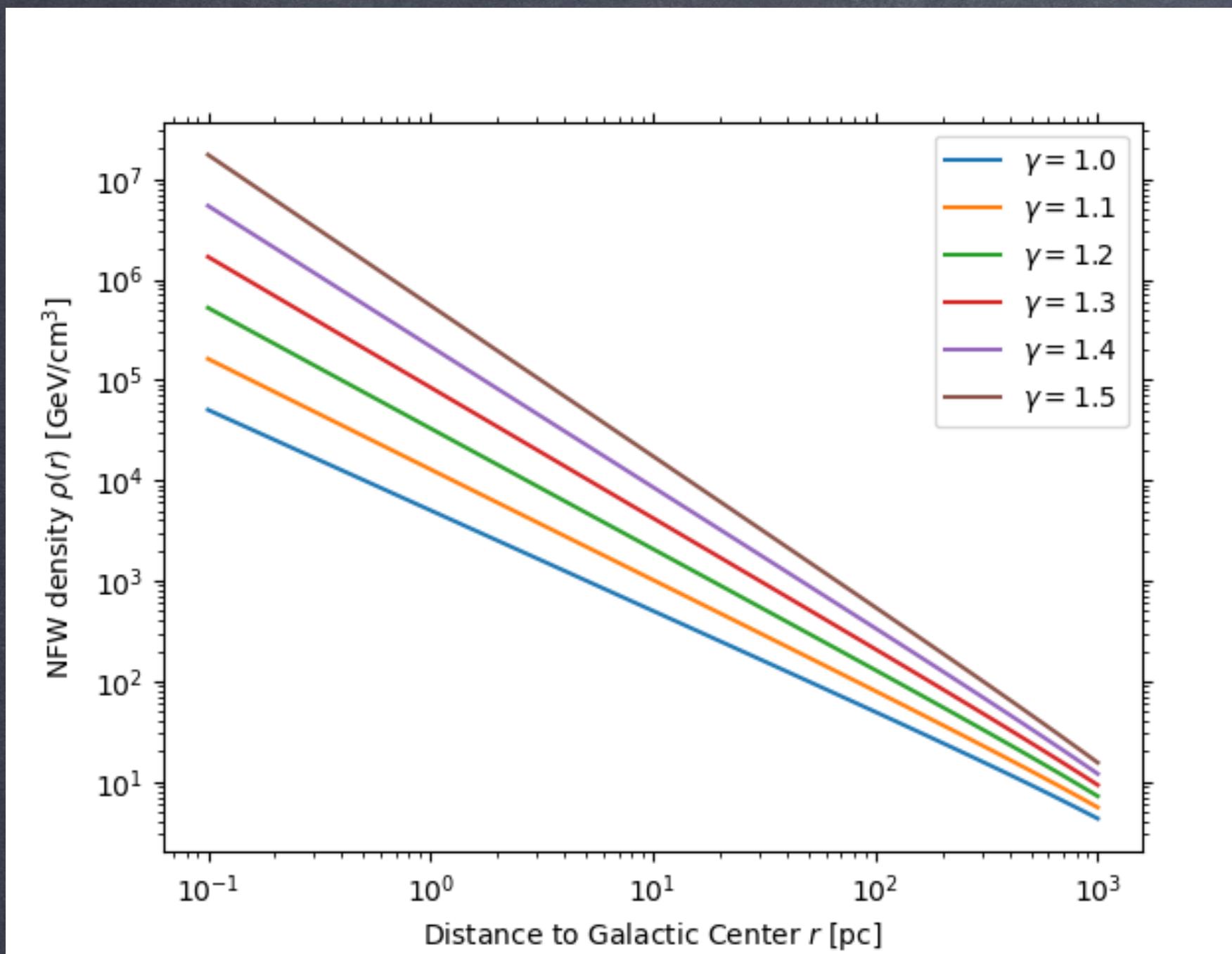
Mass component	Total Mass (M_\odot)	Scale radius (kpc)	Center density ($M_\odot \text{pc}^{-3}$)
Black hole	4×10^6	—	—
Inner bugle (core)	5.0×10^7	0.0038	3.6×10^4
Main Bugle	8.4×10^9	0.12	1.9×10^2
Disk	4.4×10^{10}	3.0	15
Dark halo	5×10^{10} ($r \leq h$)	$h = 12.0$	$\rho_0 = 0.011$

$$M(r) = M_{\text{BH}} + 4\pi \int_0^r (\rho_{\text{inner}} + \rho_{\text{outer}} + \rho_{\text{disk}} + \rho_\chi) r^2 dr. \quad (8)$$

- $\rho_0 = 0.42 \text{ GeV/cm}^3$.
- $r_s = 12.0 \text{ kpc}$.
- γ : Inner Slope (1-1.5).

Milky Way Galaxy

(arXiv:1301.8241)



Mass component	Total Mass (M_{\odot})	Scale radius (kpc)	Center density ($M_{\odot}\text{pc}^{-3}$)
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DM velocity dispersion: $\bar{v}(r) = \sqrt{\frac{3}{2}} v_c(r) = \sqrt{\frac{3}{2}} \sqrt{\frac{G_N M(r)}{r}}. \quad (9)$

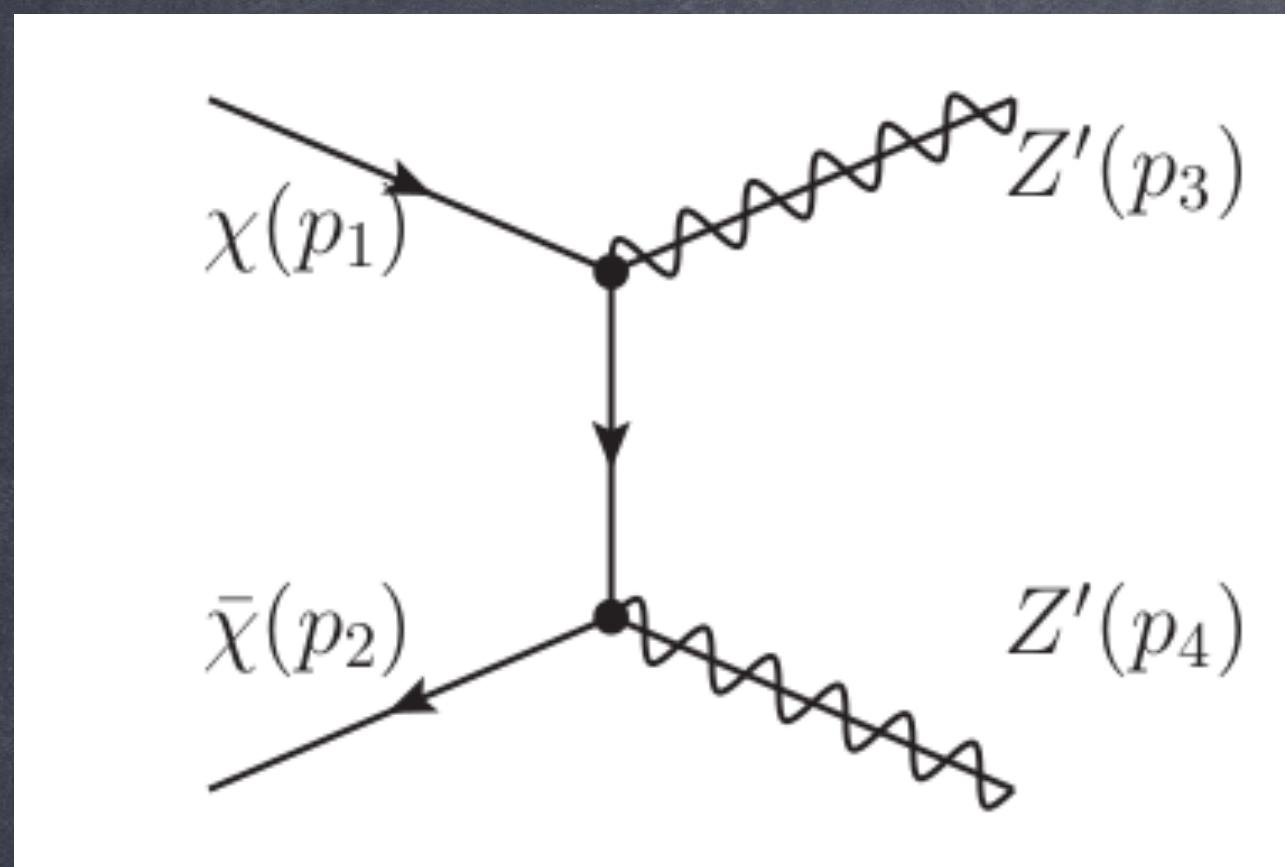
$$\rho_{\chi}(r) = \rho_{\text{NFW}}(r) = m_{\chi} n_{\chi}(r) = \frac{\rho_0}{(r/r_s)^{\gamma} (1+r/r_s)^{3-\gamma}}.$$

(arXiv:9508025)

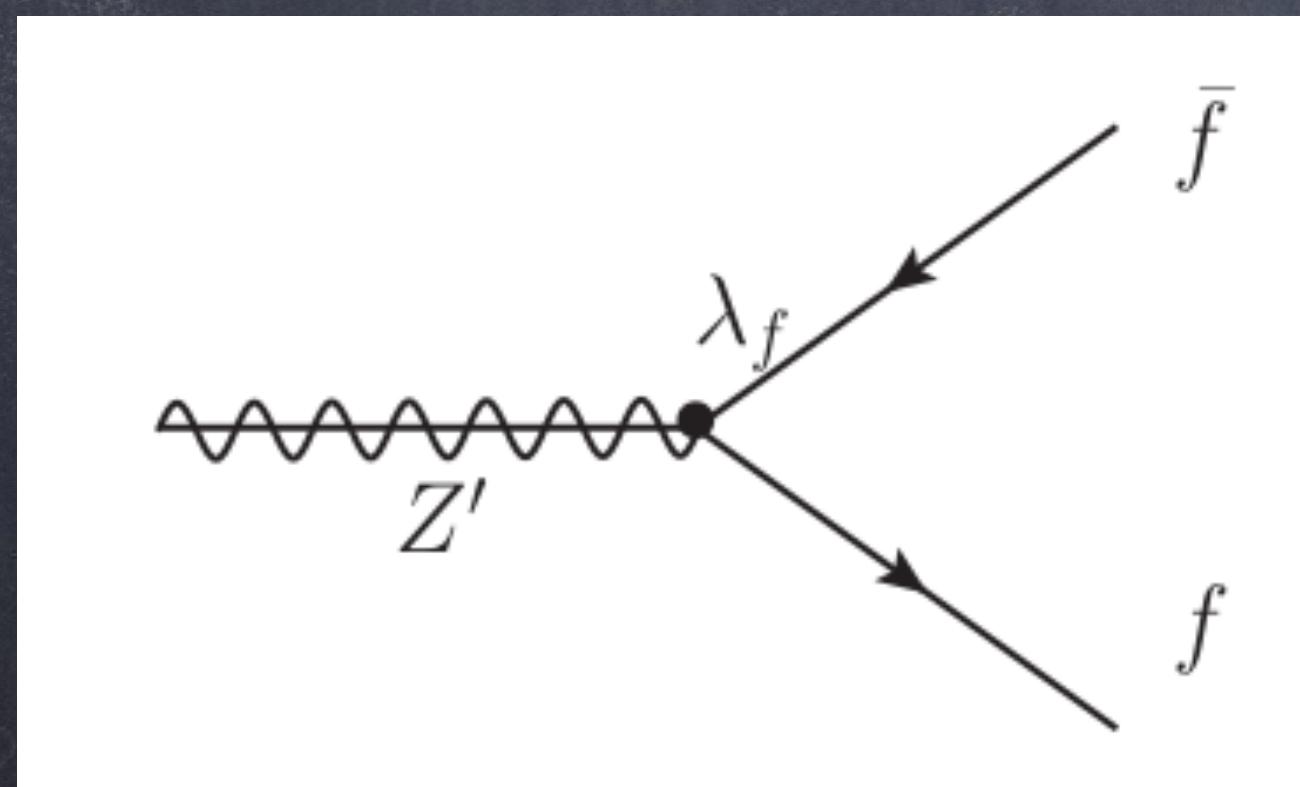
- $\rho_0 = 0.42 \text{ GeV/cm}^3$.
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Signal from DM annihilation in NS

DM annihilation in NS



Mediator live long enough! 🤝



Mediator decays to SM particles

$$\text{Equilibrium: } \Gamma_{\text{ann}} = \frac{\Gamma_{\text{cap}}}{2} = \frac{C_{\text{tot}}}{2}. \quad (10)$$

- Lorentz Boost: $\eta \approx m_\chi/m_{Z'}$. (11)

- Escaping condition: $L = \eta\beta\tau_m \approx \eta c\tau_m > R_\star$. (12)

Differential Energy Flux (measured by 1D Experiments):

$$E^2 \frac{d\Phi}{dE} = \frac{\Gamma_{\text{ann}}}{4\pi D^2} \times E^2 \frac{dN}{dE} \times \text{BR}(X \rightarrow \text{SM}) \times P_{\text{surv}}. \quad (13)$$

$[\text{GeV cm}^{-2} \text{ s}^{-1}]$

- D : Average distance from GC to detectors (Earth).
- dN/dE : Signal (neutrino) spectrum.
- Signal surviving probability: $P_{\text{surv}} = e^{-R_\star/L} - e^{-D/L}$. (14)
- Limit: $L \leq D \approx 8.0$ kpc. (15)

Neutrinos experimental results

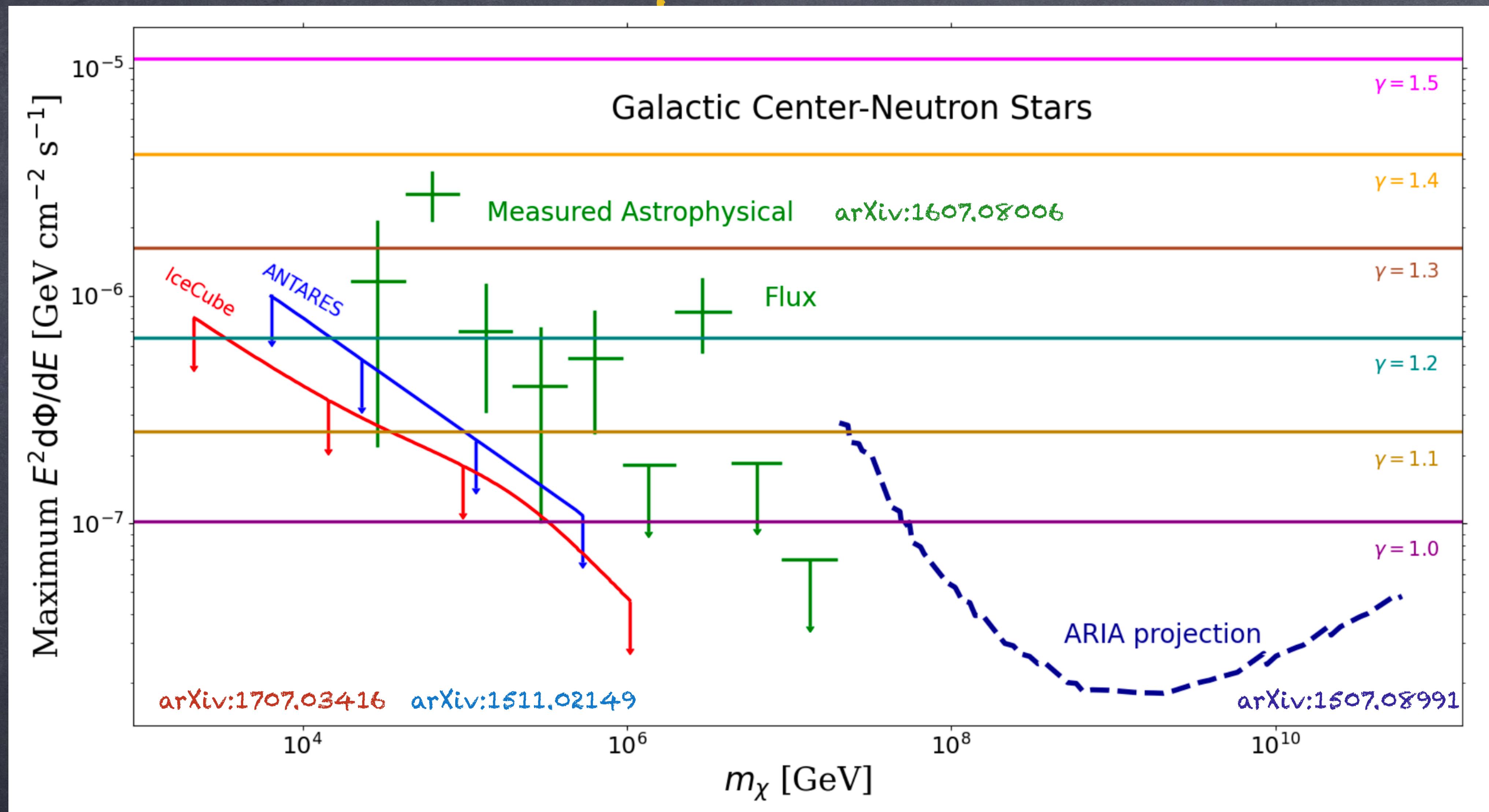
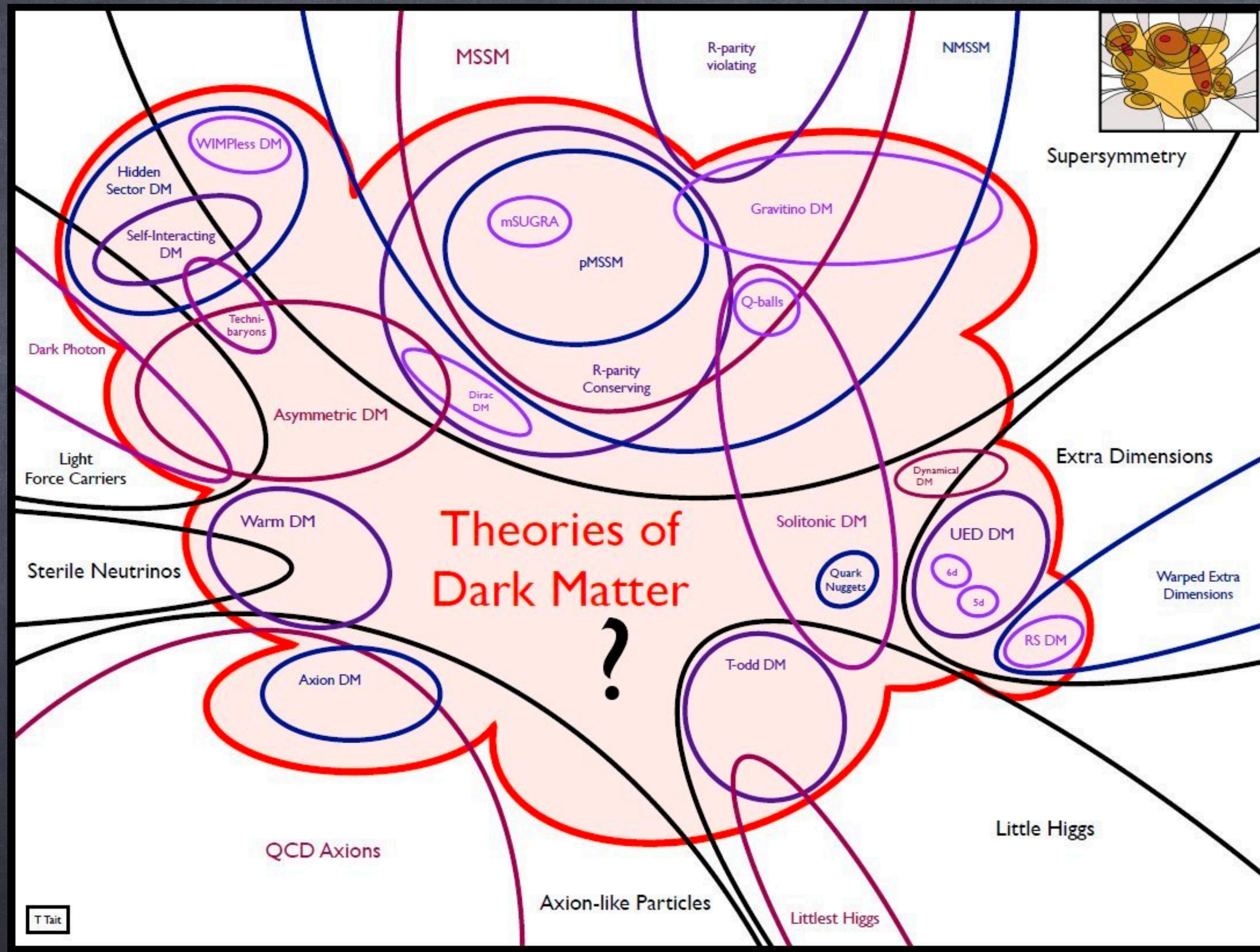


Fig. 1: Differential Energy Flux of muon neutrino: Experimental upper Limits and data. The horizontal lines for maximum fluxes from NS in GC after integrate all over the sky.

Which DM model?

Our consideration



Dark Matter model

$$SU(2)_L \times U(1)_Y \times U(1)_X$$

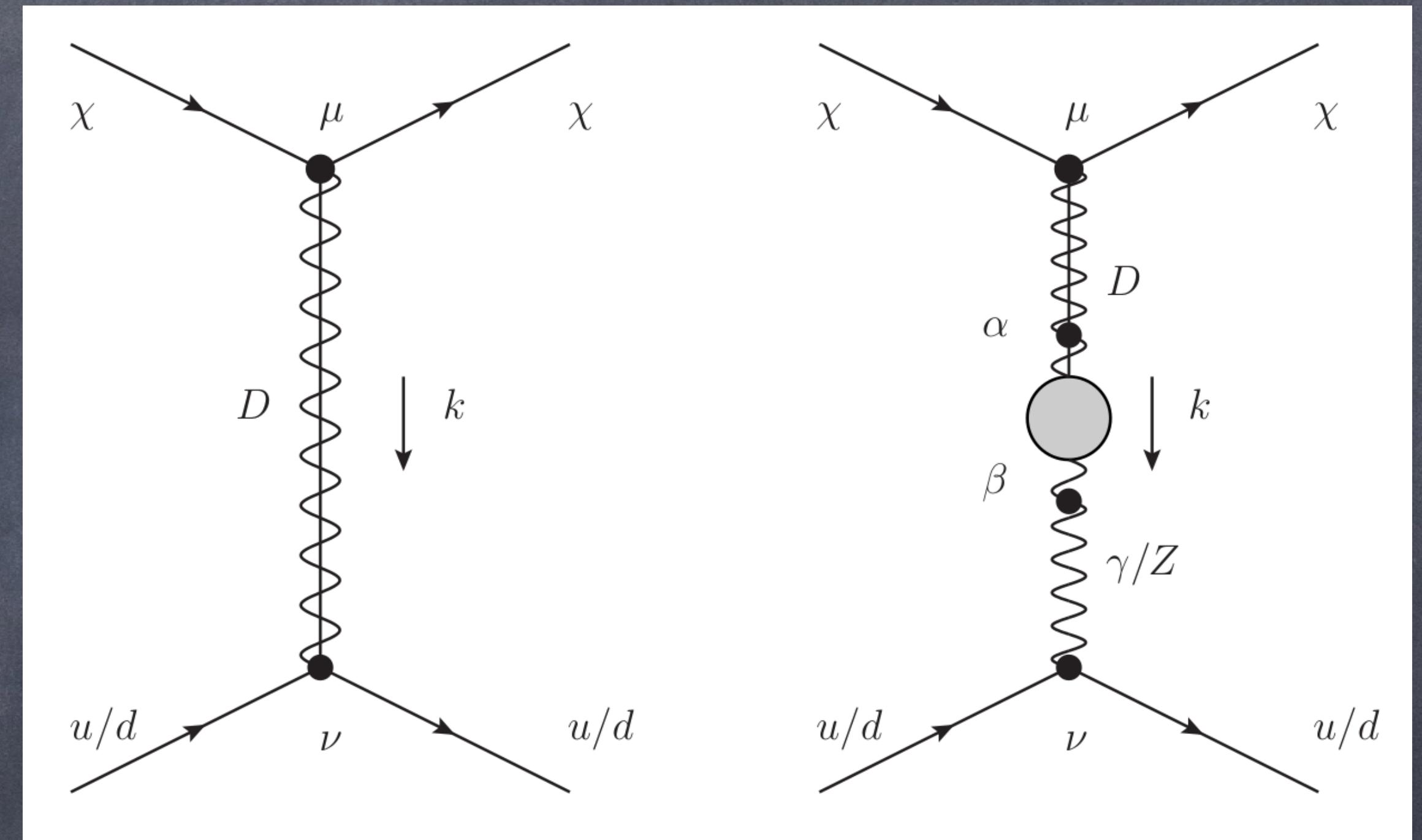
$$\begin{aligned} \mathcal{L} \supset & -\frac{1}{4} \mathcal{D}_{\mu\nu} \mathcal{D}^{\mu\nu} - \frac{\epsilon}{2} B_{\mu\nu} \mathcal{D}^{\mu\nu} \\ & + \bar{\chi} (i\gamma^\mu D_\mu - m_\chi) \chi. \end{aligned} \quad (16)$$

- Kinetic mixing coupling: ϵ
 - Dark photon:
- $$\mathcal{D}_{\mu\nu} = \partial_\mu \mathcal{D}_\nu - \partial_\nu \mathcal{D}_\mu.$$
- Covariant derivative:

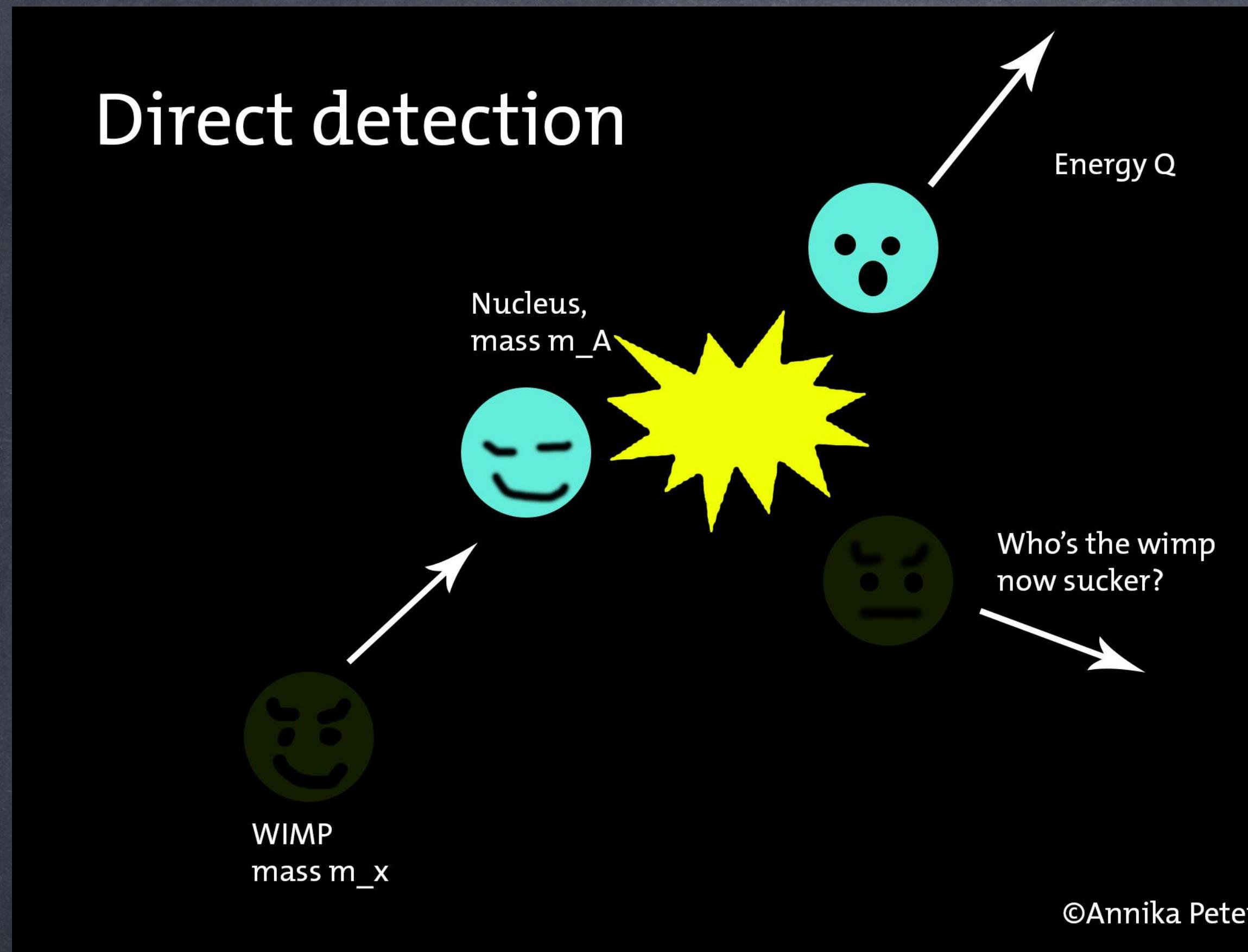
$$D_\mu = \partial_\mu - ig_2 \sum_{a=1}^3 T^a W_\mu^a - ig_1 \frac{Y}{2} B_\mu - ig_x \frac{X}{2} \mathcal{D}_\mu.$$

 Only acts on SM

Mediator can interact with DM and SM



Dark Matter-nucleon cross section



$$\sigma_{\chi n} = \frac{b_n^2 \mu_{\chi n}^2}{\pi} \text{ with } \begin{cases} b_n &= \frac{\lambda \chi (\lambda_u + 2\lambda_d)}{m_{Z'}^2} \\ \mu_{\chi n} &= \frac{m_\chi m_n}{m_\chi + m_n} \end{cases} \quad (17)$$

- $\lambda_{\chi f}$: Mediator-DM/SM coupling.
- b_n : Mediator-neutron coupling.
- $m_{Z'}$: Mediator mass.
- $\mu_{\chi n}$: DM-neutron reduced mass.

Non-relativistic Scattering

3. More detail in Prof. Tongyan Lin's lecture note ([arXiv:1904.07915](https://arxiv.org/abs/1904.07915))

(SI) Cross Section Limits

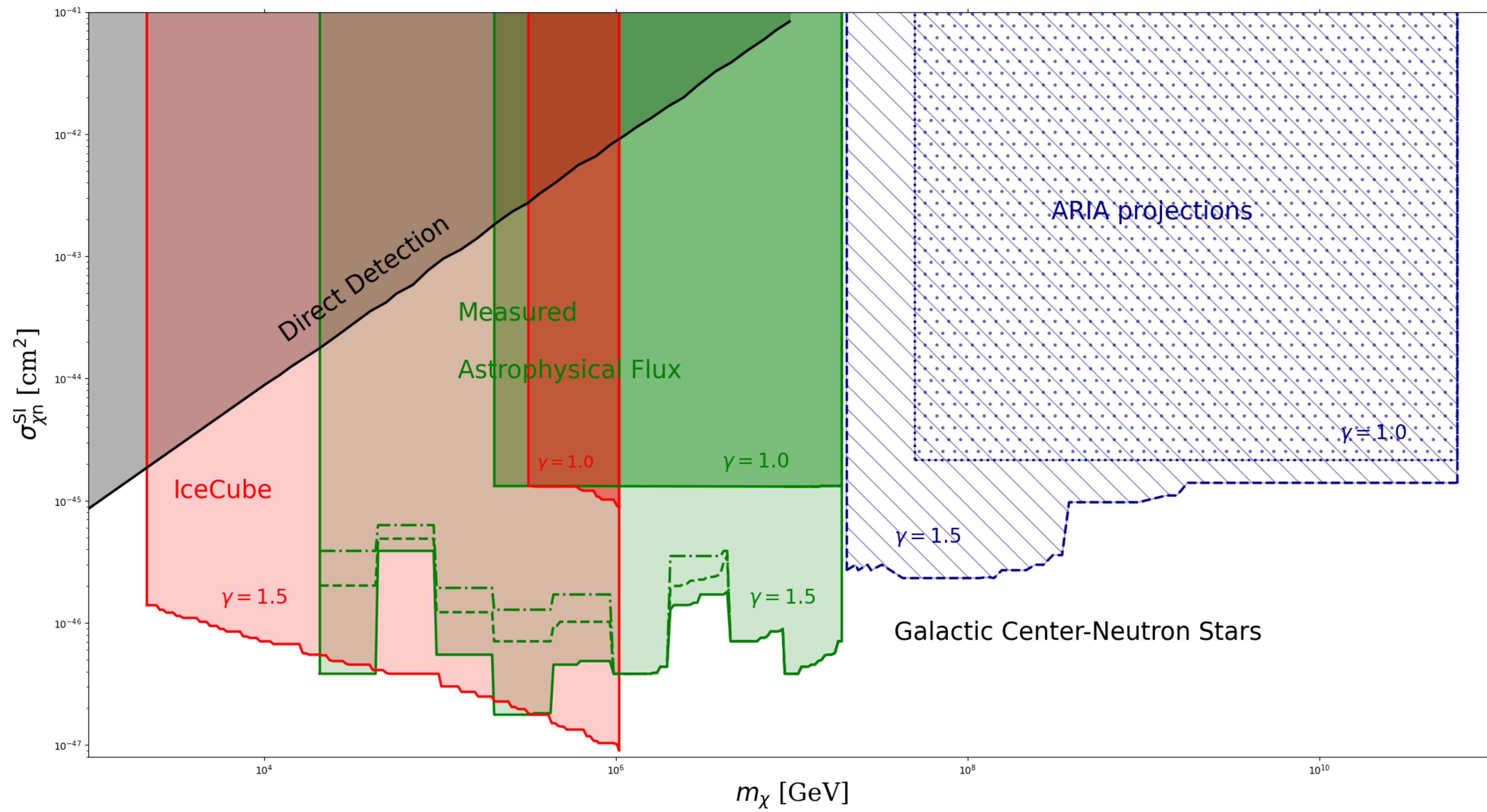


Fig. 2: SI Cross Section Limits, using IceCube, Measured Astrophysical (muon) Neutrino, and ARIA projection.

Take home message

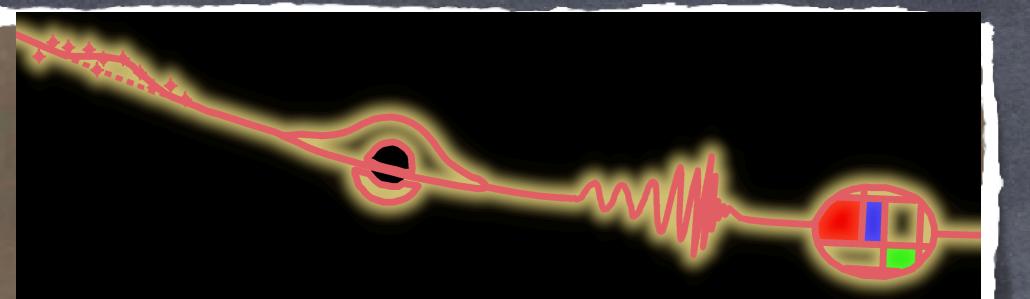
- Neutron Stars can help us investigate Long-lived Dark Matter Mediator models.
- With Light Z'-model and current IceCube result, the bounds for SI Cross Section of DM-neutron can be pushed down to $10^{-46} - 10^{-47}$ cm² (TeV - PeV mass range).
- Can use other celestial objects with large number in Galactic Center: Brown Dwarfs, White Dwarfs, ...
- Motivation for experimental results: ARIANNA, K3MNet, IceCube Gen2, ...

Acknowledgements

We would like to thanks:

- Rebecca Leane, Payel Mukhopadhyay, Natalie Toro (SLAC, Stanford) and Tim Linden (Stockholm U., OKC): capture rate calculation.
- Nicholas Rodd (CERN): neutrino spectrum.
- Meng-Ru Wu (IoP, Academia Sinica): neutrino flavor ratios.





Thank you for listening!

I'm searching for
Dog-Matter too!!



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BRACE YOURSELF



BACKUP SLIDES ARE COMING

memegenerator.net

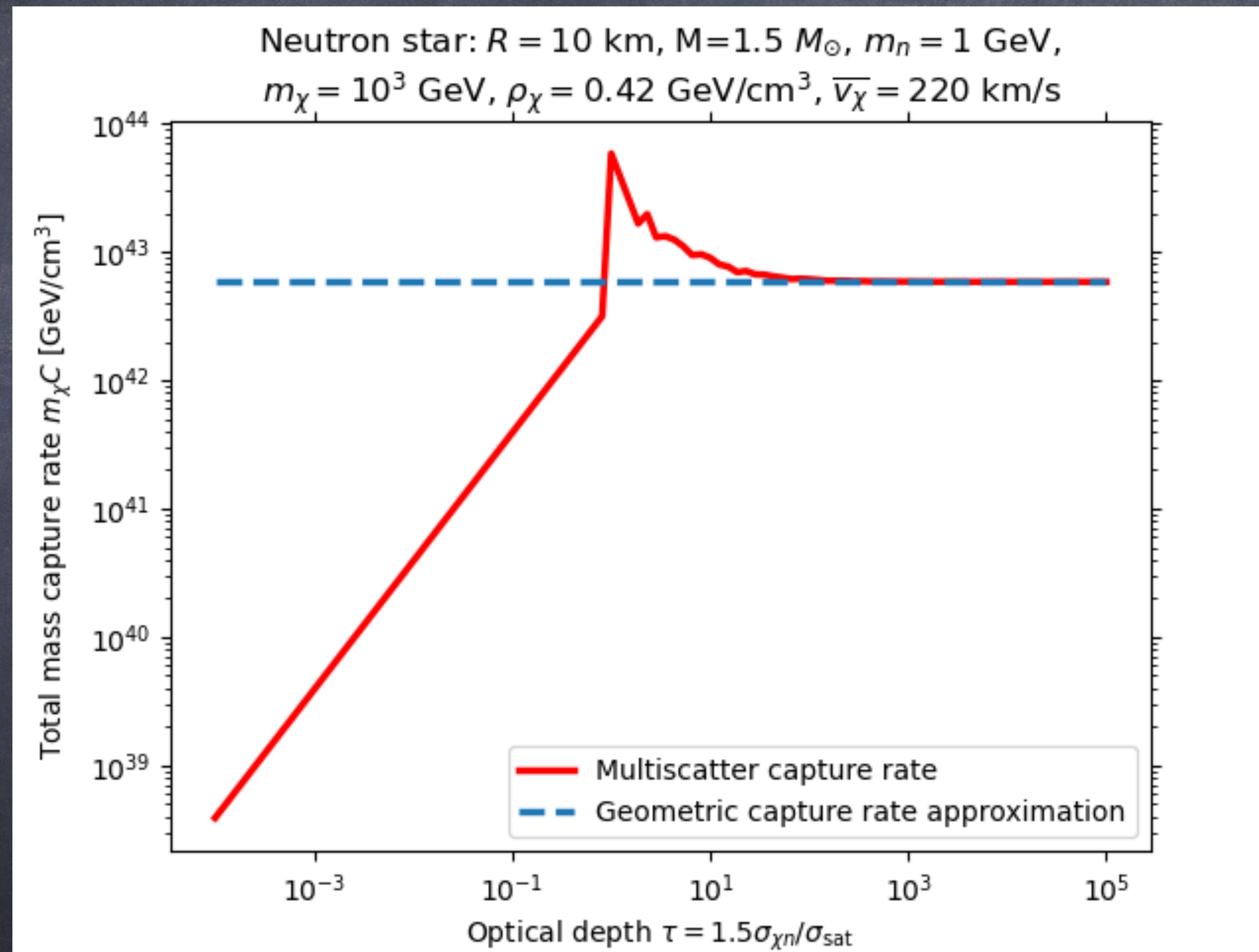
What is the optical depth?

- For multiscatter capture it is convenient to define the optical depth, the average number of times a dark matter particle with dark matter - nuclear cross section $\sigma_{\chi n}$ will scatter when traversing the star.
- To understand the $3/2$ factor in the optical depth, observe that the cross section for which 1 scatter occurs over a distance of $2R$, (where R is the radius of the star) is:

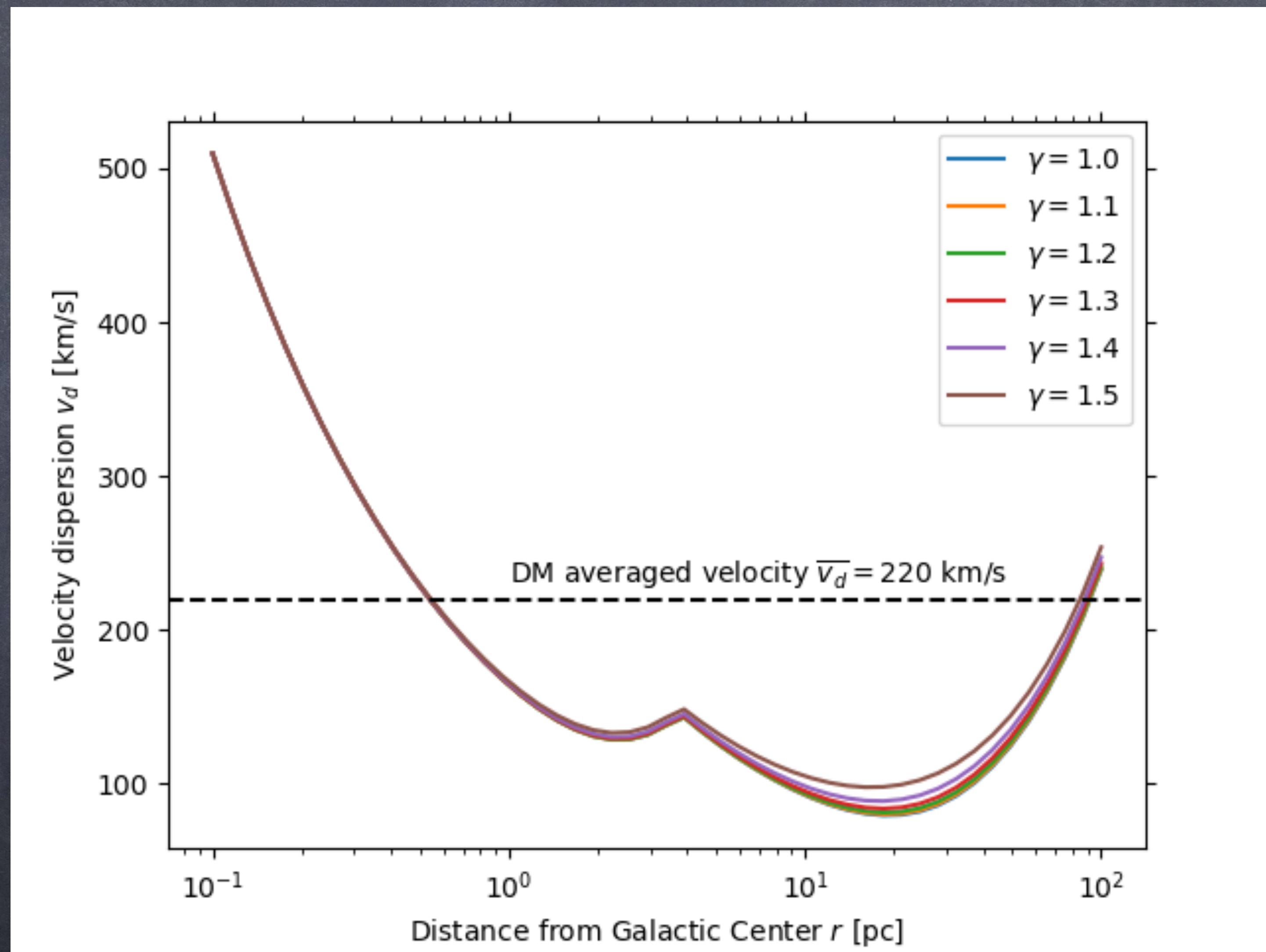
$$1 = n \sigma (2R) = \frac{N_n}{(4/3)\pi R^3} \sigma (2R) = \frac{3 N_n}{2\pi R^2} \sigma$$
$$\rightarrow \sigma = \frac{2}{3} \left(\frac{\pi R^2}{N_n} \right) = \frac{2}{3} \sigma_{\text{sat}},$$

arXiv:1703.04043

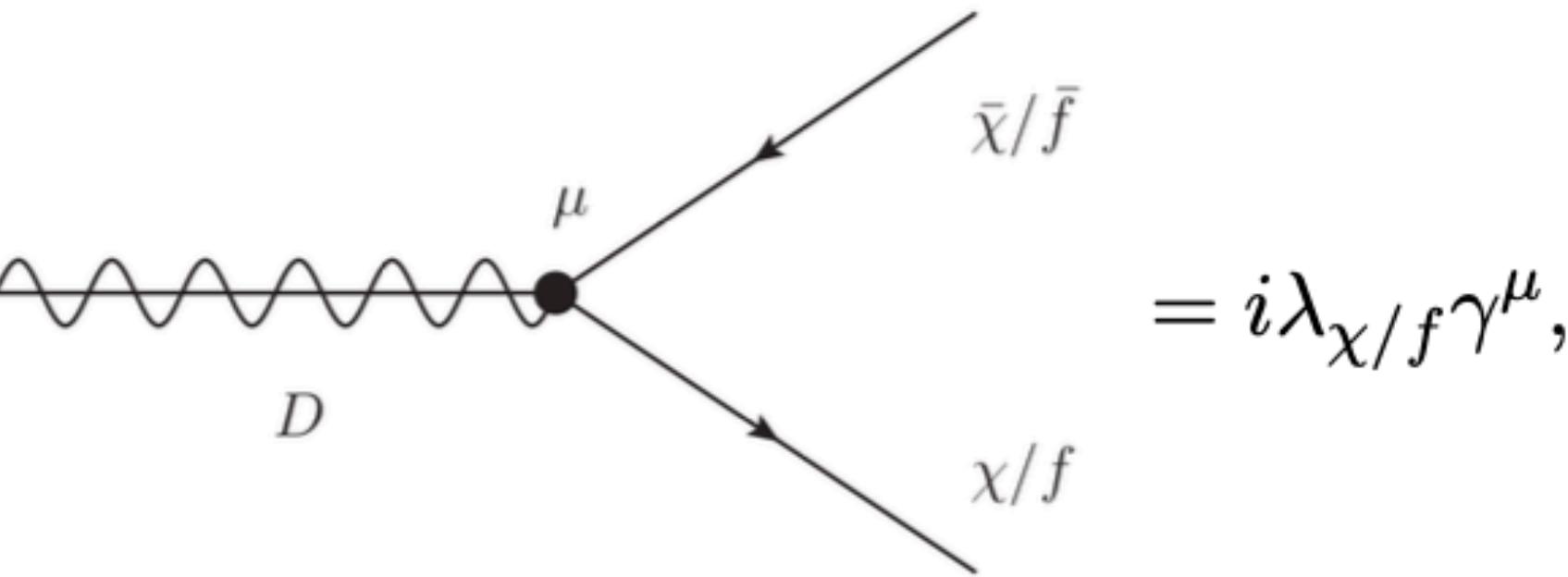
Capture Rate



Velocity Dispersions of NS in Galactic Center



Feynman rules



A Feynman diagram showing a wavy line labeled D with arrows indicating flow from left to right. The endpoints are marked with dots and labeled μ and ν above the line, and k and D below it. To the right of the line, the equation $= \frac{-ig_{\mu\nu}}{k^2 - m_D^2 + im_D\Gamma_D},$ is given.

A Feynman diagram showing a loop formed by a wavy line labeled D and a wavy line labeled γ/Z . The loop is closed by a shaded circle. The incoming wavy line has arrows pointing to the loop, with labels k and μ at the top, and D at the bottom. The outgoing wavy line has arrows pointing away from the loop, with labels ν and k at the top, and γ/Z at the bottom. To the right of the diagram, the equation is given as a piecewise function:

$$= \begin{cases} \gamma : & -i\epsilon_{\text{mix}} \cos \theta_w (k^2 g^{\mu\nu} - k^\mu k^\nu), \\ Z : & i\epsilon_{\text{mix}} \sin \theta_w (k^2 g^{\mu\nu} - k^\mu k^\nu), \end{cases}$$

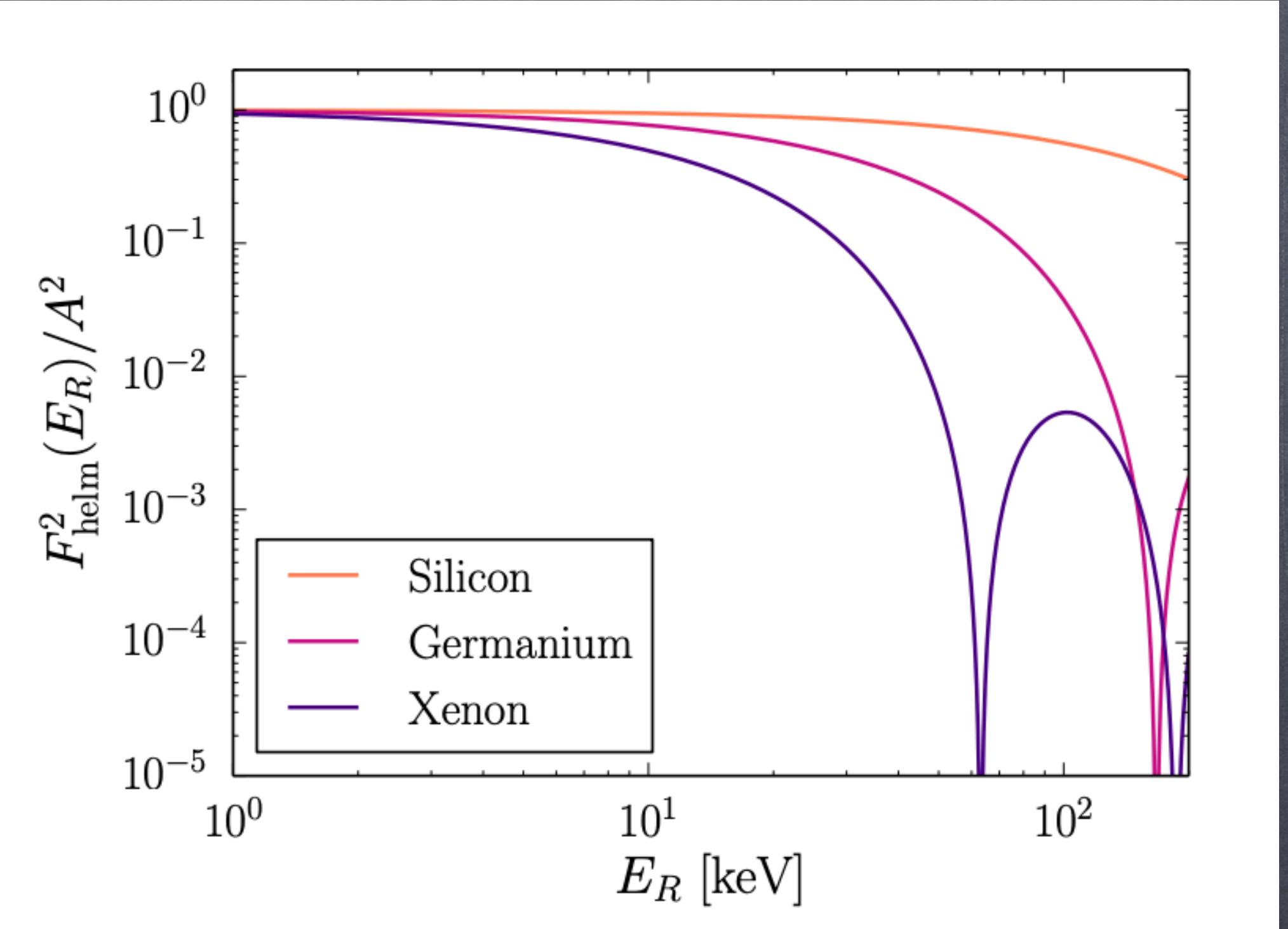
EFT: DM-nucleon scattering

$$\mathcal{M}_q^{\text{SI}} = \frac{i\lambda_\chi}{k^2 - m_D^2} \left[\lambda_q - eQ_q\epsilon_{\text{mix}}c_w + \frac{k^2}{k^2 - m_Z^2 + im_Z\Gamma_Z} \frac{es_w(I_3^q - 2Q_qs_w^2)}{2s_wc_w} \right] \times \\ \left[\bar{u}^{s'}(p_3)\gamma^\mu u^s(p_1) \right] \times \left[\bar{u}^{t'}(p_4)\gamma_\mu u^t(p_2) \right],$$

neutron: $\mathcal{M}_n = \frac{\lambda_\chi(\lambda_u + 2\lambda_d)}{m_D^2} \times (4m_\chi m_n) = b_n \times (4m_\chi m_n),$

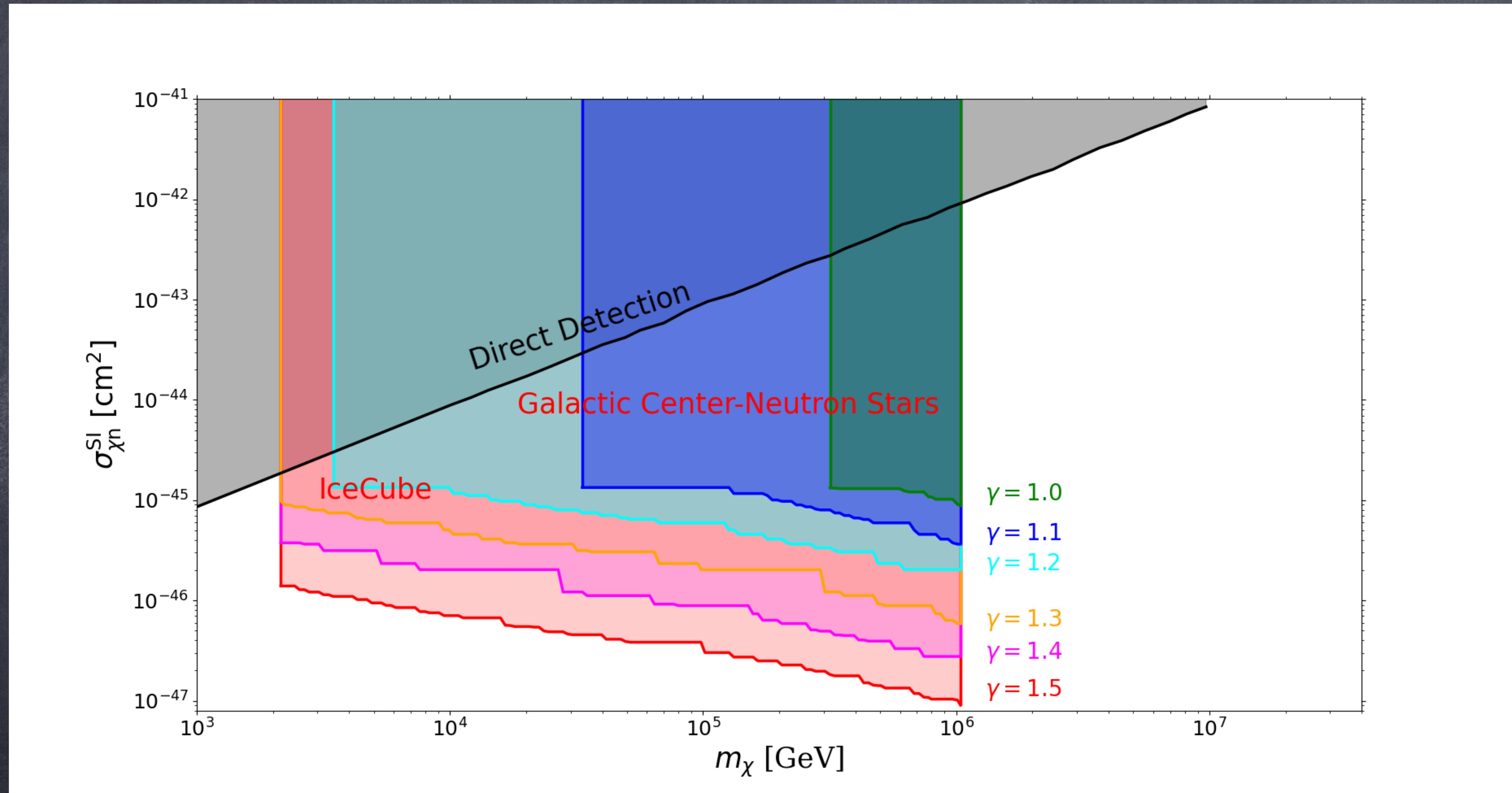
proton: $\mathcal{M}_p = \frac{\lambda_\chi(2\lambda_u + \lambda_d - ec_w\epsilon_{\text{mix}})}{m_D^2} \times (4m_\chi m_p) = b_p \times (4m_\chi m_p),$

$$d\sigma_n = \frac{|\mathcal{M}_n|^2}{4m_\chi m_n v} \frac{d^3\vec{p}_3}{(2\pi)^3 2m_\chi} \frac{d^3\vec{p}_4}{(2\pi)^3 2m_n} (2\pi)^4 \delta^{(4)}(p_1 + p_2 - p_3 - p_4) \\ = \frac{b_n^2}{4\pi v^2} d|\vec{p}_4|^2 d\cos\theta \times \delta\left(\cos\theta - \frac{|\vec{p}_4|}{2\mu_{\chi n} v}\right),$$



Dark Photon mass	m_D	$10^{-9} - 10^{-3}$	GeV
Dark matter mass	m_χ	$10^3 - 10^{11}$	GeV
Couplings	$\lambda_{\chi/f}, \epsilon$	$10^{-15} - 10^{-3}$	

Bounds from IceCube



Bounds from Data

