

A 3D rendering of a graphene lattice structure, showing a hexagonal arrangement of dark grey spheres (atoms) connected by thin lines (bonds). The perspective is from an angle, looking down at the lattice, which recedes into the distance.

Detection of Super-Light DM Using Graphene-based Sensor

with D. Kim, K.C. Fong & G.-H. Lee [arXiv: 2002.07821 & In preparation]

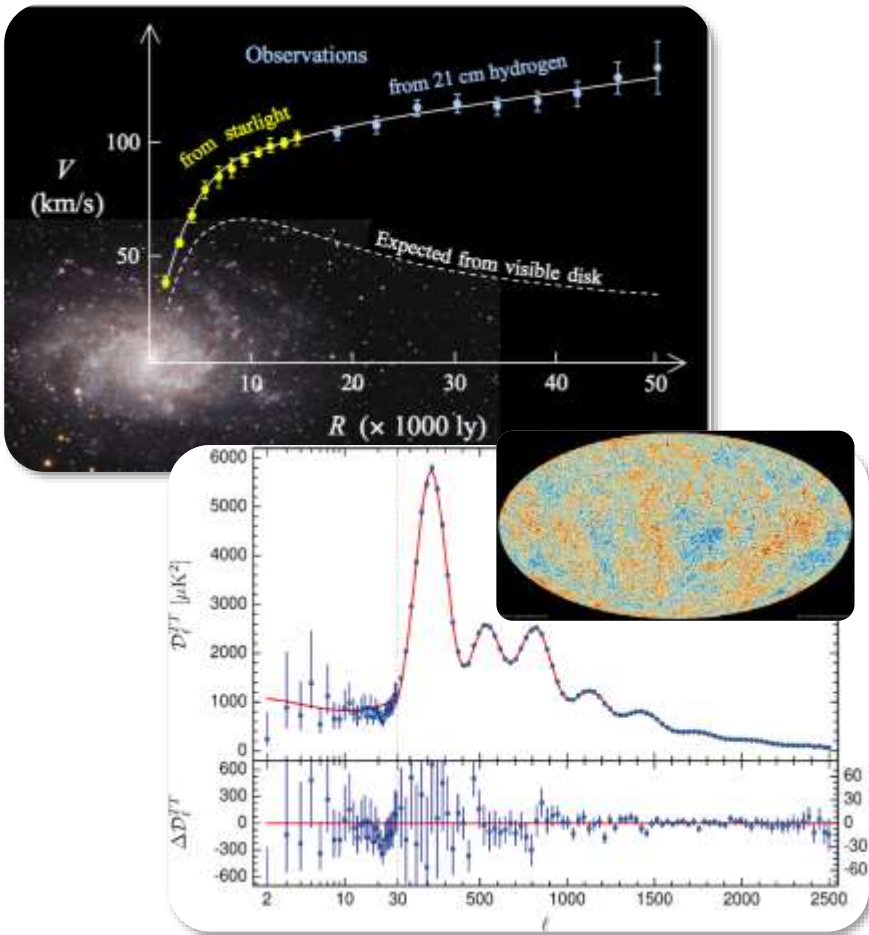
Jong-Chul Park



International Joint Workshop on the SM and Beyond

Why Light Dark Matter?

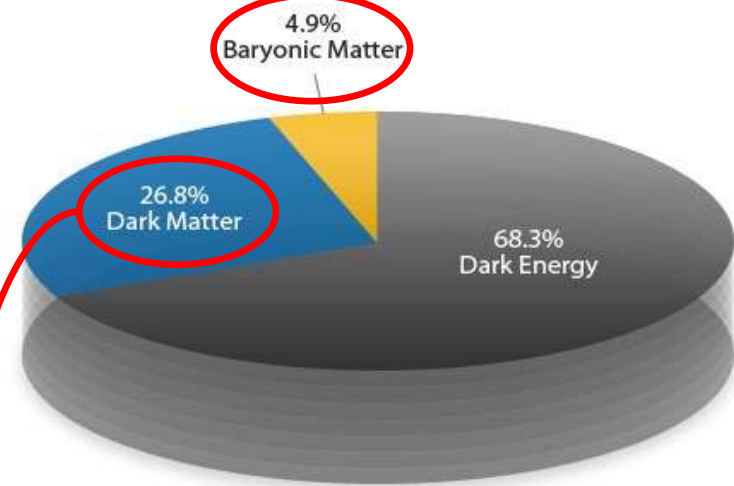
Dark Matter (DM)



- ❖ **Evidence:** Galactic rotation curve, Coma/Bullet cluster, Gravitational lensing, Structure formation, CMB, ...

❖ Modern cosmology:

The Standard Model



❖ Compelling paradigm:

- ✓ Massive,
- ✓ Non-relativistic ($v \ll c$),
- ✓ Non-luminous (no/tiny EM interaction),
- ✓ Stable particles

Classic Solution*: WIMP

Cosmological Lower Bound on Heavy-Neutrino Masses

Benjamin W. Lee^(a)

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and

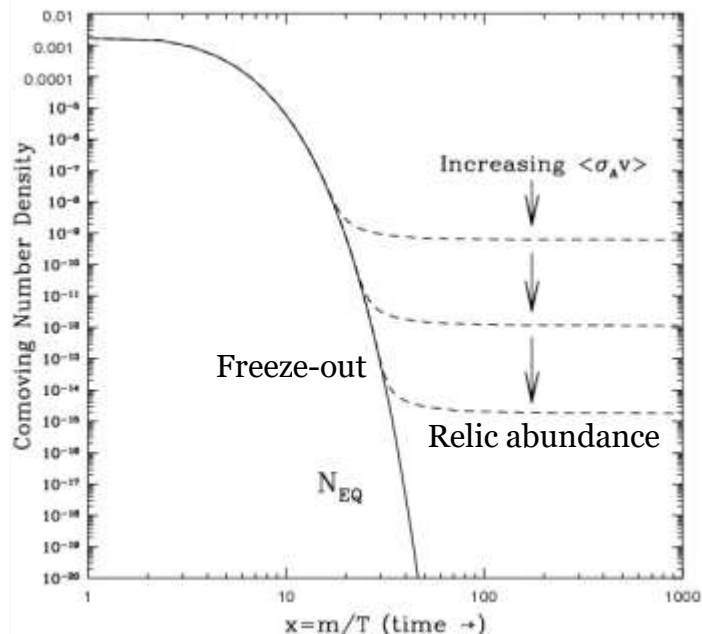
Steven Weinberg^(c)

Stanford University, Physics Department, Stanford, California 94305

(Received 13 May 1977)



The present cosmic mass density of possible stable neutral heavy leptons is calculated in a standard cosmological model. In order for this density not to exceed the upper limit of $2 \times 10^{-29} \text{ g/cm}^3$, the lepton mass would have to be *greater* than a lower bound of the order of 2 GeV.



➤ Correct thermal relic abundance:

$$\Omega h^2 \sim \frac{0.1 \text{ pb}}{\langle\sigma v\rangle} \text{ with } \langle\sigma v\rangle \sim \frac{\alpha_X^2 m_X^2}{M^4} \text{ (} M: \text{ dark scale/mediator)}$$

➤ Weak coupling → naturally weak scale mass:

~1 GeV – 10 TeV mass range favored

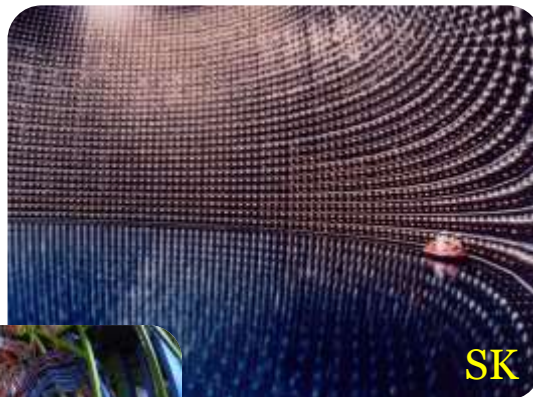
➔ weak scale (new) physics

* Of course, **axion** is another classic solution. (This Morning)

Diverging Efforts for WIMP Searches



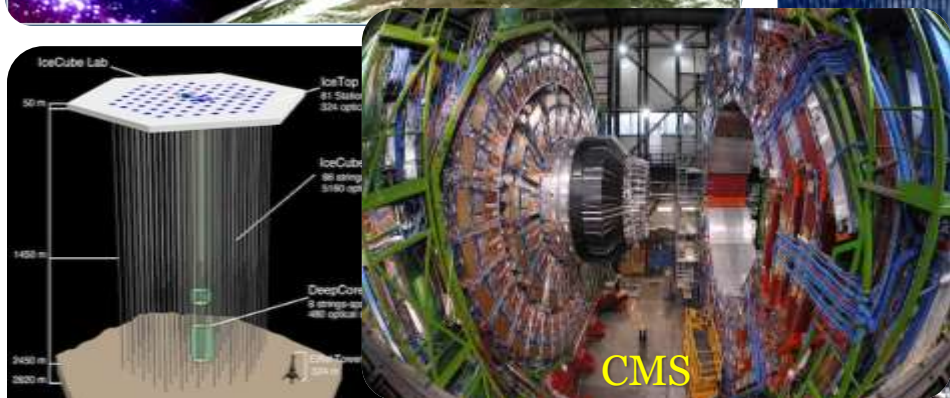
Fermi-LAT



SK

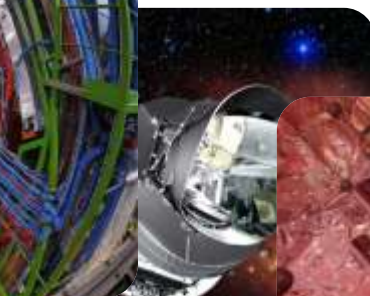


DAMA

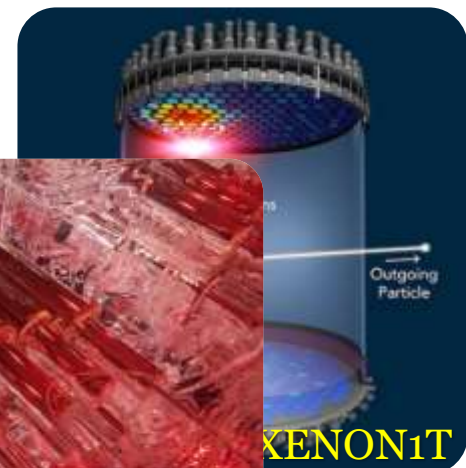


CMS

IceCube



Planck



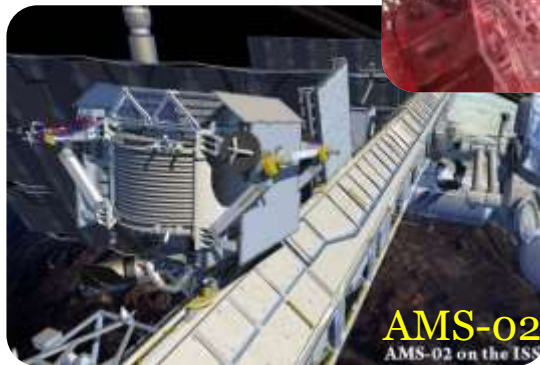
XENON1T



COSINE-100



CTA



AMS-02
AMS-02 on the ISS



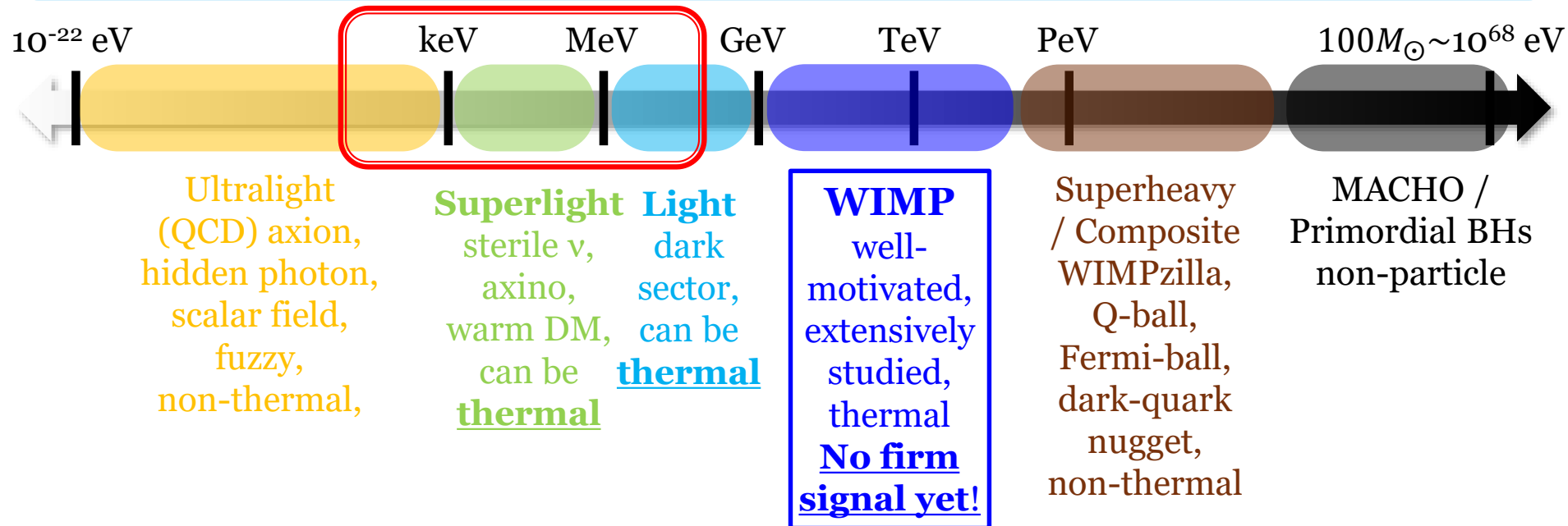
ATLAS

**Only
WIMP?**

No!



Mass Scale of DM



Light DM Sector



- ❖ For heavy mediator, $\langle\sigma v\rangle \sim \frac{\alpha_X^2 m_X^2}{M^4}$
- ❖ For **weak scale** physics,
sub-GeV DM overproduction
→ **New mediator** $< M_{\text{W}}$ for freeze-out
or **new mechanism** e.g., freeze-in, ...
- ❖ Various **light DM/mediator scenarios**:
 - ✓ MeV DM for GC 511 keV line observation [[astro-ph/0309686](#)]
 - ✓ Secluded MeV DM [[arXiv:0711.3528](#), [0711.4866](#)]
 - ✓ Sommerfeld enhancement for e^+ excess [[arXiv:0810.0713](#)]
 - ✓ $(g-2)_{e,\mu}$: $\sim 2-3\sigma$ discrepancy [[arXiv:1806.10252](#)]
 - ✓ New ν interactions for the MiniBooNE excess [[arXiv:1807.09877](#)]
 - ✓ Solutions of Yukawa coupling hierarchy prob. [[arXiv:1905.02692](#)]
 - ✓ ...
- ❖ **Light particle DM**
- ❖ **New DM relic determination mechanisms**:
 - ✓ Assisted Freeze-Out [[arXiv:1112.4491](#)]
 - ✓ Cannibal DM [[arXiv:1602.04219](#), [1607.03108](#)]
 - ✓ Co-Decaying [[arXiv:1105.1652](#), [1607.03110](#)]
 - ✓ Semi-Annihilation [[arXiv:0811.0172](#), [1003.5912](#)]
 - ✓ SIMP [[arXiv:1402.5143](#)]
 - ✓ ...

Light DM Sector



❖ $E_k \sim mv^2 < \mathbf{0(k eV)}$ with $v \sim 10^{-3}$:
 $< E_r^{th}$ of typical DM direct detectors
 for nuclear recoils

❖ New ideas for low E_r^{th} w/ e-recoil are required!

✓ Ionization by e-recoils (semiconductor)

[arXiv:1108.5383, 1509.01598]

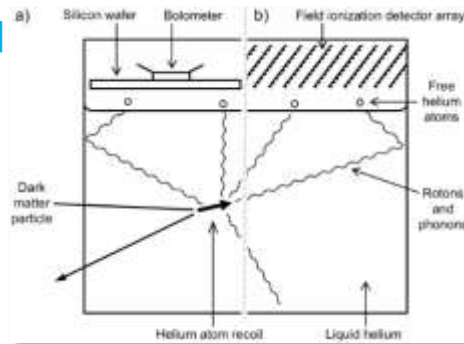
✓ Ejection of e's (graphene, C-nanotube)

[arXiv:1606.08849, 1706.02487, 1808.01892]

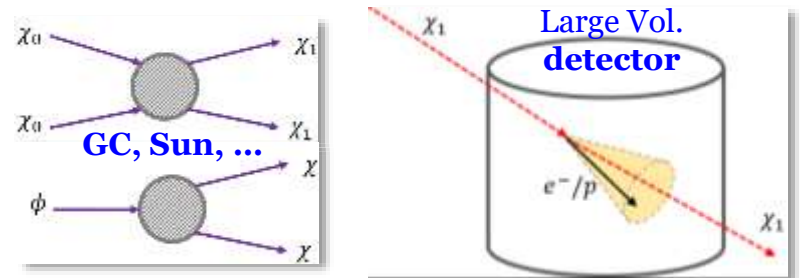
✓ Evaporation of He by nuclear-recoils

[arXiv:1706.00117]

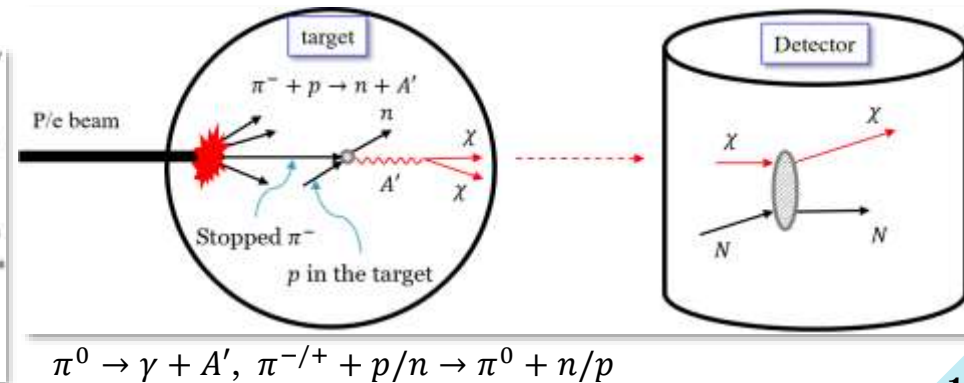
✓ ...



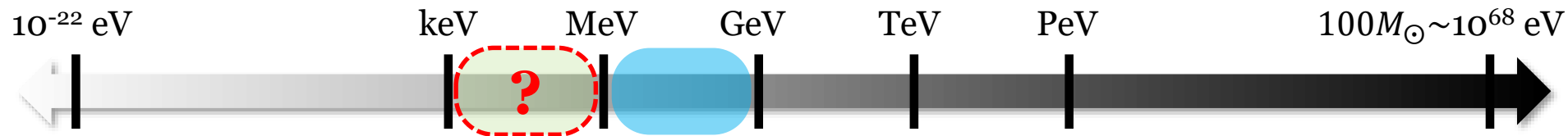
❖ Cosmogenic boosted DM searches: COSINE-100, DUNE/ProtoDUNE, IceCube, SK/HK/KNO, ...



❖ Beam-produced light DM/mediator searches: Babar, BDX, Belle-II, CCM, COHERENT, DUNE, FASER, JSNS², LDMX, MATHSULA, NA64, SeaQuest, SHiP, ...



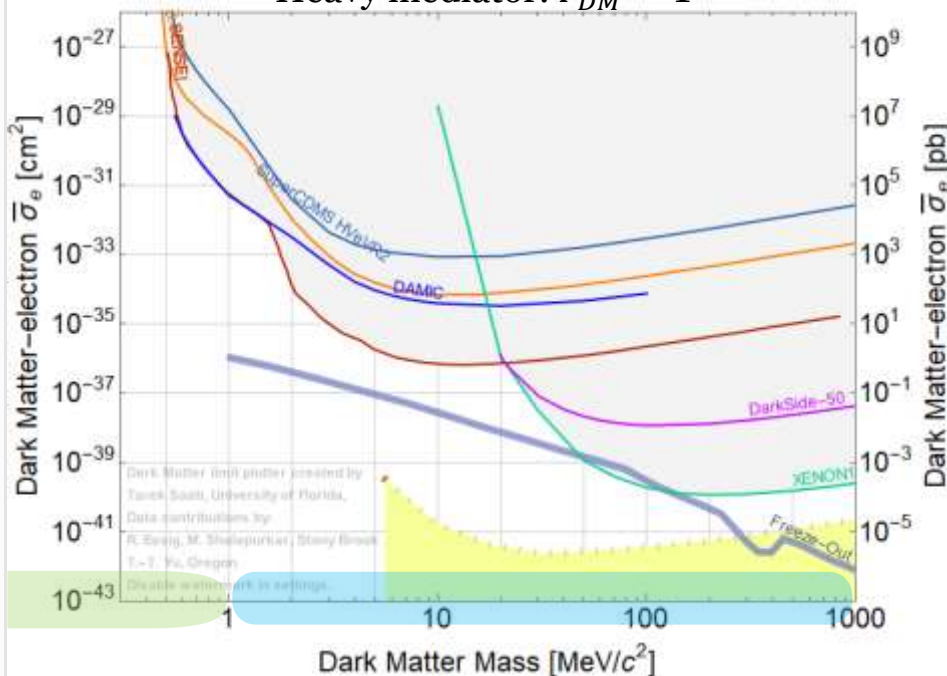
Light DM: Direct Search Status



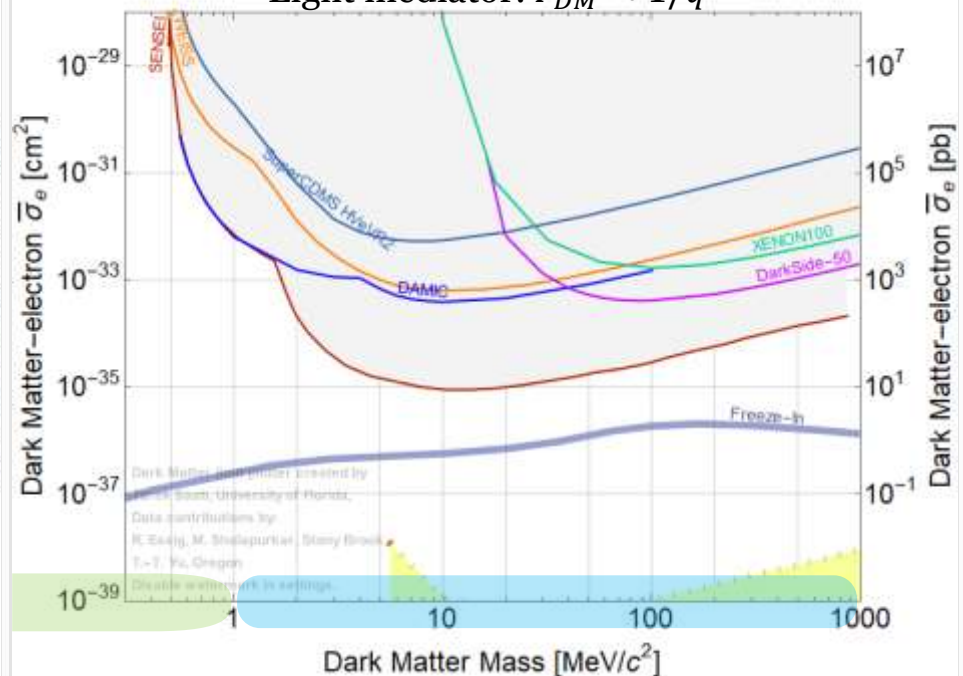
Super-light Light

DM

Heavy mediator: $F_{DM} = 1$



Light mediator: $F_{DM} \propto 1/q^2$



[Dark Matter Limit Plotter v5.16, updated Aug. 17, 2020]

Super-Light DM: Main Focus



Super-light DM

❖ Various well-motivated super-light DM pheno.:

✓ Sterile neutrinos

[[hep-ph/9303287](#), [astro-ph/9810076](#)]

✓ Mirror ν DM [[hep-ph/9505385](#)]

✓ Axino/gravitino [[arXiv: 0902.0769](#), [1407.0017](#)]

✓ Axion-like particles

[[arXiv:0912.0015](#), [1407.0017](#), [1510.07633](#)]

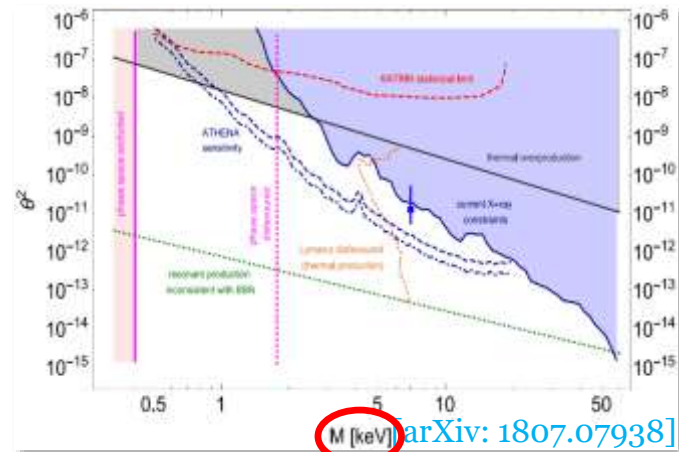
✓ Super-light dark gauge bosons

[[arXiv:1105.2812](#), [1201.5902](#)]

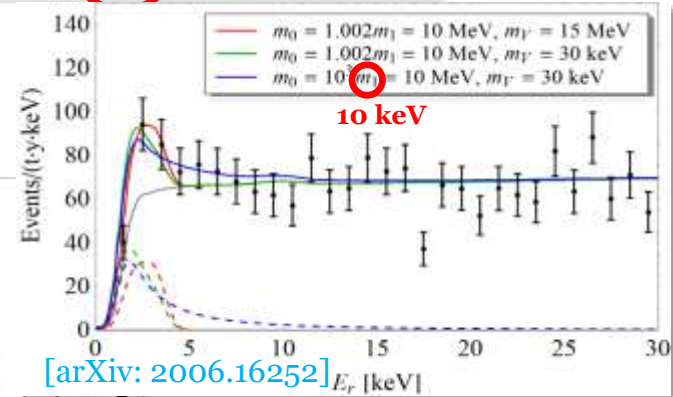
✓ Decaying DM for 3.5 keV line

[[arXiv:1403.1536](#), [1508.06640](#)]

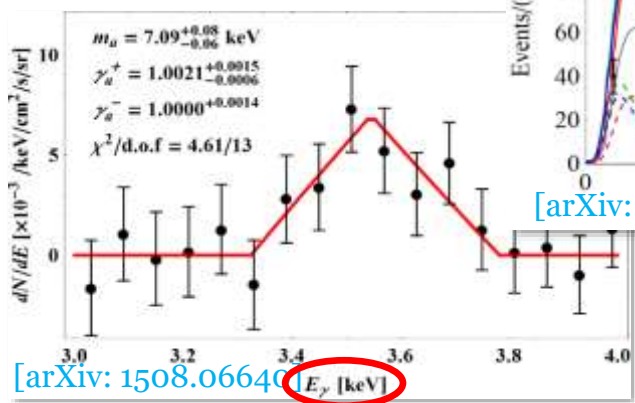
✓ keV DM for XENON1T, ...



[[arXiv: 1807.07938](#)]



[[arXiv: 2006.16252](#)]



[[arXiv: 1508.06640](#)]

Super-Light DM: Current Status



Super-light DM

Superconducting-nanowire
 $E_{th} = 0.8$ eV, 4.3 ng WSi, 10^4 s

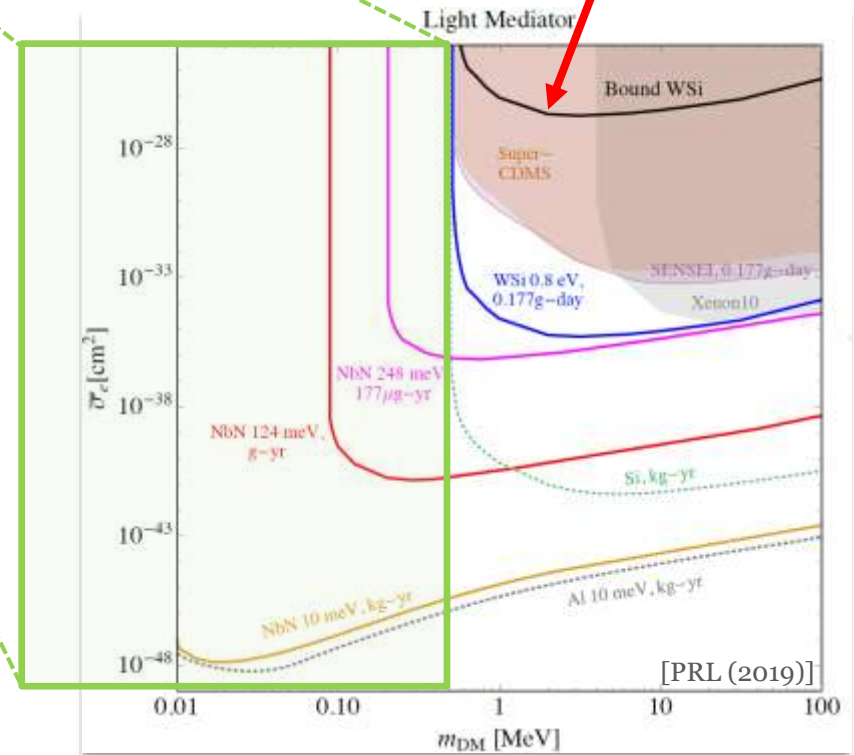
❖ $E_k \sim mv^2 \sim \mathbf{O(meV)}$ with $m \sim \text{keV}$ & $v \sim 10^{-3}$

❖ **New ideas** are required!

- ✓ Superconductor [PRL (2016)]
- ✓ Superfluid He [PRL (2016)]
- ✓ 3D Dirac material [PRD (2018)]
- ✓ Polar material [PLB (2018)]
- ✓ Superconducting-nanowire [PRL (2019)]
- ✓ ...

❖ **World race** to prove **super-light DM**.

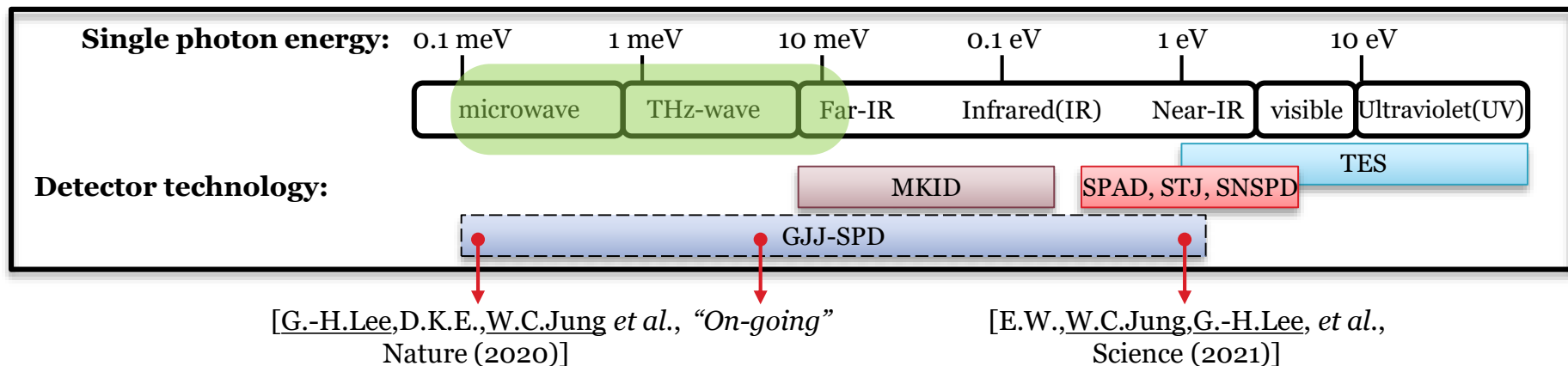
❖ **No experiment** for **O(keV) DM** so far.



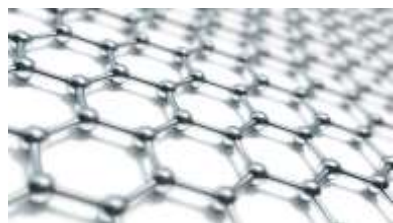
We proposed a **new super-light DM direct detection strategy** adopting the **graphene-based Josephson junction*** (GJJ) microwave single photon detector.

* A “state-of-the-art” technology:
much lower $E_{th} \sim O(0.1 \text{ meV})$

Status of Sensor Technologies



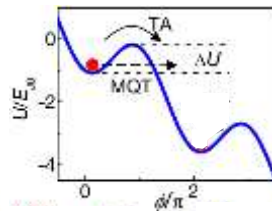
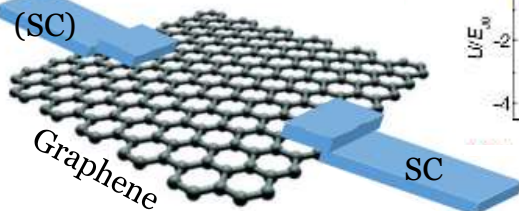
❖ Graphene



- ✓ Minute electronic heat capacity: $\sim 10 k_B/\mu\text{m}^2$
→ **Large response** in electron temperature (T)
e.g., $E=1$ meV raises from $T=0.01$ K to **1.3 K**
- ✓ **Fast thermalization** time: $\tau_{e-e} < 1$ ps
- ✓ **Slow cooling** time: $\tau_{e-ph} \sim 1$ ns

❖ Josephson junction

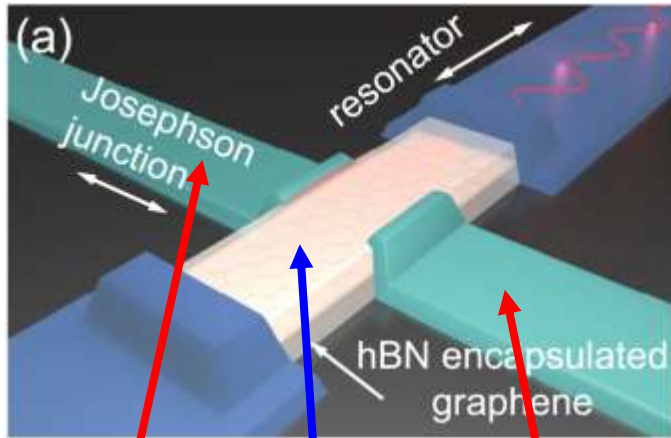
Superconductor (SC)



Plasma frequency:
 $f_p \sim 100$ GHz

- ✓ **Sensitive** response: $dI_c/dT \sim$ a few $\mu\text{A}/\text{K}$
- ✓ **Fast** response: $\tau_p = 1/f_p \sim 0.1$ ns ($\ll \tau_{e-ph}$)

GJJ Device

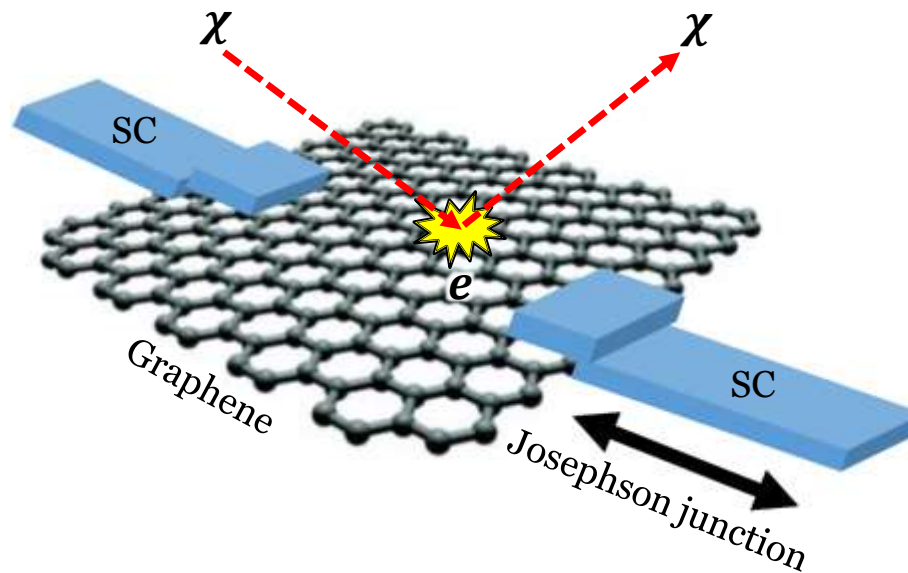


Superconductor-Graphene-Superconductor (SGS)

The device consists of a sheet of mono-layer graphene two sides of which are joined to superconductor, forming a superconductor-normal metal-superconductor Josephson junction.

- ❖ A GJJ single-photon detector was proposed, covering from near-IR to microwave. [Phys. Rev. Applied (2017)]
- ❖ K.C. Fong, G.-H. Lee & their collaborators have **demonstrated experimentally** that the GJJ microwave bolometer can have **sensitivity to $E \sim 0.1$ meV energy deposit**. [Nature (2020)]
- ❖ Currently, a GJJ single-photon detector is **under testing** in the laboratory.

Detection Principle

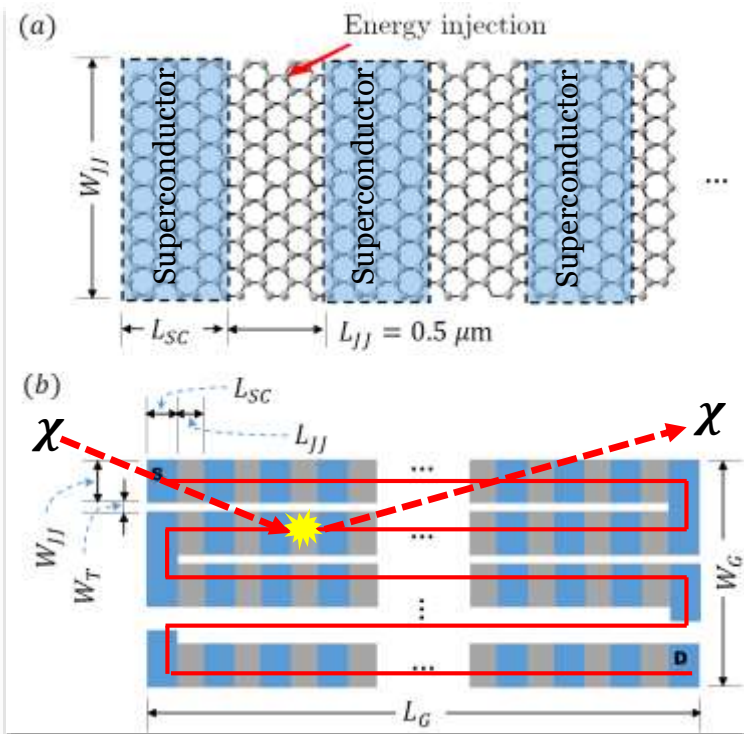


- I. **DM scatters off (π -bond) free electrons**, transferring some fraction of its incoming E_k .
- II. **The recoiling e heats up & thermalizes** with nearby e's rapidly via e-e interactions.
- III. **The JJ is triggered**: the temperature rise switches the zero-voltage (non-resistive) of JJ to a **non-zero-voltage (resistive) state**.

❖ $E_k \sim mv^2 \sim 1 \text{ meV}$ for $m_{DM} = 1 \text{ keV}$

→ **GJJ detector** ($E_{th} \sim 0.1 \text{ meV}$): **sensitivity** to the signal even by **sub-keV DM**.

Conceptual Design Proposal



- I. **Single graphene strip** (a): the assembly of a graphene strip & a number of superconducting material strips → an array of SC-graphene-SC-graphene-SC-... (SGSGS...).
- II. Each sequence of SGS represents a single GJJ device.
- III. **Full detector unit** (b): all GJJs are connected in series so that even a **single switched GJJ allows the series resistance** measured between S & D to **switch from 0 to a finite value**.

- ❖ E_{th} is determined by **the strip width W_{JJ}** : $W_{JJ} = 3 \mu\text{m} (30 \mu\text{m}) \rightarrow E_{th} \approx 0.1 \text{ meV} (1 \text{ meV})$.
- ❖ A much larger-scale detector can be made of **a stack of such detector units**.

To calculate experimental sensitivities, we should consider the **scattering** between **DM traveling in 3D** & free **electrons living in 3D but confined in 2D** graphene layer.

Calculating Signal Rates

- ❖ **Goal:** The event rate of **DM scattering off** free **electrons in a 2D** graphene sheet.
- ❖ **Key point:** An electron is still **confined in the 2D** graphene even **after the collision**.
 - ➔ **No significant momentum change** along the **surface-normal (z-axis) direction**.
 - ➔ **Signal rate depending on the DM direction**
- ❖ We will calculate the number of events/unit detector mass/unit run time:

$$n_{\text{eve}} = \frac{N_{\text{eve}}^{\text{total}}}{M_T t_{\text{run}}}$$

($N_{\text{eve}}^{\text{total}}$: total number of events, M_T : total detector mass, t_{run} : total time exposure)

Calculation Procedure I

$$\begin{aligned} \diamond n_{\text{eve}} &= \frac{N_{\text{eve}}^{\text{total}}}{M_T t_{\text{run}}} = \frac{1}{M_T t_{\text{run}}} \int_{E_r > E_{\text{th}}} dE_r \frac{dN_{\text{eve}}}{dE_r} \\ &= \frac{1}{M_T t_{\text{run}}} \int_{E_r > E_{\text{th}}} \int dE_r dv_{\chi} f_{\text{MB}}(v_{\chi}) \frac{d}{dE_r} N_e \sigma_{e\chi} v_{\text{rel}} \frac{\rho_{\chi}}{m_{\chi}} t_{\text{run}} \end{aligned}$$

$$= \int_{E_r > E_{\text{th}}} dE_r dv_{\chi} f_{\text{MB}}(v_{\chi}) \frac{dn_e^{3\text{D}} \sigma_{e\chi} v_{\text{rel}}}{dE_r} \frac{1}{\rho_T^{3\text{D}}} \frac{\rho_{\chi}}{m_{\chi}}$$

$$= \int_{E_r > E_{\text{th}}} dE_r dv_{\chi_{\parallel}} f_{\text{MB}}(v_{\chi_{\parallel}}) \frac{dn_e^{2\text{D}} \sigma_{e\chi} v_{\text{rel}\parallel}}{dE_r} \frac{1}{\rho_T^{2\text{D}}} \frac{\rho_{\chi}}{m_{\chi}}$$

2D nature of graphene

$$\begin{aligned} \checkmark N_{\text{eve}}^{\text{total}} &= n_{\text{eve}} M_T t_{\text{run}} \\ \checkmark N_{\text{eve}} &= N_e \sigma_{e\chi} \Phi_{\chi} t_{\text{run}} \\ \checkmark \Phi_{\chi} &= n_{\chi} v_{\text{rel}} \ \& \ n_{\chi} = \rho_{\chi} / m_{\chi} \end{aligned}$$

$$\begin{aligned} \checkmark \frac{N_e}{M_T} &= \frac{N_e/V}{M_T/V} = \frac{n_e^{3\text{D}}}{\rho_T^{3\text{D}}} \\ &= \frac{N_e/(A\Delta l)}{M_T/(A\Delta l)} = \frac{n_e^{2\text{D}}}{\rho_T^{2\text{D}}} \end{aligned}$$

$$\diamond n_e^{2\text{D}} = 2 \int \frac{d^2 p_{e,i}^{(xy)}}{(2\pi)^2} f_{e,i}(E_{e,i}) = 2 \int \frac{d^2 p_{e,i}^{xy}}{(2\pi)^2} \int \frac{dp_{e,i}^z}{(2\pi)} (2\pi) \delta(p_{e,i}^z - p_{e,f}^z) f_{e,i}(E_{e,i})$$

$$= 2 \int \frac{d^3 p_{e,i}}{(2\pi)^3} \delta(p_{e,i}^z - p_{e,f}^z) f_{e,i}(E_{e,i})$$

$$\checkmark f_{e,i}(E_{e,i}) = 1 / \left\{ 1 + \exp\left(\frac{E_{e,i} - \mu}{T}\right) \right\}, \ (\mu \sim E_F)$$

→ Fermi-Dirac distribution function

Consistent with the assumption of **no significant momentum change along the surface-normal direction**

Calculation Procedure II

❖ **Graphene-surface-parallel DM velocity profile:** $f_{\text{MB}}(v_{\chi\parallel}) = \frac{2(e^{-v_{\chi\parallel}^2/v_0^2} - e^{-v_{\text{esc}}^2/v_0^2})}{\sqrt{\pi}v_0\text{erf}(v_{\text{esc}}/v_0) - 2v_{\text{esc}}e^{-v_{\text{esc}}^2/v_0^2}}$

→ We take **a plane-projection** of a modified Maxwell-Boltzmann distribution.

❖ **Event rate** on a (sufficiently thin) **2D** material: $\langle n_e^{2\text{D}} \sigma_{e\chi} v_{\text{rel}\parallel} \rangle = \int \frac{d^3 p_{\chi,f}}{(2\pi)^3} \frac{|\overline{\mathcal{M}}|^2}{16\pi m_e^2 m_\chi^2} S_{2\text{D}}(E_r, q)$

❖ **Structure function** for the **2D** system: $S_{2\text{D}}(E_r, q)$

$$= 2 \int \frac{d^3 p_{e,i}}{(2\pi)^3} \int \frac{d^3 p_{e,f}}{(2\pi)^3} (2\pi) \delta(p_{e,i}^z - p_{e,f}^z) (2\pi)^4 \delta^{(4)}(p_{\chi,i} + p_{e,i} - p_{\chi,f} - p_{e,f}) f_{e,i}(E_{e,i}) \{1 - f_{e,f}(E_{e,f})\}$$

$$= (2\pi) \delta(p_{\chi,i}^z - p_{\chi,f}^z) \cdot \frac{1}{2\pi^2} \int d^3 p_{e,i} \delta(E_r + E_{\chi,i} - E_{\chi,f}) f_{e,i}(E_{e,i}) \{1 - f_{e,f}(E_{e,f})\}$$

$$= (2\pi) \delta(p_{\chi,i}^z - p_{\chi,f}^z) \cdot S_{3\text{D}}(E_r, q)$$

→ The **Pauli blocking effects(=phase space suppression)** are encoded in the structure function.

The analytic expression for $S_{3\text{D}}(E_r, q)$ is available in the non-relativistic limit.

[S. Reddy *et al.*, PRD (1998), Y. Hochberg *et al.*, JHEP (2016)]

Calculation Procedure III

$$\diamond n_{\text{eve}} = \int_{E_r > E_{\text{th}}} dE_r dv_{\chi\parallel} f_{\text{MB}}(v_{\chi\parallel}) \frac{d\langle n_e^{2\text{D}} \sigma_{e\chi} v_{\text{rel}\parallel} \rangle}{dE_r} \frac{1}{\rho_{\text{gr}}^{2\text{D}}} \frac{\rho_\chi}{m_\chi}$$

- ✓ $\rho_\chi = 0.3 \text{ GeV/cm}^3$
- ✓ $v_0 = 220 \text{ km/s}, v_{\text{esc}} = 500 \text{ km/s}$
- ✓ $\rho_{\text{gr}}^{2\text{D}} = 7.62 \times 10^{-8} \text{ g/cm}^2$

$$f_{\text{MB}}(v_{\chi\parallel}) = \frac{2(e^{-v_{\chi\parallel}^2/v_0^2} - e^{-v_{\text{esc}}^2/v_0^2})}{\sqrt{\pi}v_0 \text{erf}(v_{\text{esc}}/v_0) - 2v_{\text{esc}}e^{-v_{\text{esc}}^2/v_0^2}}$$

$$\langle n_e^{2\text{D}} \sigma_{e\chi} v_{\text{rel}\parallel} \rangle = \int \frac{d^3p_{\chi,f}}{(2\pi)^3} \frac{|\overline{\mathcal{M}}|^2}{16\pi m_e^2 m_\chi^2} S_{2\text{D}}(E_r, q)$$

$$\text{with } S_{2\text{D}}(E_r, q) = (2\pi)\delta(p_{\chi,i}^z - p_{\chi,f}^z) \cdot S_{3\text{D}}(E_r, q)$$

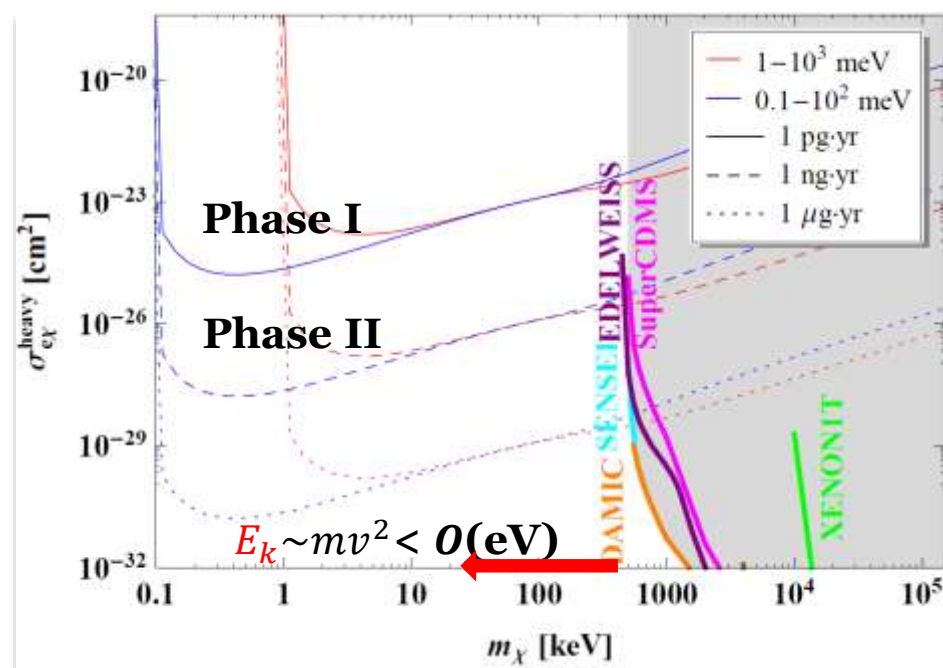
- ❖ We assume that DM interacts with electrons via an exchange of mediator ϕ as done in many of the preceding studies :

$$\sigma_{e\chi} \approx \frac{g_e^2 g_\chi^2}{\pi} \frac{\mu_{e\chi}^2}{(m_\phi^2 + q^2)^2} \rightarrow \sigma_{e\chi}^{\text{heavy}} \approx \frac{g_e^2 g_\chi^2}{\pi} \frac{\mu_{e\chi}^2}{m_\phi^4} \text{ for } (m_\phi^2 \gg q^2) \text{ \& } \sigma_{e\chi}^{\text{light}} \approx \frac{g_e^2 g_\chi^2}{\pi} \frac{\mu_{e\chi}^2}{q^4} \text{ for } (m_\phi^2 \ll q^2)$$

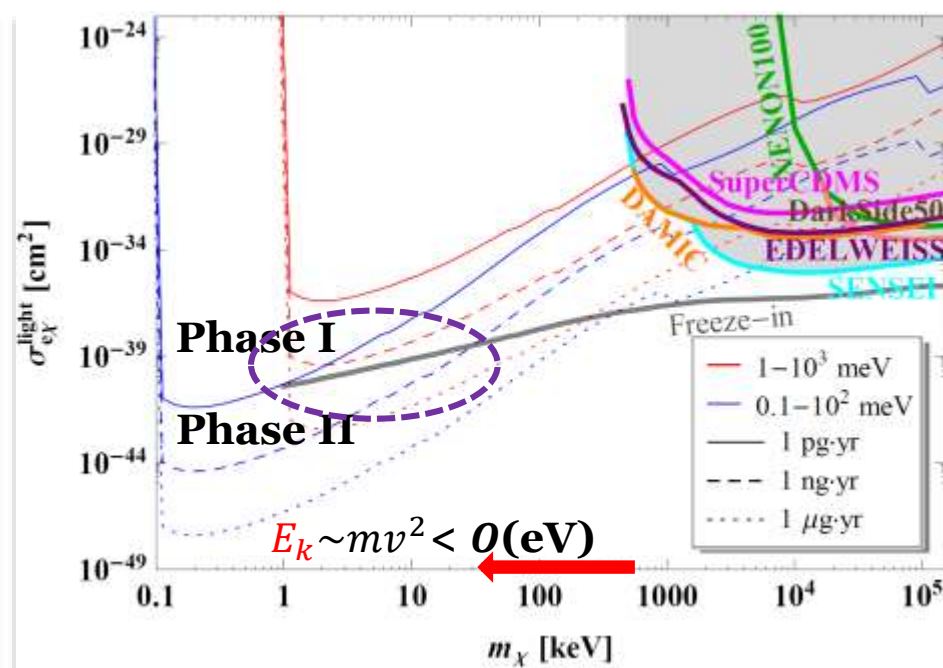
- ❖ The matrix element $|\overline{\mathcal{M}}|^2$ is related to the scattering cross section as $\sigma_{e\chi} = \frac{|\overline{\mathcal{M}}|^2}{16\pi m_e^2 m_\chi^2} \mu_{e\chi}^2$.
- ❖ From the linear dispersion of graphene: $E_F = v_F \sqrt{\pi n_c}$ with $v_F \sim 10^8 \text{ cm/s}$ & $n_c \sim 10^{12} / \text{cm}^2$.

Expected Sensitivities

Heavy mediator: $F_{DM} = 1$



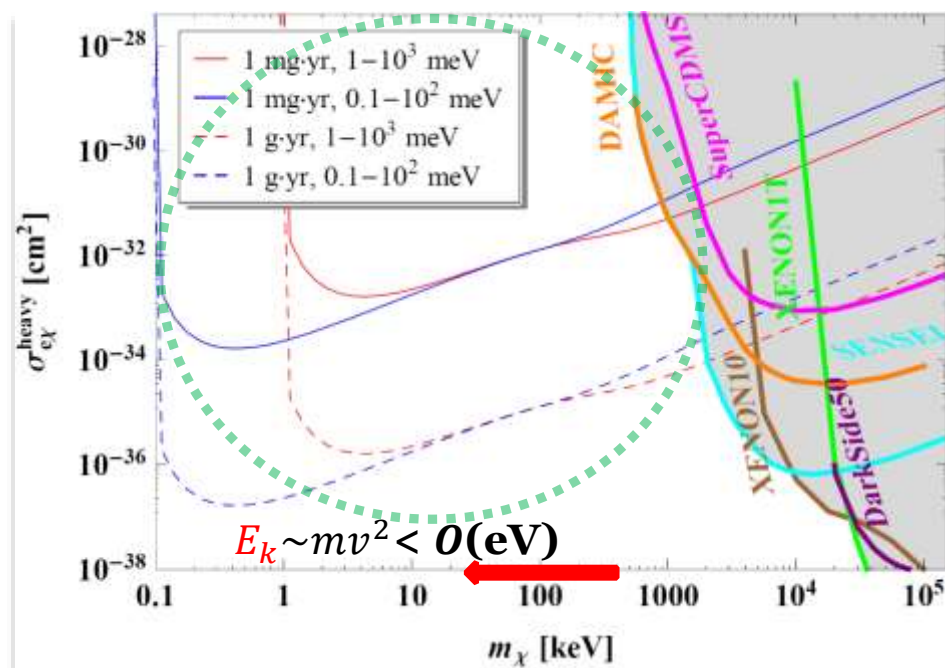
Light mediator: $F_{DM} \propto 1/q^2$ with $q_{ref} = \alpha_e m_e$



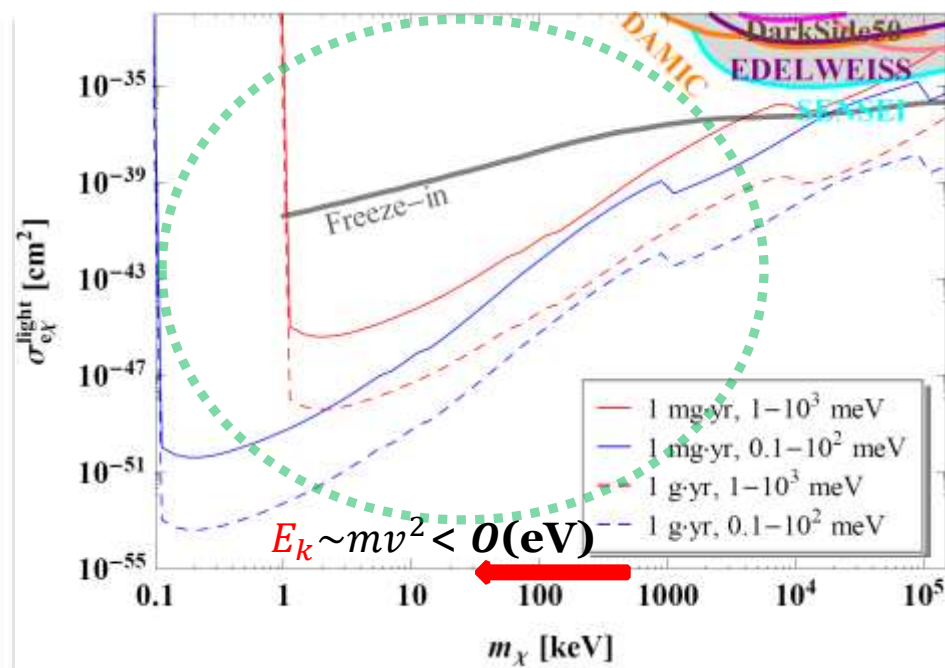
- ✓ The **proposed detector** can **improve the minimum detectable DM mass ($m_{DM} \sim 0.1$ keV)** by more than 3 orders of magnitude over the ongoing/existing experiments.
- ✓ **Capable of probing** the prediction of **freeze-in** scenarios even with a **pg-scale detector**.

Expected Sensitivities: (Far) Future

Heavy mediator: $F_{DM} = 1$



Light mediator: $F_{DM} \propto 1/q^2$ with $q_{ref} = \alpha_e m_e$



- ✓ **Capable of fully probing** the prediction of **freeze-in** scenarios with $m_{DM} < \mathbf{O}(\text{GeV})$.
- ✓ **Great search prospect** even for **sub-keV DM**.

Summary

- We have proposed a class of new DM detectors, adopting the GJJ device which has been implemented & demonstrated experimentally.
- For the scattering between DM moving in 3D space & e's confined in 2D graphene, we (for the first time) built an effective model and computed the event rate.
→ Signal rate depends on the DM incident direction!
- The proposed detector is capable of sensing sub-keV (warm) DM scattering off electrons due to its outstanding $E_{th} \sim 0.1 \text{ meV}$. → Improving the minimum detectable DM mass ($m_{DM} \sim 0.1 \text{ keV}$) by more than 3 orders of magnitude.

The Test Run with the Existing GJJs & fabrication of GJJ array is in progress.

Thank you