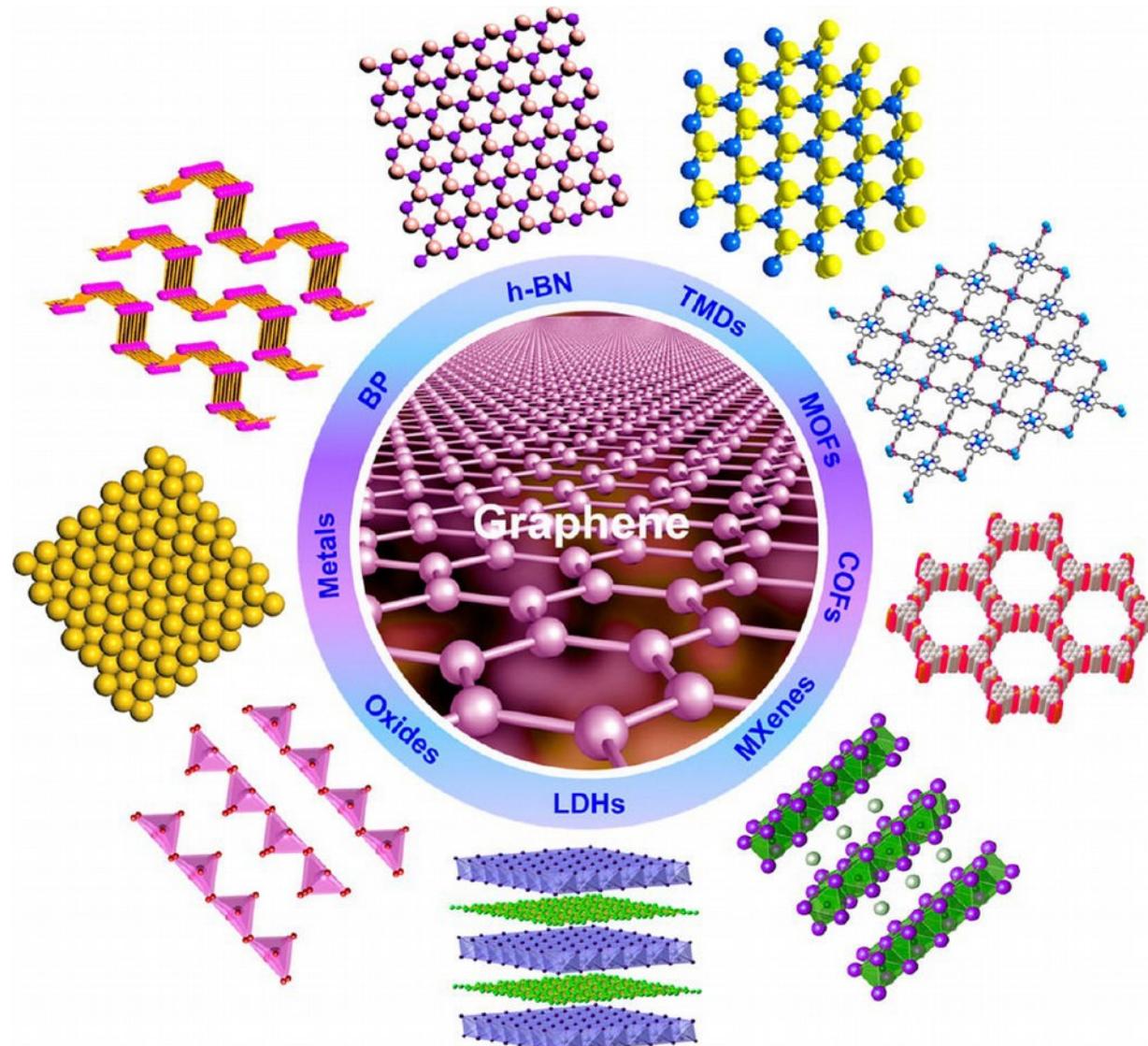


# **Prediction of Large-Gap Topological Insulator in functionalized Ordered Double Transition Metal MXene**

Zhi-Quan Huang<sup>1</sup>, Mei-Ling Xu<sup>1</sup>, Gennevieve Macam<sup>1</sup>,  
Chia-Hsiu Hsu<sup>1</sup> and Feng-Chuan Chuang<sup>1</sup>

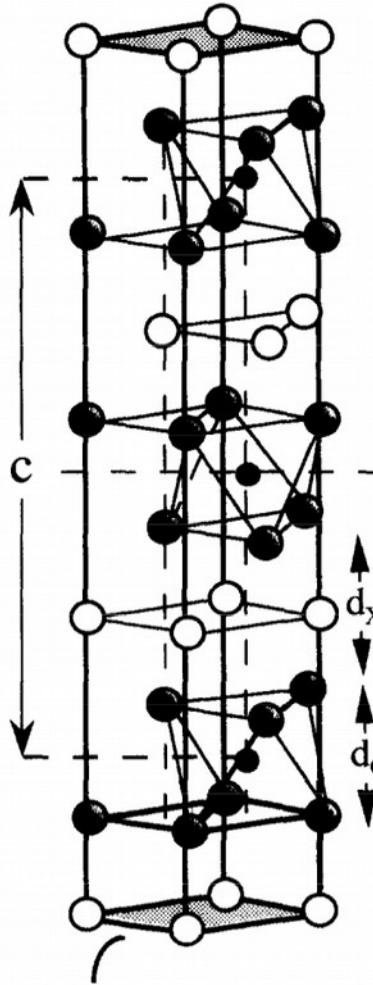
*1 Department of Physics, National Sun Yat-Sen University*

# Different kinds of typical ultrathin 2D nanomaterials

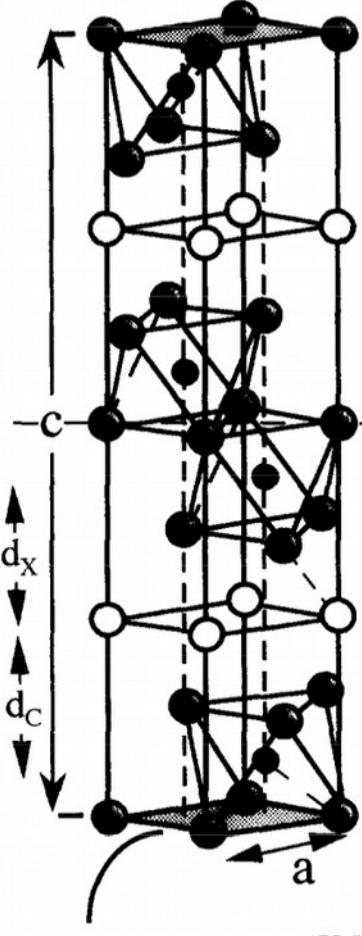


# $M_{n+1}AX_n$ Structure

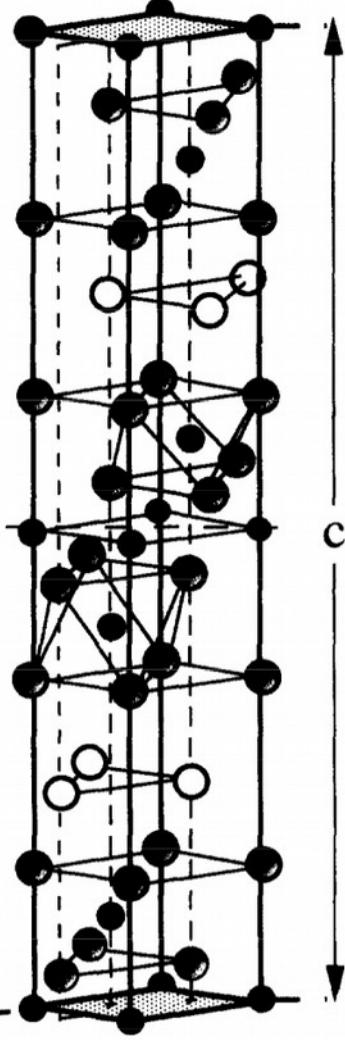
$M_2AX_1$   
**(211)**



$M_3AX_2$   
**(312)**



$M_4AX_3$   
**(413)**



$M_{n+1}AX_n$

n : 1, 2 or 3

M : early transition metal

A : A-group (mostly IIIA and IVA) element

X : C or N.

# Table of $M_{n+1}AX_n$

IIB	IIIA	IVA	VA	VIA
	<b>Al</b> Ti <sub>2</sub> AlC, <b>4.11</b> (3.04,13.60) V <sub>2</sub> AlC, <b>4.07</b> (3.1,13.83) Cr <sub>2</sub> AlC, <b>5.24</b> (2.86,12.8) Nb <sub>2</sub> AlC, <b>6.50</b> (3.10,13.8) Ta <sub>2</sub> AlC, <b>11.82</b> (3.07,13.8) Ti <sub>2</sub> AlN, <b>4.31</b> (2.989,13.614) Ti <sub>3</sub> AlC <sub>2</sub> , <b>4.5</b> (3.075,18.578) Ti <sub>4</sub> AlN <sub>3</sub> , <b>4.76</b> (2.988, 23.372)	<b>Si</b> Ti <sub>3</sub> SiC <sub>2</sub> <b>4.52</b> (3.0665,17.671)	<b>P</b> V <sub>2</sub> PC <b>5.38</b> (3.077,10.91) Nb <sub>2</sub> PC <b>7.09</b> (3.28,11.5)	<b>S</b> Ti <sub>2</sub> SC, <b>4.62</b> (3.216,11.22) Zr <sub>2</sub> SC, <b>6.20</b> (3.40, 12.13) Nb <sub>2</sub> SC <sub>0.4</sub> , (3.27,11.4) Hf <sub>2</sub> SC, (3.36, 11.99)
<b>Zn</b>	<b>Ga</b> Ti <sub>2</sub> GaC, <b>5.53</b> (3.07, 13.52) V <sub>2</sub> GaC, <b>6.39</b> (2.93, 12.84) Cr <sub>2</sub> GaC, <b>6.81</b> (2.88, 12.61) Nb <sub>2</sub> GaC, <b>7.73</b> (3.13, 13.56) Mo <sub>2</sub> GaC, <b>8.79</b> (3.01, 13.18) Ta <sub>2</sub> GaC, <b>13.05</b> (3.10, 13.57) Ti <sub>2</sub> GaN, <b>5.75</b> (3.00, 13.3) Cr <sub>2</sub> GaN, <b>6.82</b> (2.875, 12.77) V <sub>2</sub> GaN, <b>5.94</b> (3.00, 13.3)	<b>Ge</b> Ti <sub>2</sub> GeC, <b>5.68</b> (3.07, 12.93) V <sub>2</sub> GeC, <b>6.49</b> (3.00, 12.25) Cr <sub>2</sub> GeC, <b>6.88</b> (2.95, 12.08) Ti <sub>3</sub> GeC <sub>2</sub> , <b>5.55</b> (3.07, 17.76)	<b>As</b> V <sub>2</sub> AsC <b>6.63</b> (3.11, 11.3) Nb <sub>2</sub> AsC <b>8.025</b> (3.31, 11.9)	<b>Se</b>
<b>Cd</b>	<b>In</b> Sc <sub>2</sub> InC Ti <sub>2</sub> InC, <b>6.2</b> (3.13, 14.06) <b>9.71</b> (3.1, 14.41) Zr <sub>2</sub> InC, <b>7.1</b> (3.34, 14.91) Nb <sub>2</sub> InC, <b>8.3</b> (3.17,14.37) Hf <sub>2</sub> InC, <b>11.57</b> (3.30,14.73) Ti <sub>2</sub> InN, <b>6.54</b> (3.07,13.97) Zr <sub>2</sub> InN, <b>7.53</b> (3.27,14.83)	<b>Sn</b> Ti <sub>2</sub> SnC, <b>6.36</b> (3.163,13.679) Zr <sub>2</sub> SnC, <b>7.16</b> (3.3576, 14.57) Nb <sub>2</sub> SnC, <b>8.4</b> (3.241,13.802) Hf <sub>2</sub> SnC, <b>11.8</b> (3.320,14.388) Hf <sub>2</sub> SnN, <b>7.72</b> (3.31,14.3)	<b>Sb</b>	<b>Te</b>
	<b>Tl</b> Ti <sub>2</sub> TlC, <b>8.63</b> (3.15,13.98) Zr <sub>2</sub> TlC, <b>9.17</b> (3.36,14.78) Hf <sub>2</sub> TlC <b>13.65</b> (3.32,14.62) Zr <sub>2</sub> TlN, <b>9.60</b> (3.3,14.71)	<b>Pb</b> Ti <sub>2</sub> PbC, <b>8.55</b> (3.20,13.81) Zr <sub>2</sub> PbC, <b>9.2</b> 3.38,14.66 Hf <sub>2</sub> PbC, <b>12.13</b> (3.55,14.46)	<b>Bi</b>	

$M_{n+1}AX_n$

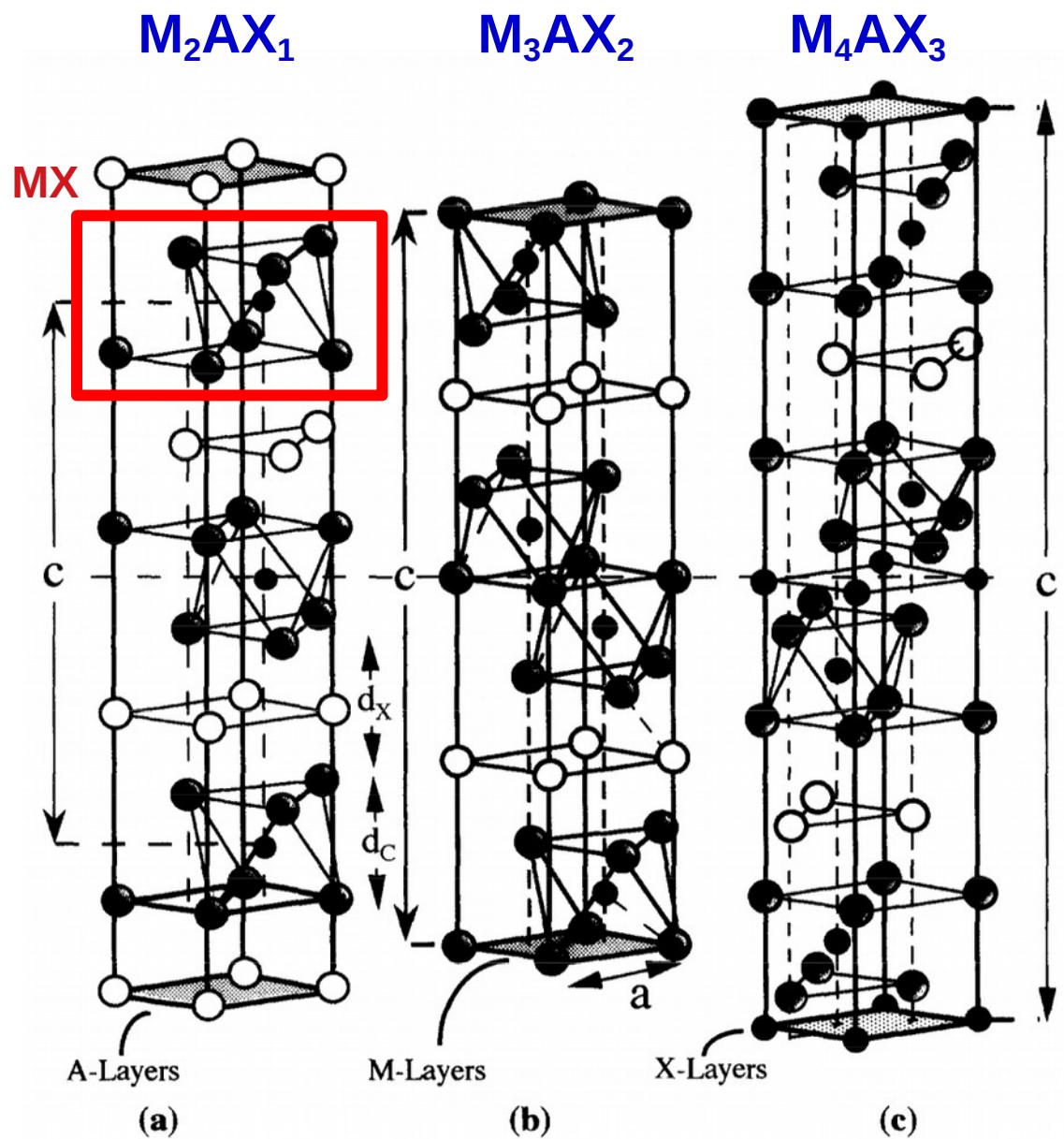
n : 1, 2 or 3

M : early transition metal

A : A-group (mostly IIIA and IVA) element

X : C or N.

# $M_{n+1}AX_n$ Structure



$M_{n+1}AX_n$

$n : 1, 2 \text{ or } 3$

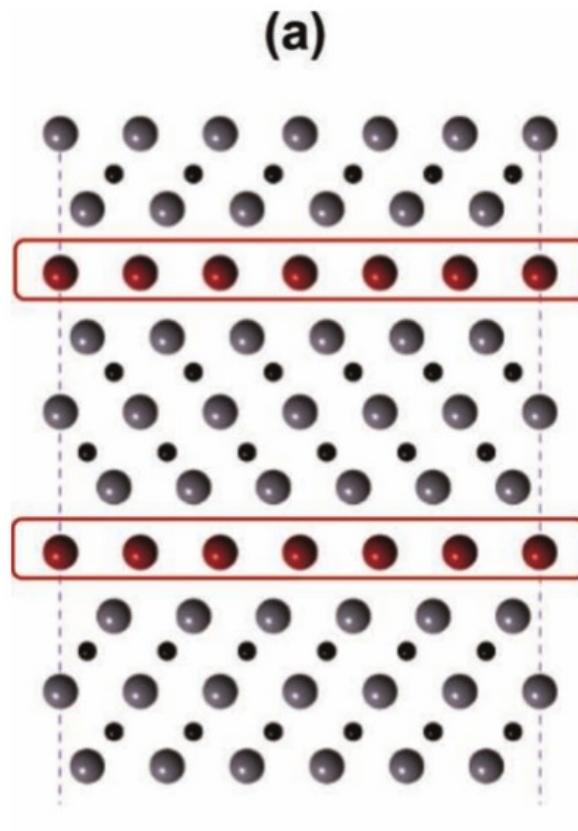
$M : \text{early transition metal}$

$A : \text{A-group (mostly IIIA and IVA) element}$

$X : \text{C or N.}$

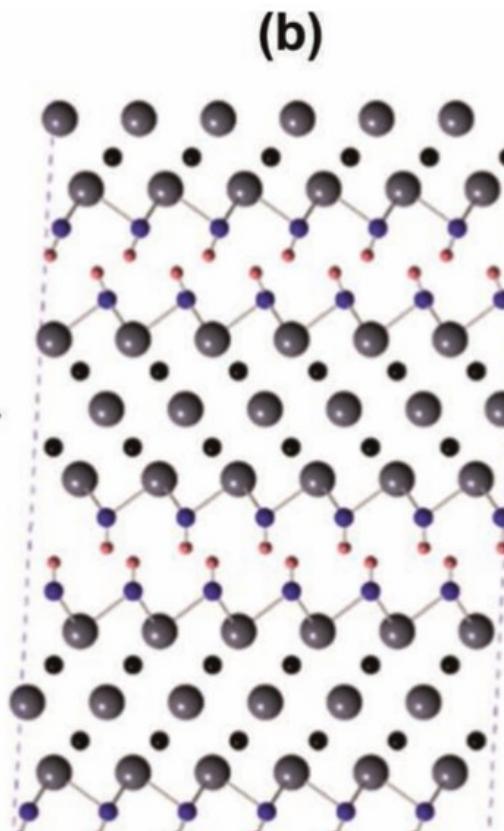
# Two-Dimensional Nanocrystals Produced by Exfoliation of $\text{Ti}_3\text{AlC}_2$

$\text{Ti}_3\text{AlC}_2$  structure

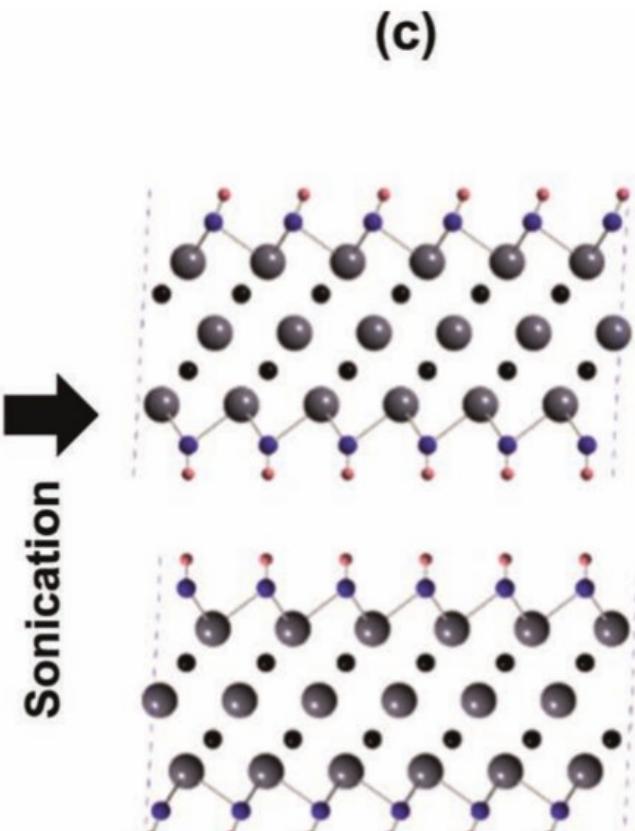


HF Treatment

Al atoms  
replaced by OH



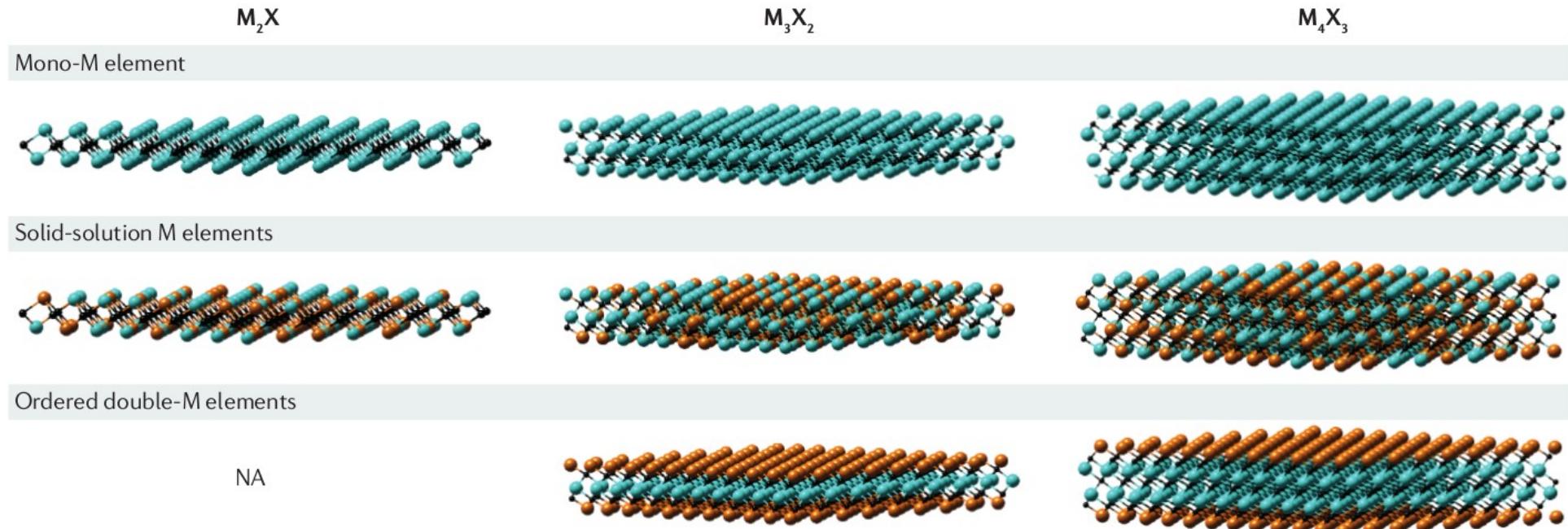
Breakage of the hydrogen  
bonds and separation



● Ti      ● C      ● Al  
● O      ● H

M. Naguib, M. Kurtoglu, V. Presser, J. Lu, J. Niu, M. Heon, L. Hultman, Y. Gogotsi, and M. W. Barsoum, Advanced Materials **23**, 4248 (2011).

# MXene Structure



$M_{n+1}X_nT_x$

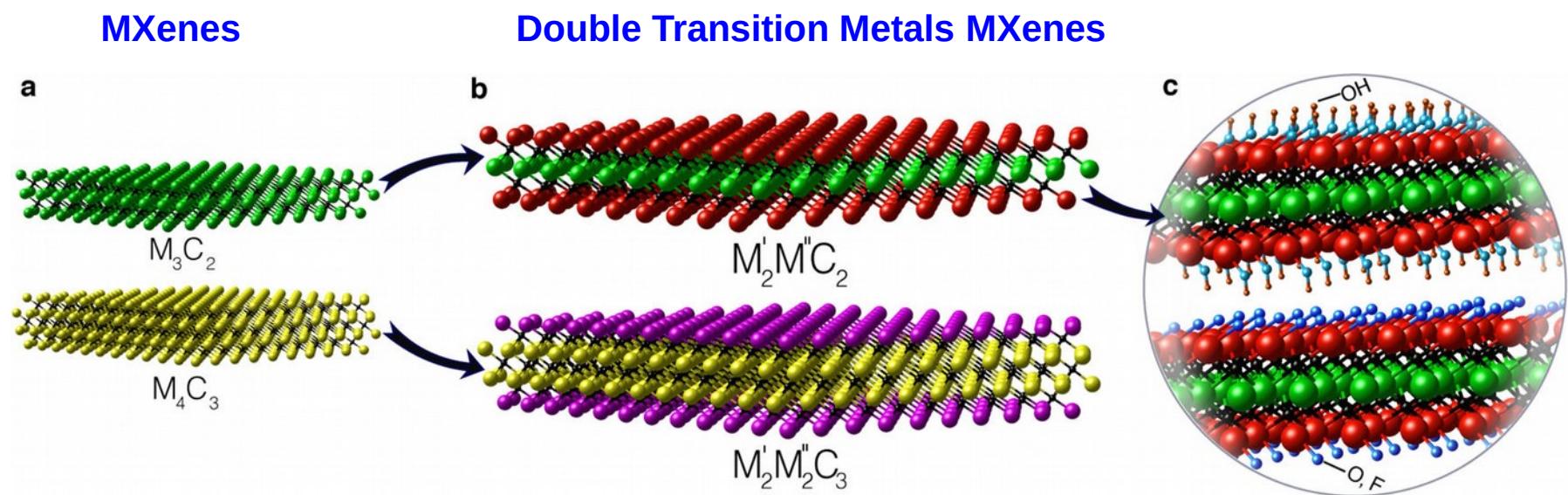
n : 1, 2 or 3

M : early transition metal

X : C or N

T : stands for the surface terminations (ex. H, O, F)

# MXenes and Double Transition Metals MXenes



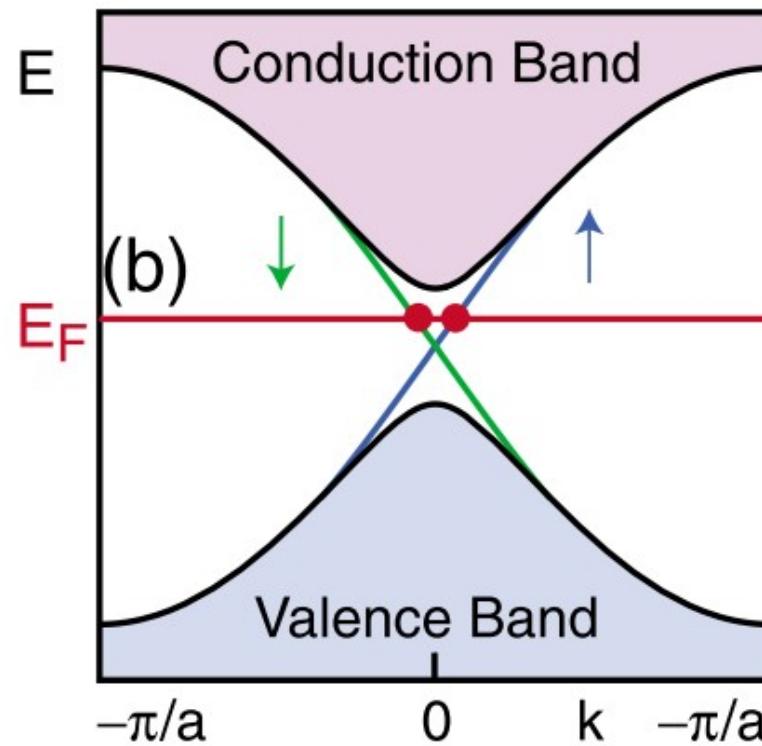
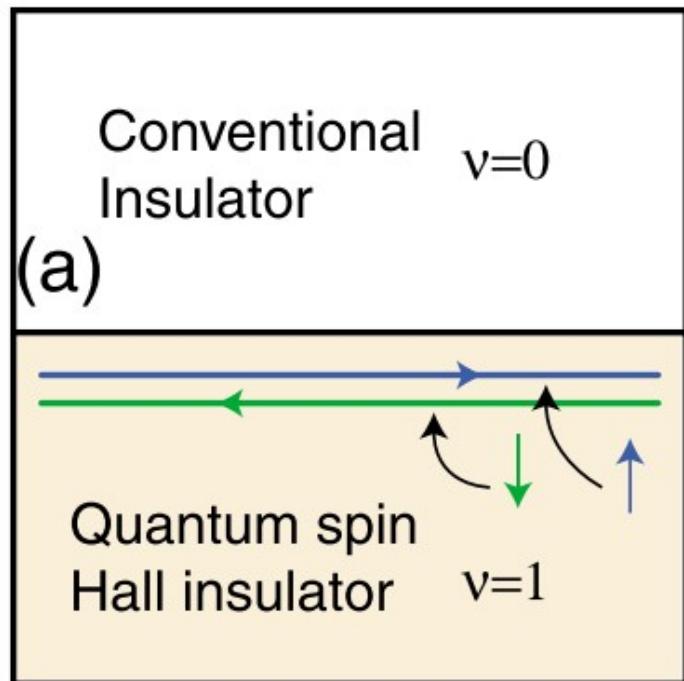
B. Anasori, Y. Xie, M. Beidaghi, J. Lu, B. C. Hosler, L. Hultman, P. R. C. Kent, Y. Gogotsi, and M. W. Barsoum, *ACS Nano* 9, 9507 (2015).

$Sc_2C$	$Ti_2C$	$Ti_2N$	$Zr_2C$	$Ti_3C_2$	$Ti_3N_2$	$Ti_3(C,N)_2$	$Zr_3C_2$	$Ti_4N_3$	$V_4C_3$	$Nb_4C_3$	$Ta_4C_3$
$Zr_2N$	$Hf_2C$	$Hf_2N$	$V_2C$	$(Ti,V)_3C_2$	$(Cr,V)_3C_2$	$(Ti_2Ta)C_2$	$(Ti_2Nb)C_2$	$(Ti,Nb)_4C_3$	$(Nb,Zr)_4C_3$	$(Ti_2Nb_2)C_3$	$(Ti_2Ta_2)C_3$
$V_2N$	$Nb_2C$	$Ta_2C$	$Cr_2C$	$(Cr_2V)C_2$	$(Mo_2V)C_2$	$(Cr_2Nb)C_2$	$(Cr_2Ta)C_2$	$(V_2Ti_2)C_3$	$(V_2Nb_2)C_3$	$(V_2Ta_2)C_3$	$(Nb_2Ta_2)C_3$
$Cr_2N$	$Mo_2C$	$W_2C$		$(Mo_2Ti)C_2$	$(Cr_2Ti)C_2$	$(Mo_2Nb)C_2$	$(Mo_2Ta)C_2$	$(Cr_2Ti_2)C_3$	$(Cr_2V_2)C_3$	$(Cr_2Nb_2)C_3$	$(Cr_2Ta_2)C_3$
$(Ti,V)_2C$	$(Ti,Nb)_2C$							$(Mo_2Ti_2)C_3$	$(Mo_2V_2)C_3$	$(Mo_2Nb_2)C_3$	$(Mo_2Ta_2)C_3$

■ Experimental ■ Theoretical ■ Ordered double-M ■ Solid-solution M

B. Anasori, M. R. Lukatskaya, and Y. Gogotsi, *Nature Reviews Materials* 2, 16098 (2017).

## (2D) Topological insulators



- $v$  does not change without closing the gap.
- Quantum spin Hall edge states
- Protected by time-reversal symmetry
- No backscattering

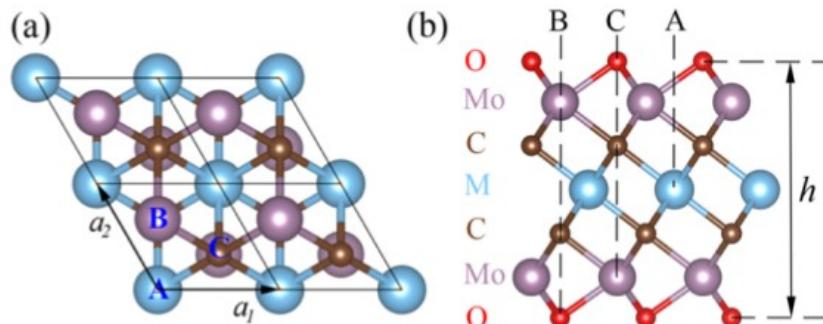
# Large-Gap Quantum Spin Hall State in MXenes: *d*-Band Topological Order in a Triangular Lattice

Chen Si,<sup>†,‡</sup> Kyung-Hwan Jin,<sup>§</sup> Jian Zhou,<sup>†</sup> Zhimei Sun,<sup>\*,†,‡</sup> and Feng Liu<sup>§</sup>

<sup>†</sup>School of Materials Science and Engineering, Beihang University, Beijing 100191, China

<sup>‡</sup>Center for Integrated Computational Materials Engineering, International Research Institute for Multidisciplinary Science, Beihang University, Beijing 100191, China

<sup>§</sup>Department of Materials Science and Engineering, University of Utah, Salt Lake City, Utah 84112, United States



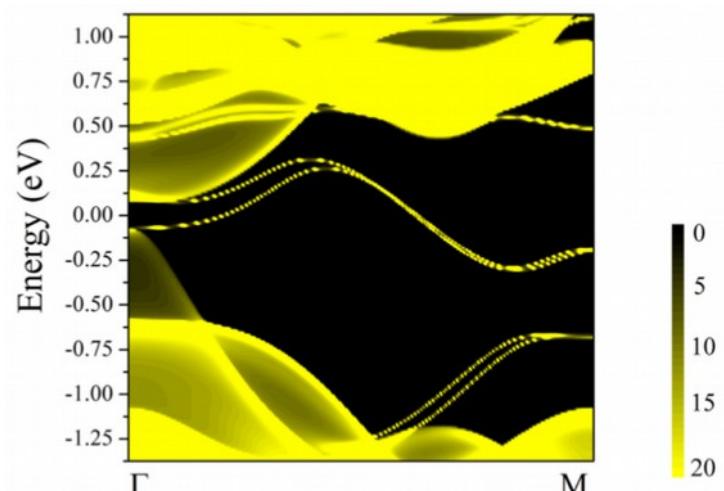
**Figure 1.** (a) Top view of the crystal structure of  $\text{Mo}_2\text{MC}_2$  ( $\text{M} = \text{Ti}$ ,  $\text{Zr}$ , or  $\text{Hf}$ ) MXene displaying the hexagonal unit cell with Bravais lattice vectors  $a_1$  and  $a_2$ . (b) Side view of the crystal structure of  $\text{Mo}_2\text{MC}_2\text{O}_2$ .  $h$  denotes the thickness of septuple atomic layers of  $\text{Mo}_2\text{MC}_2\text{O}_2$ .

**Table 1.** Lattice Constants ( $a$ ), Thickness ( $h$ ), Nontrivial Gaps at the  $\Gamma$  Point ( $E_\Gamma$ ), Indirect Bulk Gaps ( $E_{\text{bulk}}$ ), and  $Z_2$  Topological Invariants for  $\text{Mo}_2\text{MC}_2\text{O}_2$ <sup>a</sup>

compound	$\text{Mo}_2\text{TiC}_2\text{O}_2$	$\text{Mo}_2\text{ZrC}_2\text{O}_2$	$\text{Mo}_2\text{HfC}_2\text{O}_2$
$a$ (Å)	2.94	3.02	3.01
$h$ (Å)	7.59	7.79	7.75
$E_\Gamma$ (eV)	GGA HSE06	0.052 0.125	0.087 0.147
$E_{\text{bulk}}$ (eV)	GGA HSE06	0.041 0.096	0.066 0.105
$Z_2$	1	1	1

<sup>a</sup>The values of  $E_\Gamma$  and  $E_{\text{bulk}}$  calculated by GGA and HSE06 are all shown for comparison.

## $\text{Mo}_2\text{HfC}_2\text{O}_2$ on the zigzag edge



**Topological insulators in the ordered double transition metals  $M'_2M''C_2$  MXenes  
( $M' = \text{Mo, W}$ ;  $M'' = \text{Ti, Zr, Hf}$ )**

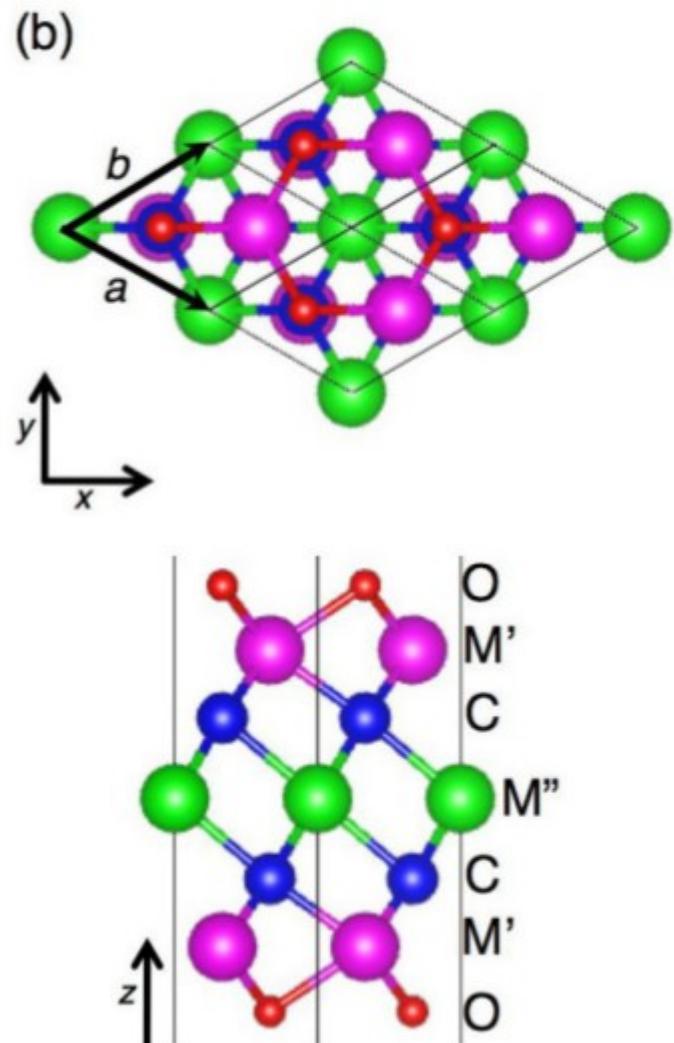
Mohammad Khazaei,<sup>1,\*</sup> Ahmad Ranjbar,<sup>1</sup> Masao Arai,<sup>2</sup> and Seiji Yunoki<sup>1,3,4</sup>

<sup>1</sup>Computational Materials Science Research Team, RIKEN Advanced Institute for Computational Science (AICS), Kobe, Hyogo 650-0047, Japan

<sup>2</sup>International Center for Materials Nanoarchitectonics, National Institute for Materials Science (NIMS), 1-1 Namiki, Tsukuba 305-0044, Ibaraki, Japan

<sup>3</sup>Computational Condensed Matter Physics Laboratory, RIKEN, Wako, Saitama 351-0198, Japan

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(Received 27 July 2016; revised manuscript received 7 September 2016; published 30 September 2016)



$M_2MC_2O_2$  ( $M = \text{Mo, W}; M = \text{Ti, Zr, Hf}$ ) MXenes are TIs

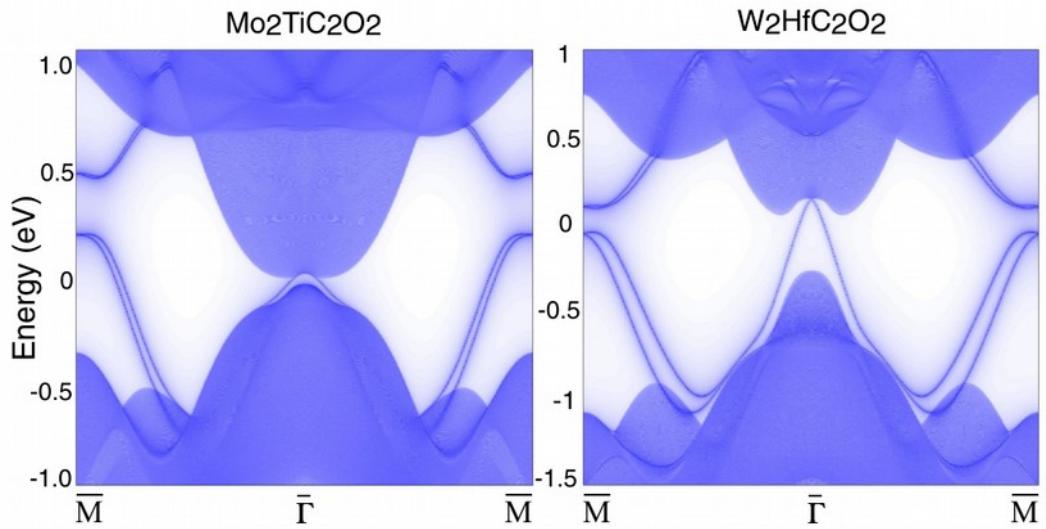
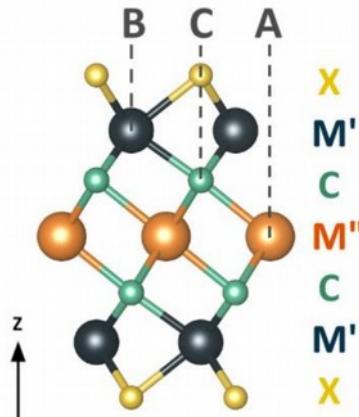


FIG. 4. Edge band structures for  $\text{Mo}_2\text{TiC}_2\text{O}_2$  and  $\text{W}_2\text{HfC}_2\text{O}_2$ . The Fermi energy is located at zero energy.

# Search

$M'_{\text{2}}M''\text{C}_2X_2$



**Yellow X** : F, Cl, Br, I, O, or H  
**Black M'** : V, Nb, or Tb  
**light green** : C  
**orange M''** : Ti, Hf, or Zr

Group Period	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	
1	1 H																2 He		
2	3 Li	4 Be											5 B	6 C	7 N	8 O	9 F	10 Ne	
3	11 Na	12 Mg											13 Al	14 Si	15 P	16 S	17 Cl	18 Ar	
4	19 K	20 Ca	21 Sc	22 Ti	23 V	24 Cr	25 Mn	26 Fe	27 Co	28 Ni	29 Cu	30 Zn	31 Ga	32 Ge	33 As	34 Se	35 Br	36 Kr	
5	37 Rb	38 Sr	39 Y	40 Zr	41 Nb	42 Mo	43 Tc	44 Ru	45 Rh	46 Pd	47 Ag	48 Cd	49 In	50 Sn	51 Sb	52 Te	53 I	54 Xe	
6	55 Cs	56 Ba	57 La	*	72 Hf	73 Ta	74 W	75 Re	76 Os	77 Ir	78 Pt	79 Au	80 Hg	81 Tl	82 Pb	83 Bi	84 Po	85 At	86 Rn
7	87 Fr	88 Ra	89 Ac	*	104 Rf	105 Db	106 Sg	107 Bh	108 Hs	109 Mt	110 Ds	111 Rg	112 Cn	113 Nh	114 Fl	115 Mc	116 Lv	117 Ts	118 Og
	*	58 Ce	59 Pr	60 Nd	61 Pm	62 Sm	63 Eu	64 Gd	65 Tb	66 Dy	67 Ho	68 Er	69 Tm	70 Yb	71 Lu				
	*	90 Th	91 Pa	92 U	93 Np	94 Pu	95 Am	96 Cm	97 Bk	98 Cf	99 Es	100 Fm	101 Md	102 No	103 Lr				

# Computational Method

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Package: Vienna Ab initio simulation package ([VASP 5.4.4](#))

Pseudopotential: Projector augmented wave method ([PAW](#))

Exchange-correction: Generalized Gradient Approximation ([PBE](#))

k-point grid: [12x12x1](#) Gamma-center Monkhorst-Pack

Cut off energy: [400 eV](#)

vacuum space : [~20 Å](#)

forces : < [10<sup>-3</sup> eV/Å](#) in fully relaxed structures

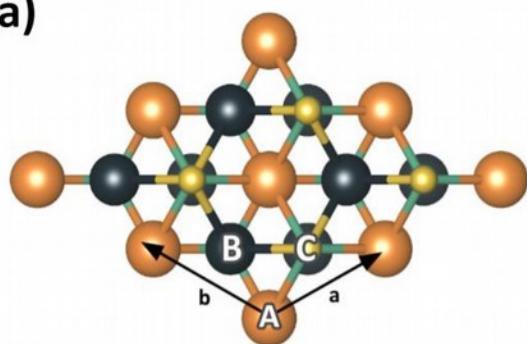
convergence criteria : [10<sup>-6</sup>eV](#)

# Crystal structure of $M'_2M''C_2X_2$



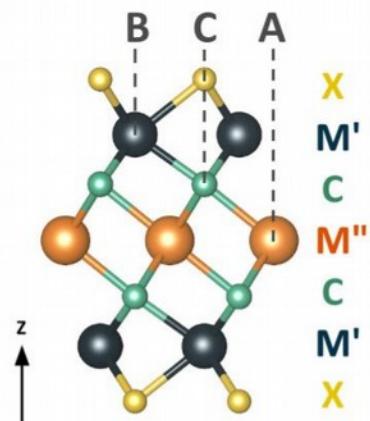
Top view

(a)



(b)

Side view



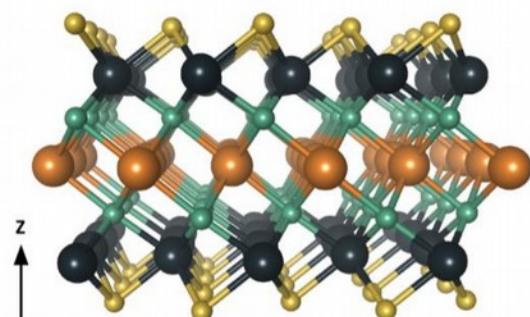
**Black M'** : V, Nb, or Tb

**orange M''** : Ti, Hf, or Zr

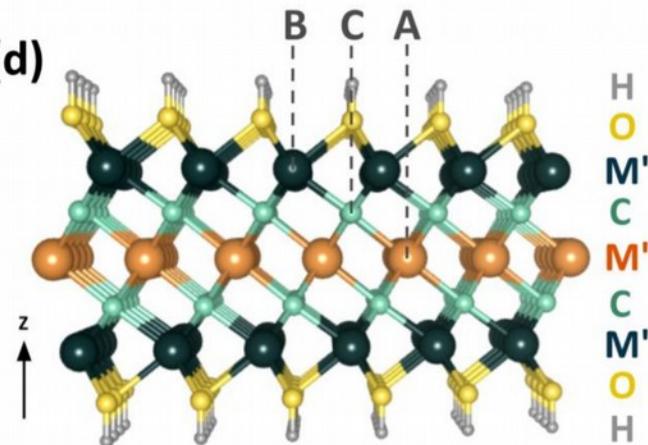
**light green** : C

**Yellow X** : F, Cl, Br, I, O, H, OH

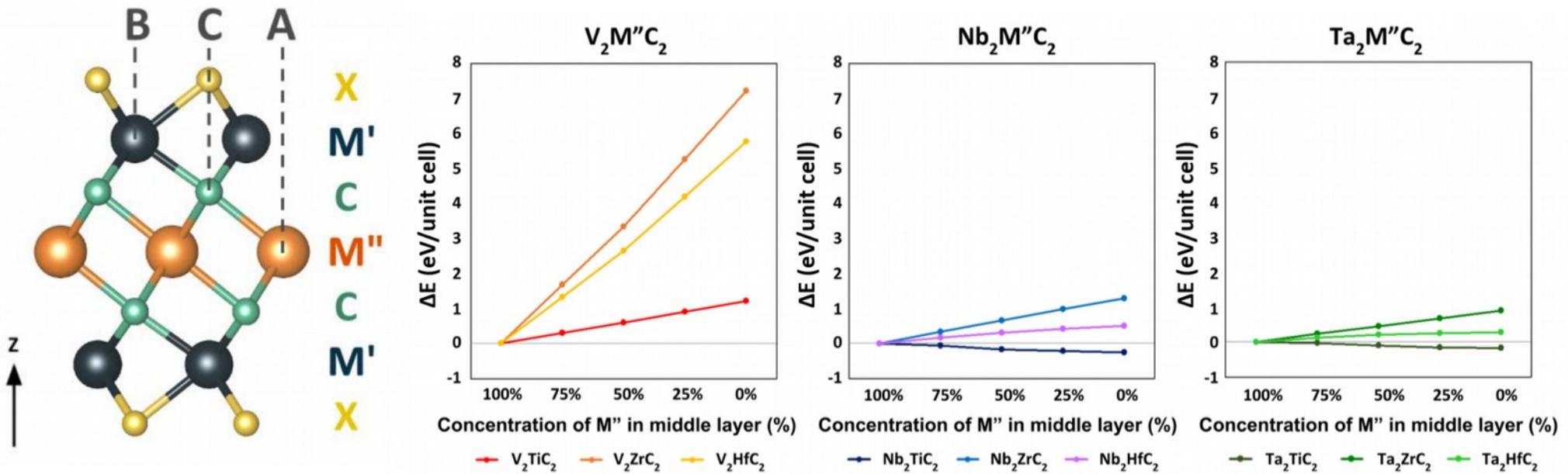
(c)



(d)



# Order Double Transition Metals MXenes



The 100% concentration of M'' in the middle layer corresponds to the fully ordered structure.

Most of them are order, except Nb<sub>2</sub>TiC<sub>2</sub> and Ta<sub>2</sub>TiC<sub>2</sub>.

# $V_2TiC_2X_2$ ( $X=F, Cl, Br, I, O, OH$ )

	Lattice constant(Å)	$Z_2$	System band gap (meV)	$\Gamma$ -point band gap (meV)
$V_2TiC_2F_2$	2.86	1	37	39
$V_2TiC_2Cl_2$	3.02	1	-187	12
$V_2TiC_2Br_2$	3.10	1	-446	135
$V_2TiC_2I_2$	3.24	1	-463	270
$V_2TiC_2O_2$	2.88	0	-788	14
$V_2TiC_2H_2$	2.88	1	-419	29
$V_2TiC_2(OH)_2$	2.84	1	-151	48

**Table 1.** The lattice constant,  $Z_2$  topological invariant, system band gap, and  $\Gamma$ -point band gap of  $V_2TiC_2X_2$  ( $X = F, Cl, Br, I, O, H$ , or  $OH$ ).

$V_2TiC_2X_2$  (where  $X = F, Cl, I, Br, H$ , or  $OH$ ) are topological semimetals, and only  $V_2TiC_2O_2$  is a trivial insulator

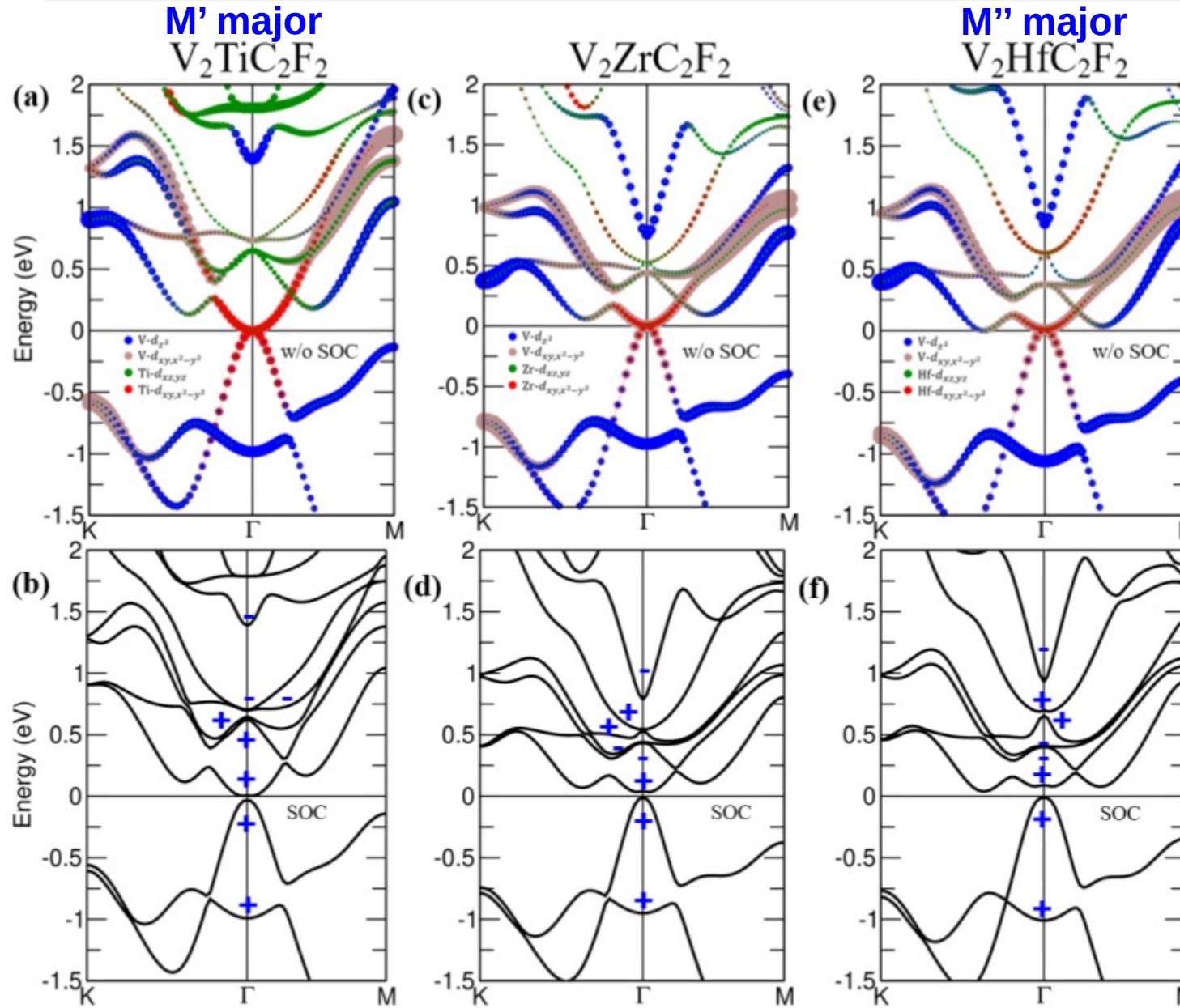
## **M'₂M''C₂F₂ (M'=V,Nb,Ta ; M''=Ti,Zr,Hf)**

Lattice constant (Å)	Z <sub>2</sub>	System band gap	Γ-point band gap (meV)
		(meV) PBE(HSE06)	PBE(HSE06)
V <sub>2</sub> TiC <sub>2</sub> F <sub>2</sub>	2.86	1 37 (212)	39 (248)
V <sub>2</sub> ZrC <sub>2</sub> F <sub>2</sub>	2.99	1 48 (192)	55 (252)
V <sub>2</sub> HfC <sub>2</sub> F <sub>2</sub>	2.96	1 49 (295)	101 (389)
Nb <sub>2</sub> TiC <sub>2</sub> F <sub>2</sub>	3.00	1 53 (223)	82 (259)
Nb <sub>2</sub> ZrC <sub>2</sub> F <sub>2</sub>	3.07	1 4 (139)	110 (263)
Nb <sub>2</sub> HfC <sub>2</sub> F <sub>2</sub>	3.04	1 -6 (130)	217 (399)
Ta <sub>2</sub> TiC <sub>2</sub> F <sub>2</sub>	3.01	1 5 (319)	207 (483)
Ta <sub>2</sub> ZrC <sub>2</sub> F <sub>2</sub>	3.04	1 -70 (49)	278 (489)
Ta <sub>2</sub> HfC <sub>2</sub> F <sub>2</sub>	3.05	1 -23 (128)	424 (658)

**Table 2.** The lattice constant, Z<sub>2</sub> topological invariant, system band gap, and Γ-point band gap by PBE and HSE06 of M'₂M''C₂F₂ (M' = V, Nb, or Ta ; M'' = Ti, Zr, or Hf). The values in the parentheses are obtained by hybrid functional calculations.

Since PBE will underestimate the band gap, HSE06 will give a more accurate band gap. The topological phase is the same in PBE and HSE06 calculations.

# Band structures



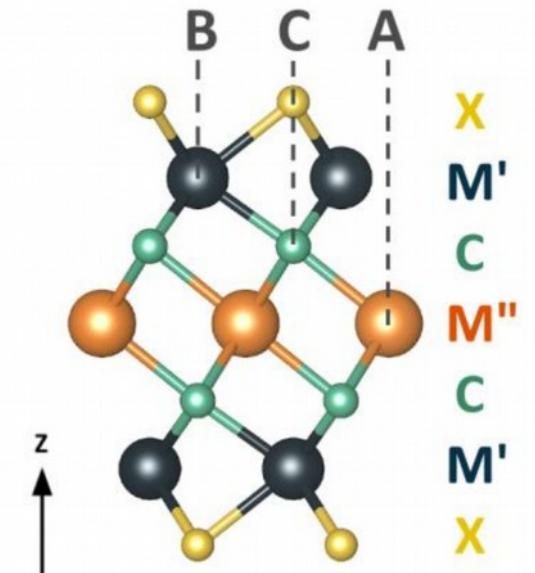
brown M' : V  $d_{xy}+d_{x^2-y^2}$

red M'' : Ti  $d_{xy}+d_{x^2-y^2}$

At  $\Gamma$  gap

V<sub>2</sub>TiC<sub>2</sub>F<sub>2</sub> : Ti  $d_{xy}+d_{x^2-y^2}$

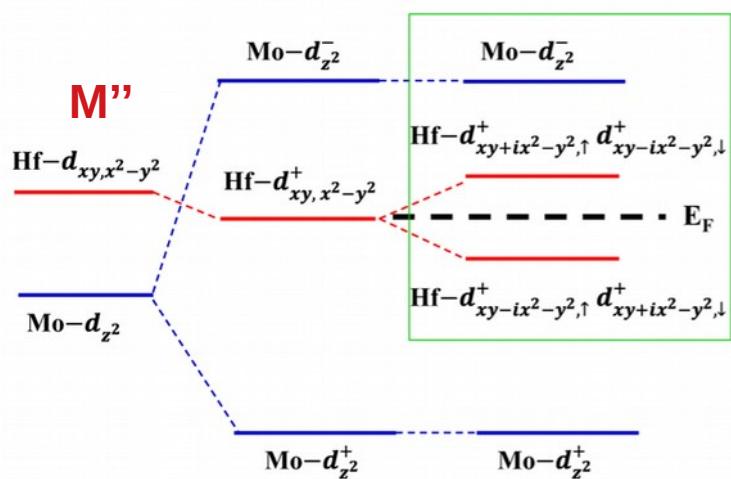
V<sub>2</sub>HfC<sub>2</sub>F<sub>2</sub> : V  $d_{xy}+d_{x^2-y^2}$



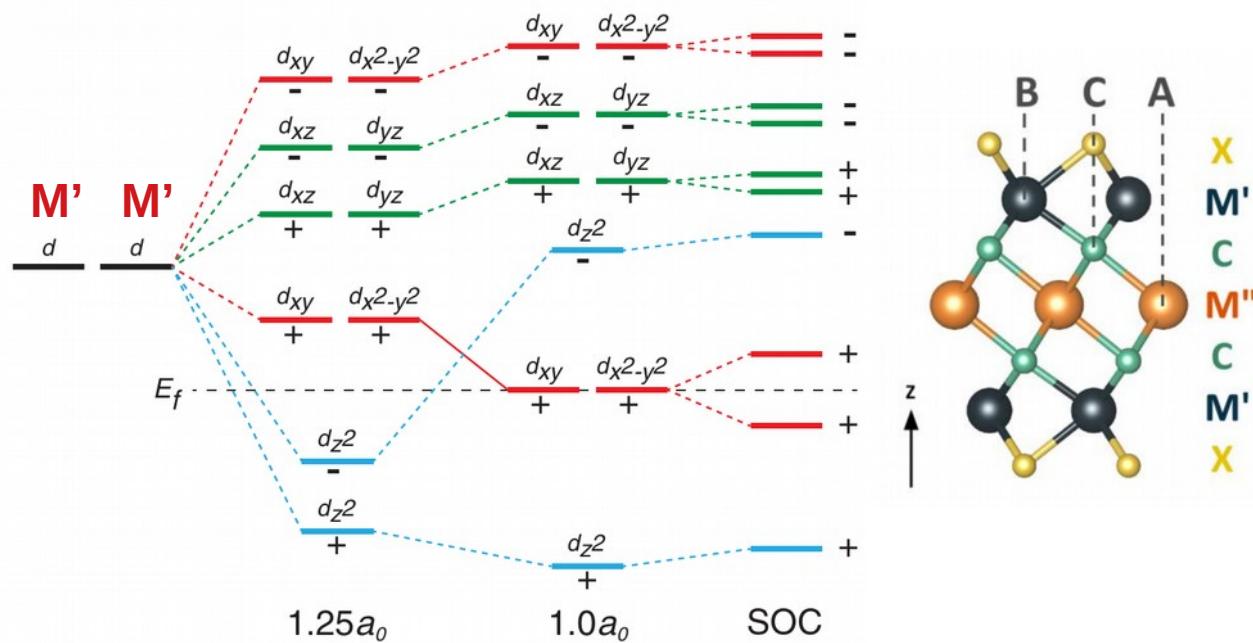
# Different mechanism at $\Gamma$ point

$\text{Mo}_2\text{M''C}_2\text{O}_2$  ( $\text{M''}=\text{Ti,Zr,Hf}$ )

(a)



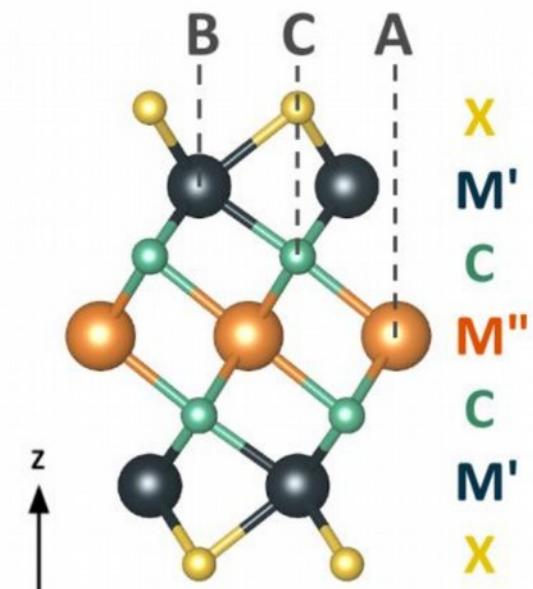
$\text{M'}_2\text{M''C}_2\text{O}_2$  ( $\text{M'}=\text{Mo,W}$  ;  $\text{M''}=\text{Ti,Zr,Hf}$ )



# Band gaps at the $\Gamma$ point

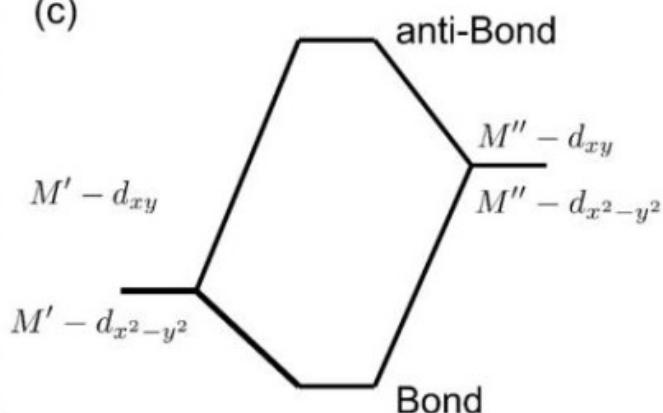
$M'{}_2M''C_2F_2$	SOC gap (eV) at $\Gamma$			$d_{xy} + d_{x^2-y^2}$ orbitals at $\Gamma$	
	$M' \& M''$	$M'$	$M''$	Contribution from $M'$	Contribution from $M''$
$V_2TiC_2F_2$	0.0393	0.0245	0.0120	0.231	0.367
$V_2ZrC_2F_2$	0.0553	0.0258	0.0254	0.258	0.232
$V_2HfC_2F_2$	0.1014	0.0203	0.0753	0.244	0.174
$Nb_2TiC_2F_2$	0.0821	0.0654	0.0141	0.182	0.400
$Nb_2ZrC_2F_2$	0.1104	0.0691	0.0372	0.196	0.309
$Nb_2HfC_2F_2$	0.2167	0.0692	0.1416	0.201	0.298
$Ta_2TiC_2F_2$	0.2070	0.1871	0.0163	0.142	0.462
$Ta_2ZrC_2F_2$	0.2777	0.2268	0.0458	0.173	0.369
$Ta_2HfC_2F_2$	0.4237	0.2513	0.1613	0.190	0.334

Gap induced by  $M'$  and  $M''$

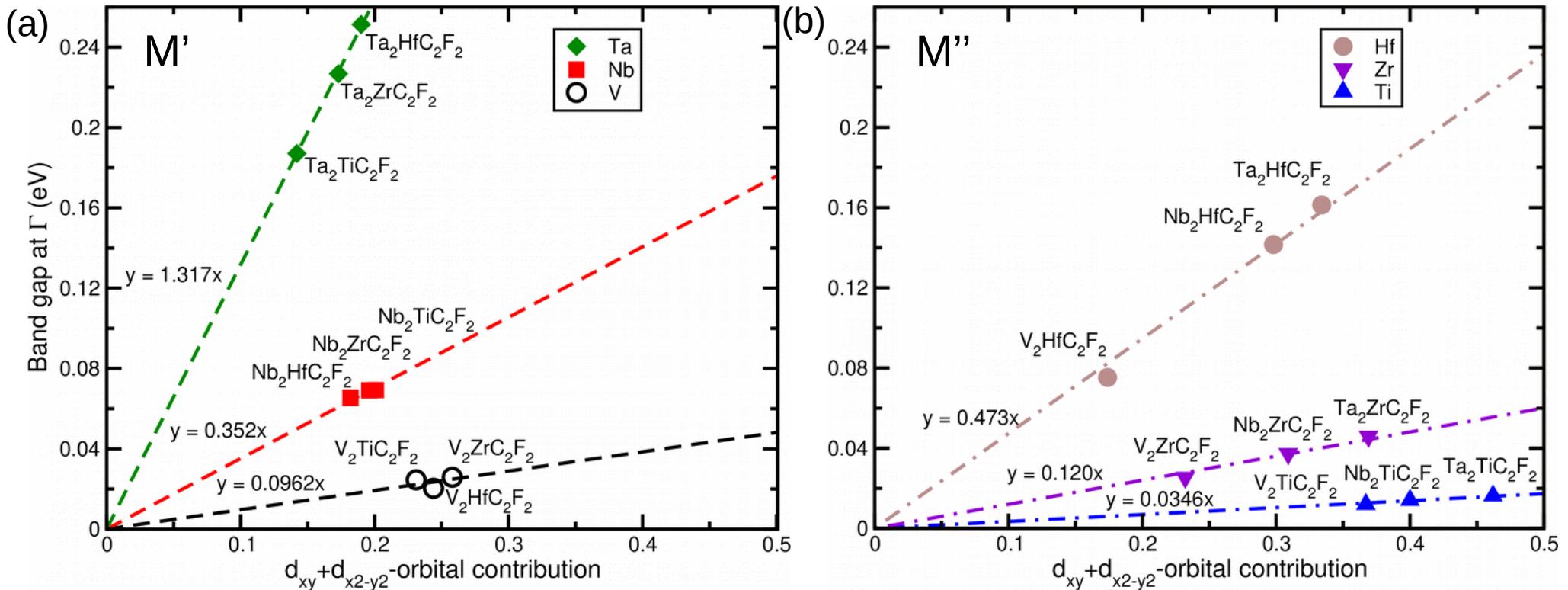


# Band gaps at the $\Gamma$ point

$M'{}_2M''C_2F_2$	SOC gap (eV) at $\Gamma$			$d_{xy} + d_{x^2-y^2}$ orbitals at $\Gamma$	
	$M' \& M''$	$M'$	$M''$	Contribution from $M'$	Contribution from $M''$
$V_2TiC_2F_2$	0.0393	0.0245	0.0120	0.231	0.367
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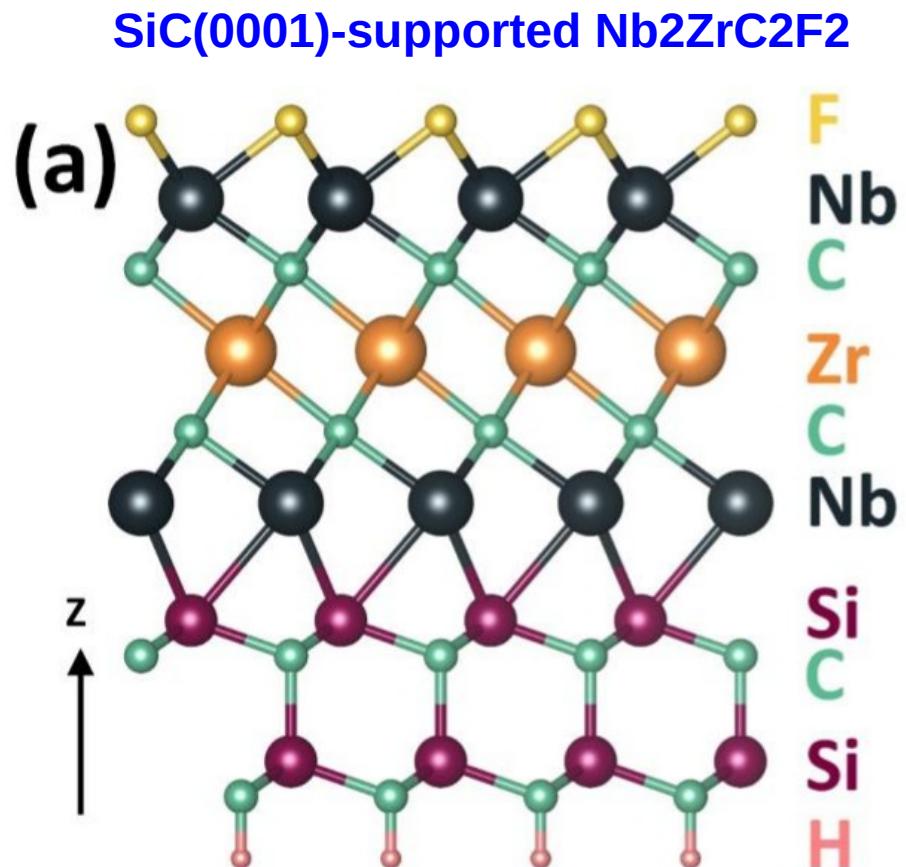
# Band gaps at the $\Gamma$ point



linear combination

$$Gap \sim \langle d_{M'} | \Psi \rangle^2 \lambda_{\text{SOC}}(M') + \langle d_{M''} | \Psi \rangle^2 \lambda_{\text{SOC}}(M'')$$

# The substrate supported MXenes



Red dots : the contribution from Nb and Zr atoms

# Conclusions

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- Some ordered double-transition metal MXenes,  $M'_2M''C_2X_2$  ( $M' = V, Nb$ , or  $Ta$ ;  $M'' = Ti, Zr$ , or  $Hf$  ;  $X = F, Cl, Br, I, H$ , or  $OH$ ) are topological insulators by first-principles calculation.
- Atomic and orbital contribution analyses show that majority of the contribution in the bands near fermi level at the  $\Gamma$ -point are from  $d_{xy}$  and  $d_{x^2-y^2}$  orbitals of the transition metal  $M'$  and  $M''$ .
- Propose SiC(0001) as a candidate substrate for material realization