

Searching beyond the SM

“...the direct method may be used...but indirect methods will be needed in order to secure victory.”

“...there are not more than two methods of attack – the direct and the indirect, ... who can exhaust the possibilities of their combination?”

Sun Tzu, *The Art of War*

John Ellis

KING'S
College
LONDON

Where are we?

Summary of the Standard Model

- Particles and $SU(3) \times SU(2) \times U(1)$ quantum numbers:

L_L	$\begin{pmatrix} \nu_e \\ e^- \end{pmatrix}_L, \begin{pmatrix} \nu_\mu \\ \mu^- \end{pmatrix}_L, \begin{pmatrix} \nu_\tau \\ \tau^- \end{pmatrix}_L$	$(1,2,-1)$
E_R	e_R^-, μ_R^-, τ_R^-	$(1,1,-2)$
Q_L	$\begin{pmatrix} u \\ d \end{pmatrix}_L, \begin{pmatrix} c \\ s \end{pmatrix}_L, \begin{pmatrix} t \\ b \end{pmatrix}_L$	$(3,2,+1/3)$
U_R	u_R, c_R, t_R	$(3,1,+4/3)$
D_R	d_R, s_R, b_R	$(3,1,-2/3)$

- Lagrangian:

$$\begin{aligned} \mathcal{L} = & -\frac{1}{4} F_{\mu\nu}^a F^{a\ \mu\nu} \\ & + i\bar{\psi} \not{D}\psi + h.c. \\ & + \psi_i y_{ij} \psi_j \phi + h.c. \\ & + |D_\mu \phi|^2 - V(\phi) \end{aligned}$$

gauge interactions

matter fermions

Yukawa interactions

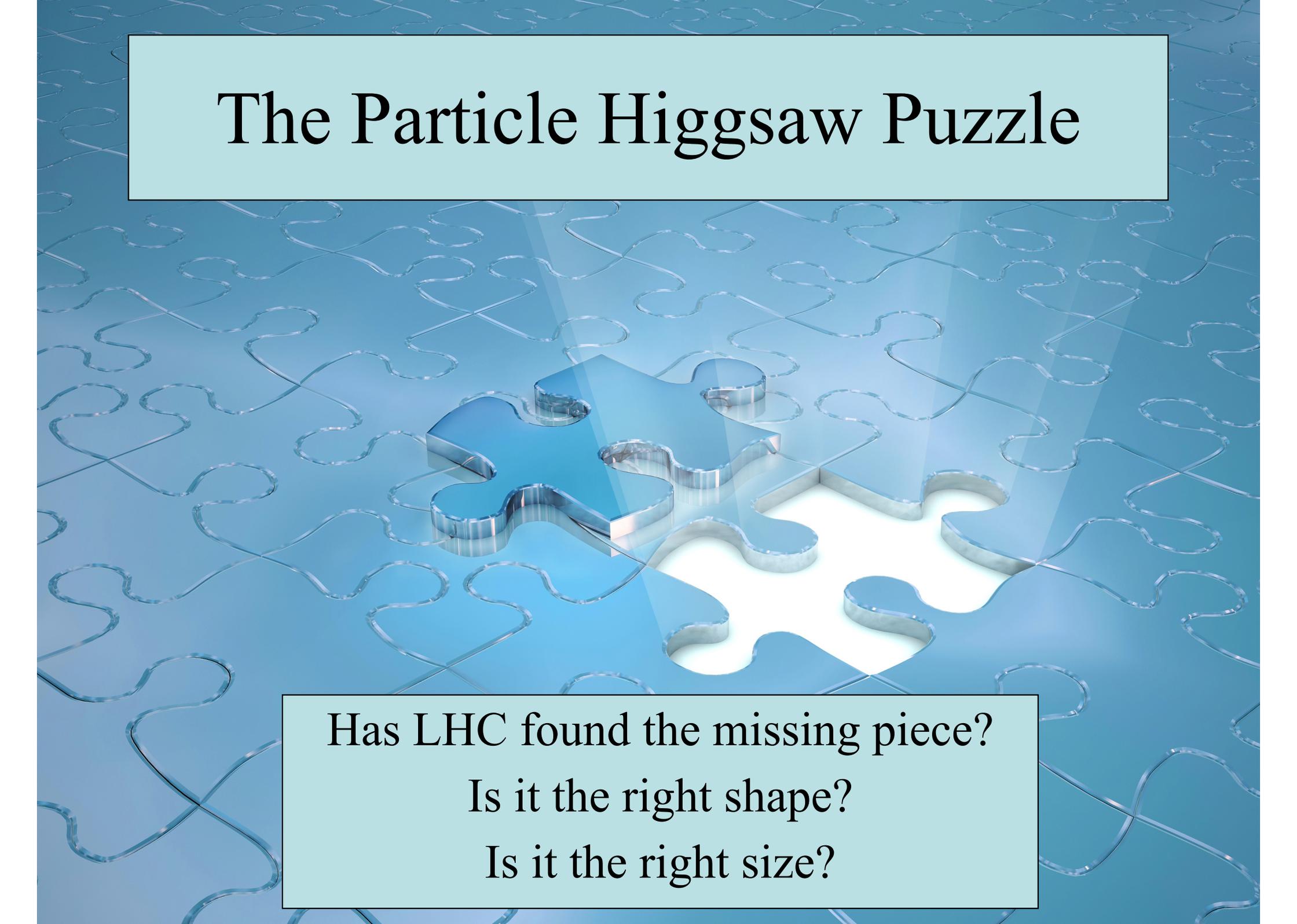
Higgs potential

Tested < 0.1%
before LHC

Testing now
in progress

What lies beyond?

The Particle Higgsaw Puzzle

The background of the slide is a blue grid with wavy, organic lines. In the center, there is a 3D rendering of a puzzle. One piece is missing, revealing a white surface underneath. The puzzle pieces are blue and have a metallic sheen.

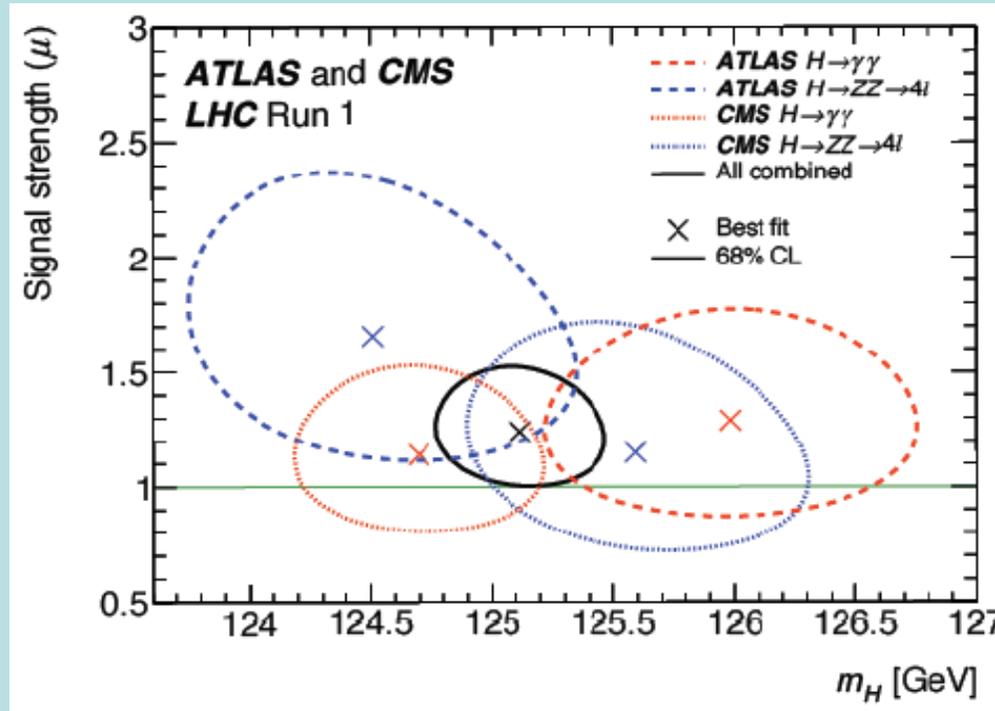
Has LHC found the missing piece?

Is it the right shape?

Is it the right size?

Higgs Mass Measurements

- ATLAS + CMS ZZ^* and $\gamma\gamma$ final states



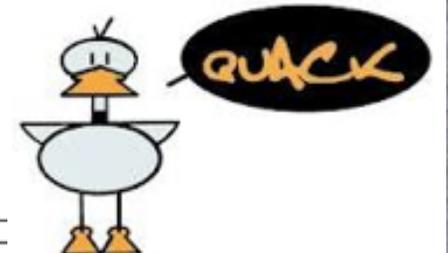
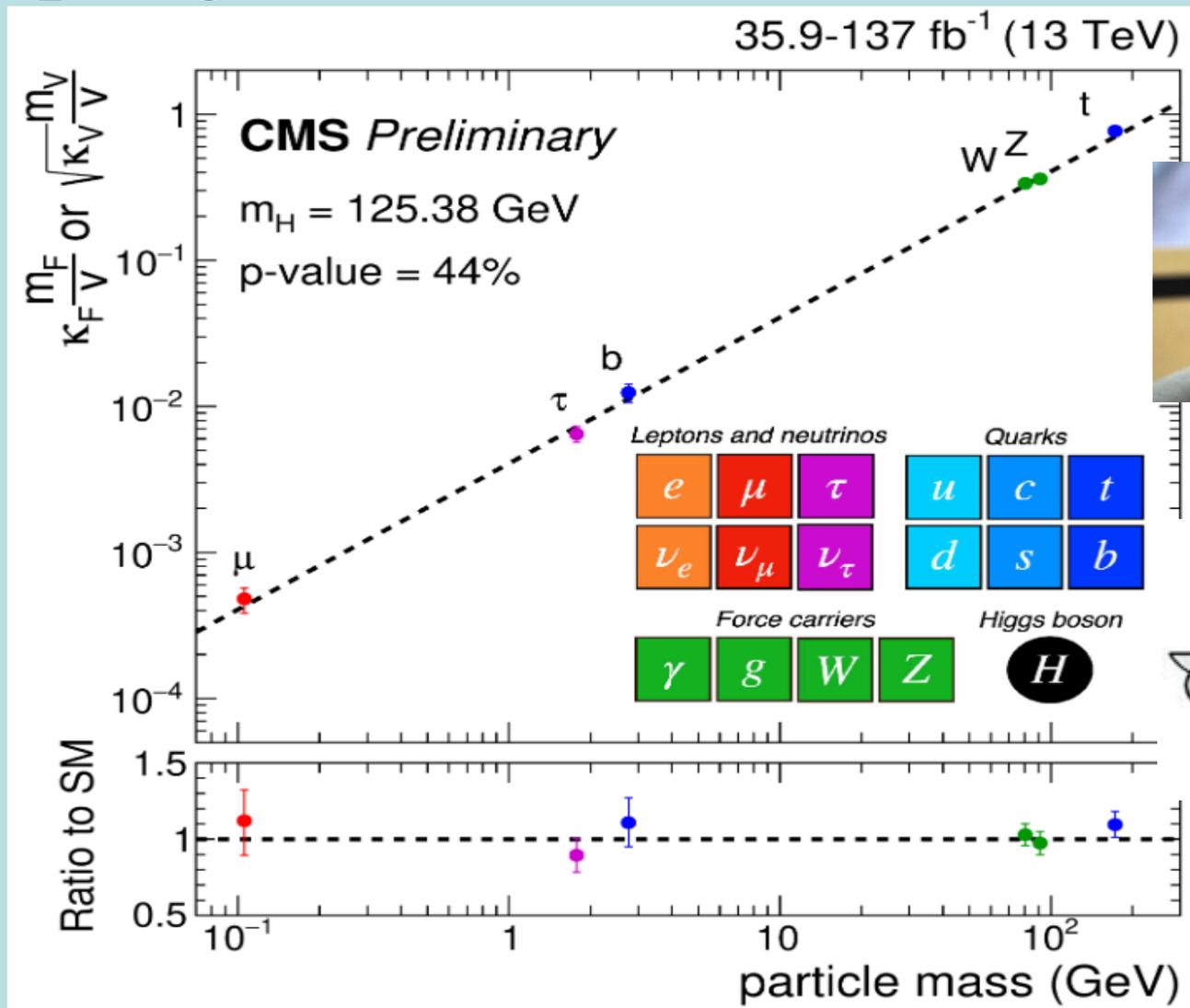
Crucial for
stability of
electroweak
vacuum

- Run 1: 125.09 ± 0.21 (stat) ± 0.11 (syst)
- ATLAS Run 2: 124.97 ± 0.24 GeV
- CMS Run 2: 125.35 ± 0.15 GeV

0.1% accuracy!

It Walks and Quacks like a Higgs

- Do couplings scale \sim mass? With scale = v ?



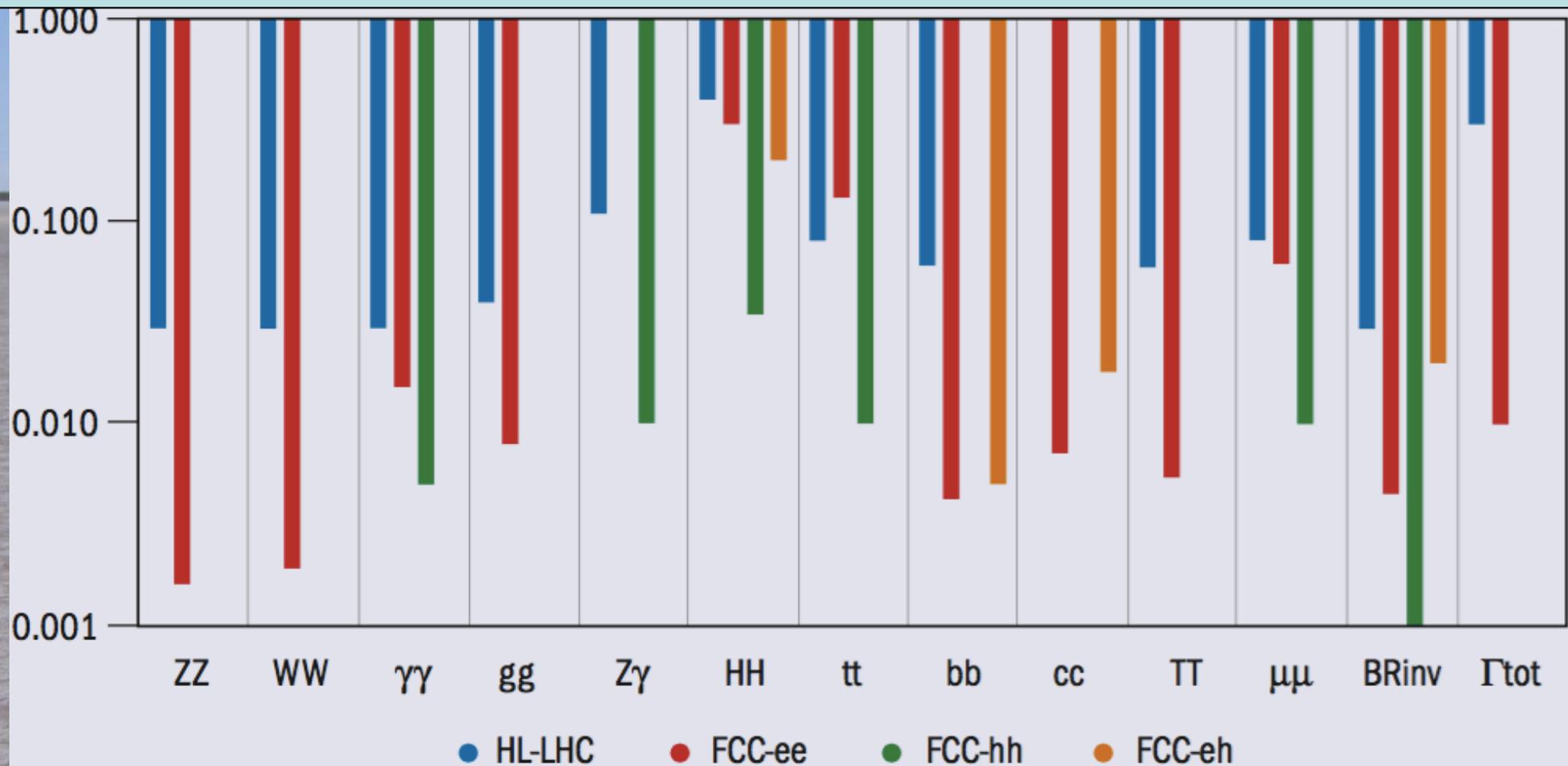
Everything about Higgs is Puzzling

$$\mathcal{L} = yH\psi\bar{\psi} + \mu^2|H|^2 - \lambda|H|^4 - V_0 + \dots$$

- Pattern of Yukawa couplings y :
 - **Flavour problem**
- Magnitude of mass term μ :
 - **Naturalness/hierarchy problem**
- Magnitude of quartic coupling λ :
 - **Stability of electroweak vacuum**
- Cosmological constant term V_0 :
 - **Dark energy**

Higher-dimensional interactions?

Possible Future Higgs Measurements



- Need to reduce theoretical uncertainties to match experimental errors
 - Needed for BSM interpretation

High precision at FCC-ee/CEPC

Big statistics at FCC-hh/SppC

Numbers of Diagrams to be Calculated

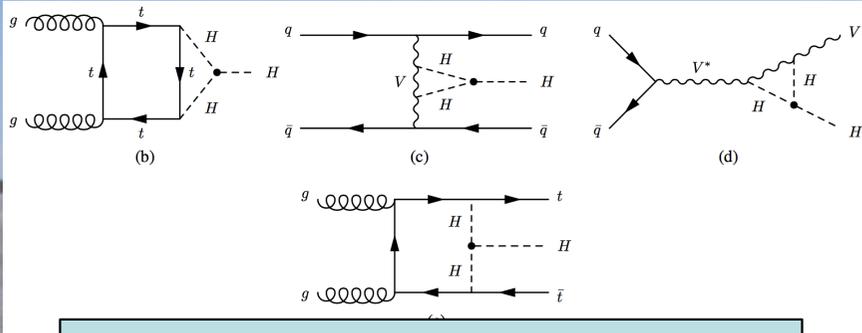
Blondel et al, arXiv:1809.01830

$Z \rightarrow b\bar{b}$			
Number of topologies	1 loop	2 loops	3 loops
		1	$14 \xrightarrow{(A)} 7 \xrightarrow{(B)} 5$
Number of diagrams	15	$2383 \xrightarrow{(A,B)} 1074$	$490387 \xrightarrow{(A,B)} 120472$
Fermionic loops	0	150	17580
Bosonic loops	15	924	102892
Planar / Non-planar	15 / 0	981/133	84059/36413
QCD / EW	1 / 14	98 / 1016	10386/110086

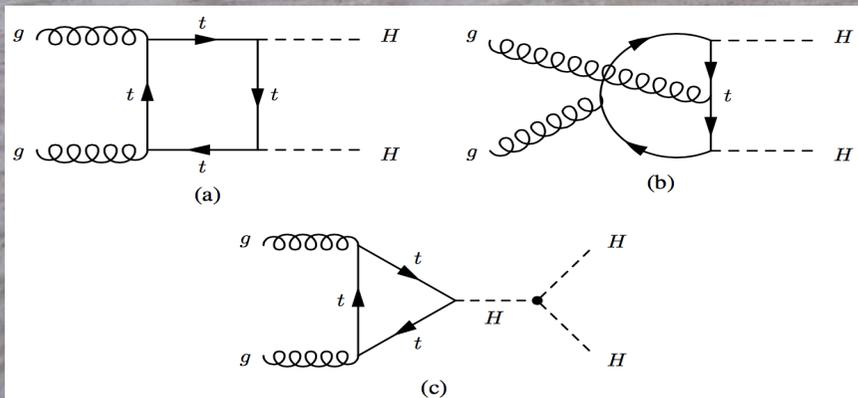
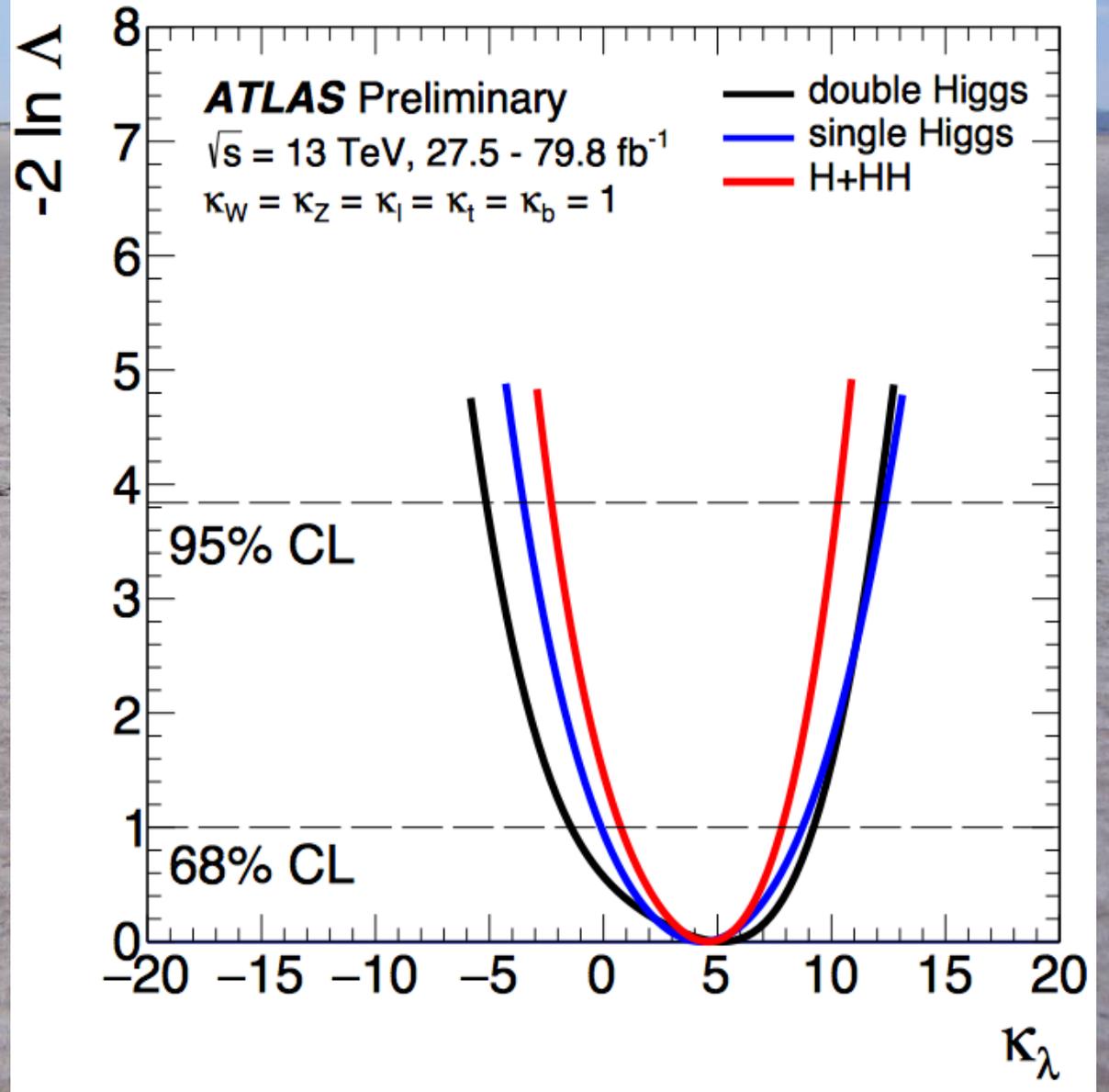
$Z \rightarrow e^+e^-, \dots$			
Number of topologies	1 loop	2 loops	3 loops
		1	$14 \xrightarrow{(A)} 7 \xrightarrow{(B)} 5$
Number of diagrams	14	$2012 \xrightarrow{(A,B)} 880$	$397690 \xrightarrow{(A,B)} 91472$
Fermionic loops	0	114	13104
Bosonic loops	14	766	78368
Planar / Non-planar	14 / 0	782/98	65487/25985
QCD / EW	0 / 14	0 / 880	144/91328

A lot of work for theorists, but feasible!

Sensitivity to HHH Coupling

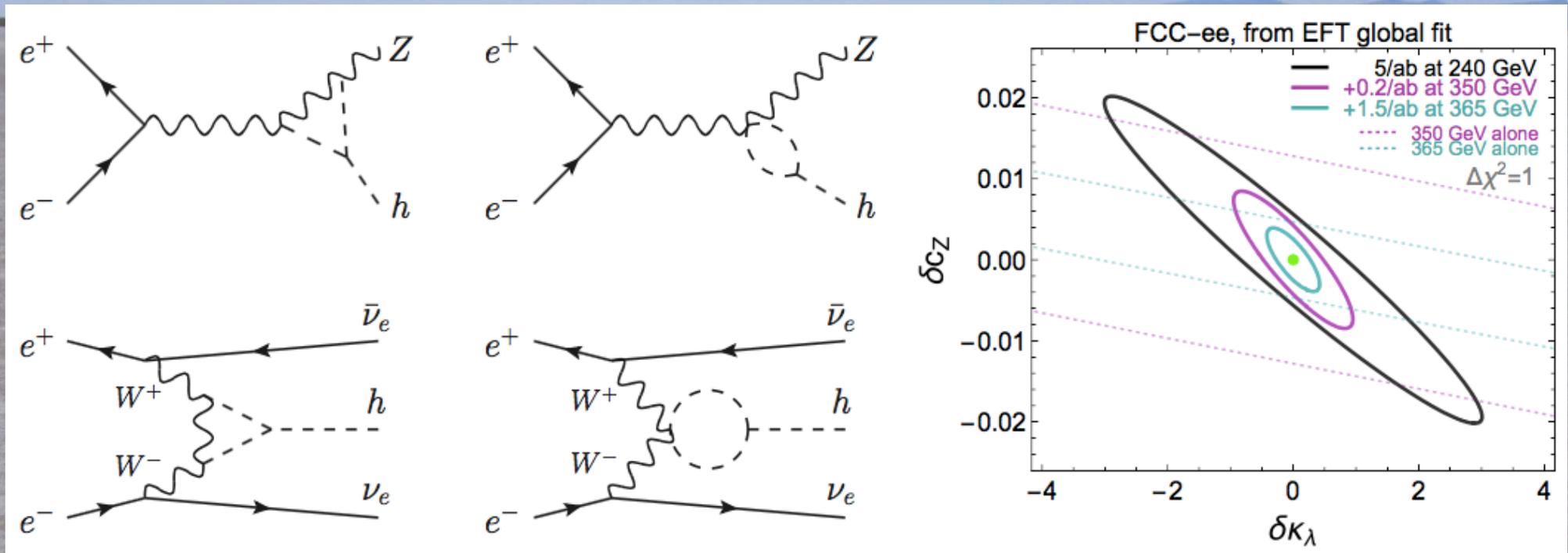


Similar sensitivities
from single and
double Higgs
production – but still
a long way to go!



Sensitivity to HHH Coupling

Sensitivity through radiative corrections



Combining all FCC-ee centre-of-mass energies: precision in κ_λ of $\pm 40\%$

Improved to $\pm 35\%$ in combination with HL-LHC

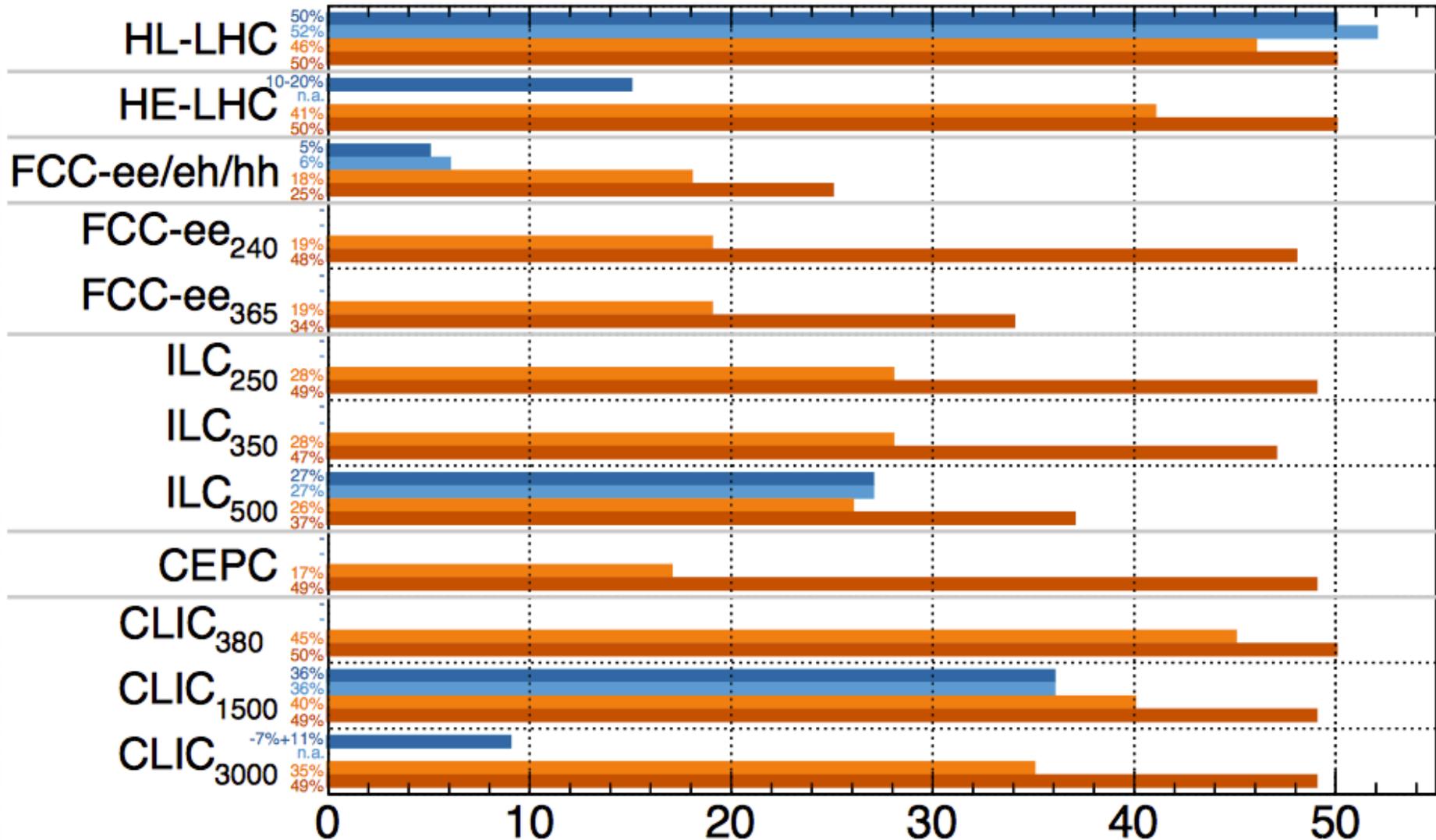
Further improved to $\pm 25\%$ when c_Z fixed to SM value.

Triple-Higgs Coupling Analyses

Higgs@FC WG

■ di-H, excl.
 ■ di-H, glob.
 ■ single-H, excl.
 ■ single-H, glob.

All future colliders combined with HL-LHC



May 2019

De Blas et al, arXiv:1905.03764

68% CL bounds on κ_3 [%]

Nothing (yet) at the LHC

No supersymmetry

Nothing else, either

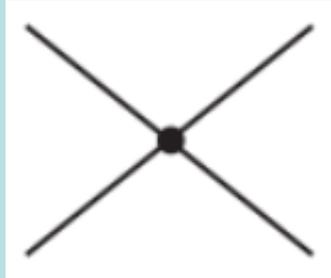


Unexplored nooks?
 Novel signatures?
 Look indirectly?

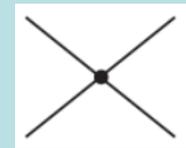
Effective Field Theories (EFTs)

a long and glorious History

- 1930's: "Standard Model" of QED had $d=4$
- Fermi's four-fermion theory of the weak force



- Dimension-6 operators: form = S, P, V, A, T?
 - Due to exchanges of massive particles?
- V-A \rightarrow massive vector bosons \rightarrow gauge theory
- Yukawa's meson theory of the strong N-N force
 - Due to exchanges of mesons? \rightarrow pions
- Chiral dynamics of pions: $(\partial\pi\partial\pi)\pi\pi$ clue \rightarrow QCD



Standard Model Effective Field Theory

- Higher-dimensional operators as relics of higher-energy physics, e.g., dimension 6:

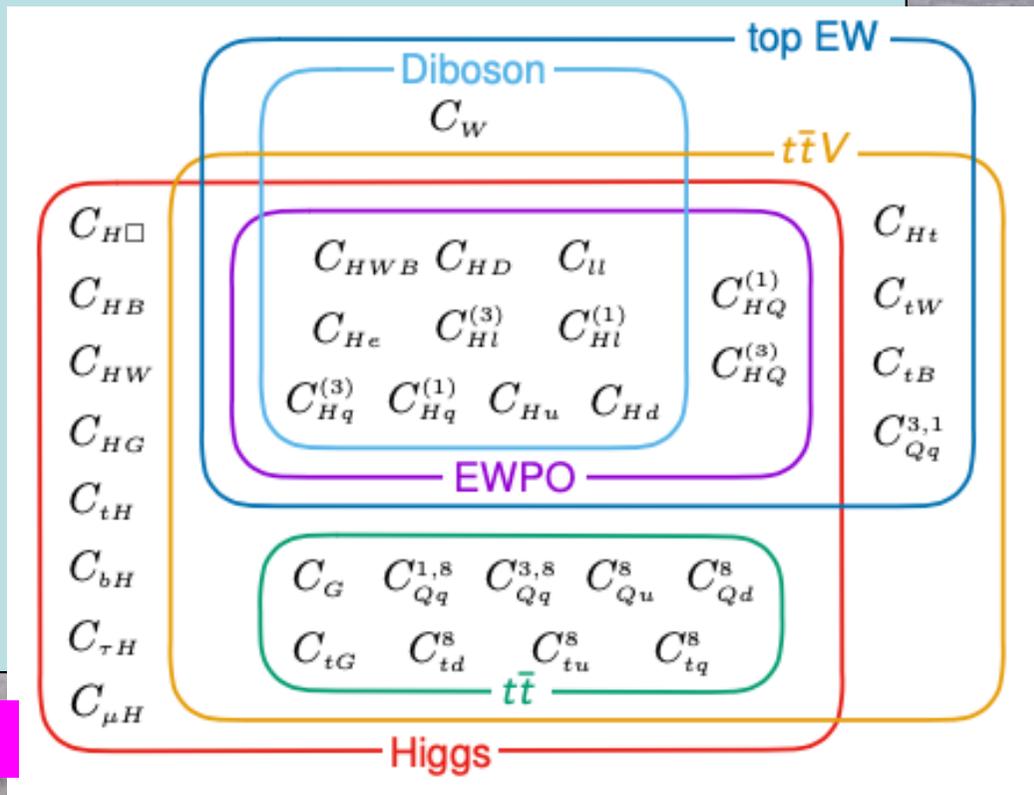
$$\mathcal{L}_{\text{eff}} = \sum_n \frac{f_n}{\Lambda^2} \mathcal{O}_n$$

- Operators constrained by $SU(2) \times U(1)$ symmetry, assuming conventional representation assignments for SM particles
- Constrain coefficients with top, EW, Higgs, diboson data
- Non-zero coefficient(s) could indicate what BSM
 - Masses, spins, quantum numbers of new particles?
 - Derivative interactions characteristic of new strong dynamics?

Global SMEFT Fit

to Top, Higgs, Diboson, Electroweak Data

- Global fit to dimension-6 operators using precision electroweak data, W^+W^- at LEP, top, Higgs and diboson data from LHC Runs 1 and 2
- Constraints on BSM
 - At tree level
 - At loop level
- Any indications?



Dimension-6 Operators in Detail

- Including 2- and 4-fermion operators
- Grey cells violate $SU(3)^5$ symmetry
- Use when including top observables

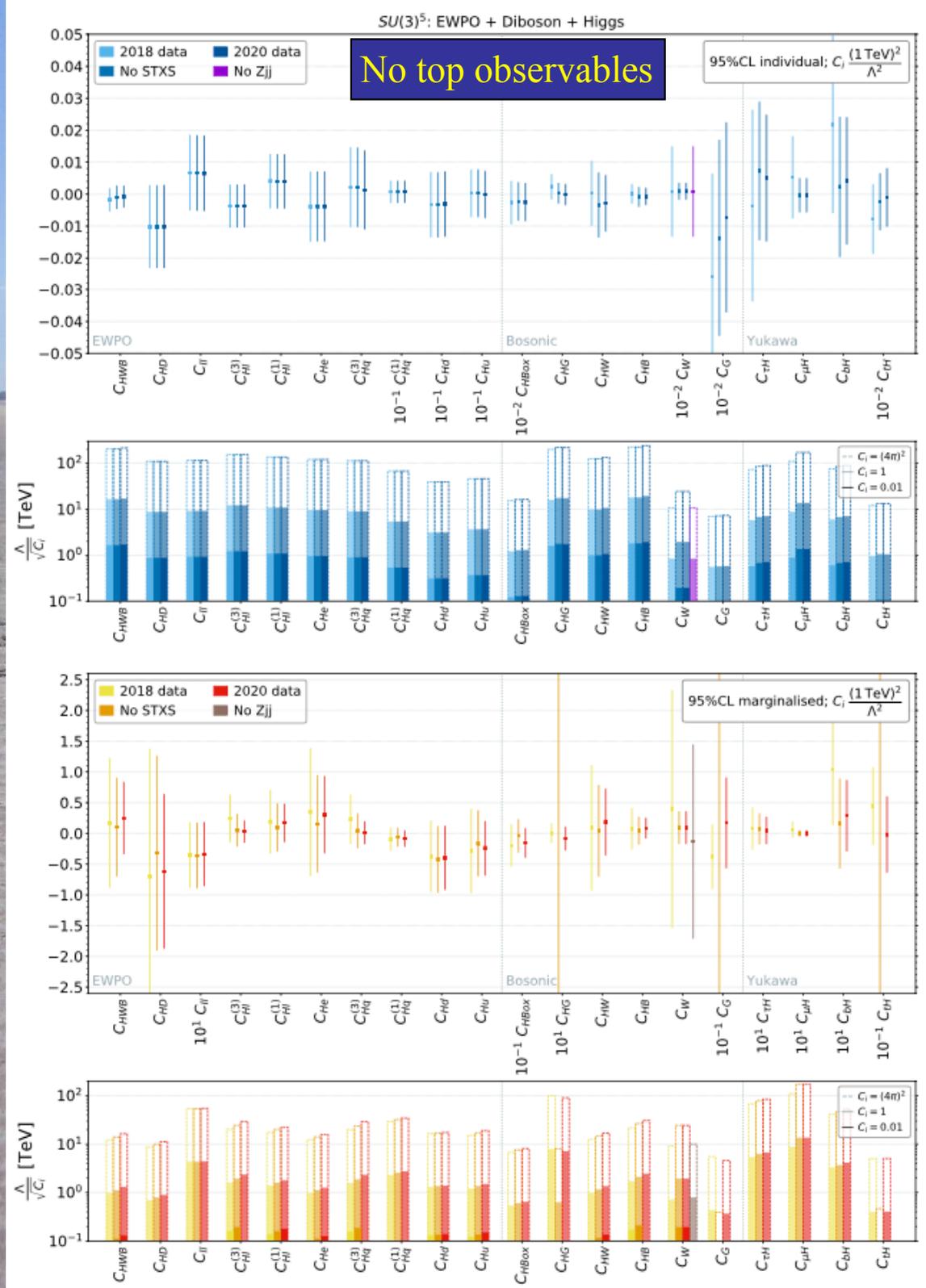
Cosmological phase transition

Derivative interaction

X^3		H^6 and $H^4 D^2$	
\mathcal{O}_G	$f^{ABC} G_{\mu\nu}^A G_{\nu\rho}^B G_{\rho\mu}^C$	\mathcal{O}_H	$(H^\dagger H)^3$
$\mathcal{O}_{\tilde{G}}$	$f^{ABC} \tilde{G}_{\mu\nu}^A G_{\nu\rho}^B G_{\rho\mu}^C$	$\mathcal{O}_{H\Box}$	$(H^\dagger H)(\Box H)$
\mathcal{O}_W	$\varepsilon^{IJK} W_{\mu\nu}^I W_{\nu\rho}^J W_{\rho\mu}^K$	\mathcal{O}_{HD}	$(H^\dagger D^\mu H)^* (H^\dagger D_\mu H)$
$\mathcal{O}_{\tilde{W}}$	$\varepsilon^{IJK} \tilde{W}_{\mu\nu}^I W_{\nu\rho}^J W_{\rho\mu}^K$		
	$X^2 H^2$		$\psi^2 XH$
\mathcal{O}_{HG}	$H^\dagger H G_{\mu\nu}^A G^{A\mu\nu}$	\mathcal{O}_{eW}	$(\bar{l}_p \sigma^{\mu\nu} e_r) \tau^I H W_{\mu\nu}^I$
$\mathcal{O}_{H\tilde{G}}$	$H^\dagger H \tilde{G}_{\mu\nu}^A G^{A\mu\nu}$	\mathcal{O}_{eB}	$(\bar{l}_p \sigma^{\mu\nu} e_r) H B_{\mu\nu}$
\mathcal{O}_{HW}	$H^\dagger H W_{\mu\nu}^I W^{I\mu\nu}$	\mathcal{O}_{uG}	$(\bar{q}_p \sigma^{\mu\nu} T^A u_r) \tilde{H} G_{\mu\nu}^A$
$\mathcal{O}_{H\tilde{W}}$	$H^\dagger H \tilde{W}_{\mu\nu}^I W^{I\mu\nu}$	\mathcal{O}_{uW}	$(\bar{q}_p \sigma^{\mu\nu} u_r) \tau^I \tilde{H} W_{\mu\nu}^I$
\mathcal{O}_{HB}	$H^\dagger H B_{\mu\nu} B^{\mu\nu}$	\mathcal{O}_{uB}	$(\bar{q}_p \sigma^{\mu\nu} u_r) \tilde{H} B_{\mu\nu}$
$\mathcal{O}_{H\tilde{B}}$	$H^\dagger H \tilde{B}_{\mu\nu} B^{\mu\nu}$	\mathcal{O}_{dG}	$(\bar{q}_p \sigma^{\mu\nu} T^A d_r) H G_{\mu\nu}^A$
\mathcal{O}_{HWB}	$H^\dagger \tau^I H W_{\mu\nu}^I B^{\mu\nu}$	\mathcal{O}_{dW}	$(\bar{q}_p \sigma^{\mu\nu} d_r) \tau^I H W_{\mu\nu}^I$
$\mathcal{O}_{H\tilde{W}B}$	$H^\dagger \tau^I H \tilde{W}_{\mu\nu}^I B^{\mu\nu}$	\mathcal{O}_{dB}	$(\bar{q}_p \sigma^{\mu\nu} d_r) H B_{\mu\nu}$
	$(\bar{L}L)(\bar{L}L)$		$(\bar{R}R)(\bar{R}R)$
\mathcal{O}_{ll}	$(\bar{l}_p \gamma_\mu l_r)(\bar{l}_s \gamma^\mu l_t)$	\mathcal{O}_{ee}	$(\bar{e}_p \gamma_\mu e_r)(\bar{e}_s \gamma^\mu e_t)$
$\mathcal{O}_{qq}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{q}_s \gamma^\mu q_t)$	\mathcal{O}_{uu}	$(\bar{u}_p \gamma_\mu u_r)(\bar{u}_s \gamma^\mu u_t)$
$\mathcal{O}_{qq}^{(3)}$	$(\bar{q}_p \gamma_\mu \tau^I q_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	\mathcal{O}_{dd}	$(\bar{d}_p \gamma_\mu d_r)(\bar{d}_s \gamma^\mu d_t)$
$\mathcal{O}_{lq}^{(1)}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{q}_s \gamma^\mu q_t)$	\mathcal{O}_{eu}	$(\bar{e}_p \gamma_\mu e_r)(\bar{u}_s \gamma^\mu u_t)$
$\mathcal{O}_{lq}^{(3)}$	$(\bar{l}_p \gamma_\mu \tau^I l_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	\mathcal{O}_{ed}	$(\bar{e}_p \gamma_\mu e_r)(\bar{d}_s \gamma^\mu d_t)$
		$\mathcal{O}_{ud}^{(1)}$	$(\bar{u}_p \gamma_\mu u_r)(\bar{d}_s \gamma^\mu d_t)$
		$\mathcal{O}_{ud}^{(8)}$	$(\bar{u}_p \gamma_\mu T^A u_r)(\bar{d}_s \gamma^\mu T^A d_t)$
			$(\bar{q}_p \gamma_\mu q_r)(\bar{e}_s \gamma^\mu e_t)$
			$(\bar{l}_p \gamma_\mu l_r)(\bar{u}_s \gamma^\mu u_t)$
			$(\bar{l}_p \gamma_\mu l_r)(\bar{d}_s \gamma^\mu d_t)$
			$(\bar{q}_p \gamma_\mu q_r)(\bar{e}_s \gamma^\mu e_t)$
			$(\bar{q}_p \gamma_\mu q_r)(\bar{u}_s \gamma^\mu u_t)$
			$(\bar{q}_p \gamma_\mu T^A q_r)(\bar{u}_s \gamma^\mu T^A u_t)$
			$(\bar{q}_p \gamma_\mu q_r)(\bar{d}_s \gamma^\mu d_t)$
			$(\bar{q}_p \gamma_\mu T^A q_r)(\bar{d}_s \gamma^\mu T^A d_t)$
	$(\bar{L}R)(\bar{R}L)$ and $(\bar{L}R)(\bar{L}R)$		B -violating
\mathcal{O}_{ledq}	$(\bar{l}_p^j e_r)(\bar{d}_s^k q_t^j)$	\mathcal{O}_{duq}	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jk} [(d_p^\alpha)^T C u_r^\beta] [(q_s^\gamma)^T C l_t^k]$
$\mathcal{O}_{quqd}^{(1)}$	$(\bar{q}_p^j u_r) \varepsilon_{jk} (\bar{q}_s^k d_t)$	\mathcal{O}_{quq}	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jk} [(q_p^\alpha)^T C q_r^\beta] [(u_s^\gamma)^T C e_t]$
$\mathcal{O}_{quqd}^{(8)}$	$(\bar{q}_p^j T^A u_r) \varepsilon_{jk} (\bar{q}_s^k T^A d_t)$	\mathcal{O}_{quq}	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jnm} [(q_p^\alpha)^T C q_r^\beta] [(u_s^\gamma)^T C l_t^m]$
$\mathcal{O}_{lequ}^{(1)}$	$(\bar{l}_p^j e_r) \varepsilon_{jk} (\bar{q}_s^k u_t)$	\mathcal{O}_{duu}	$\varepsilon^{\alpha\beta\gamma} [(d_p^\alpha)^T C u_r^\beta] [(u_s^\gamma)^T C e_t]$
$\mathcal{O}_{lequ}^{(3)}$	$(\bar{l}_p^j \sigma_{\mu\nu} e_r) \varepsilon_{jk} (\bar{q}_s^k \sigma^{\mu\nu} u_t)$		

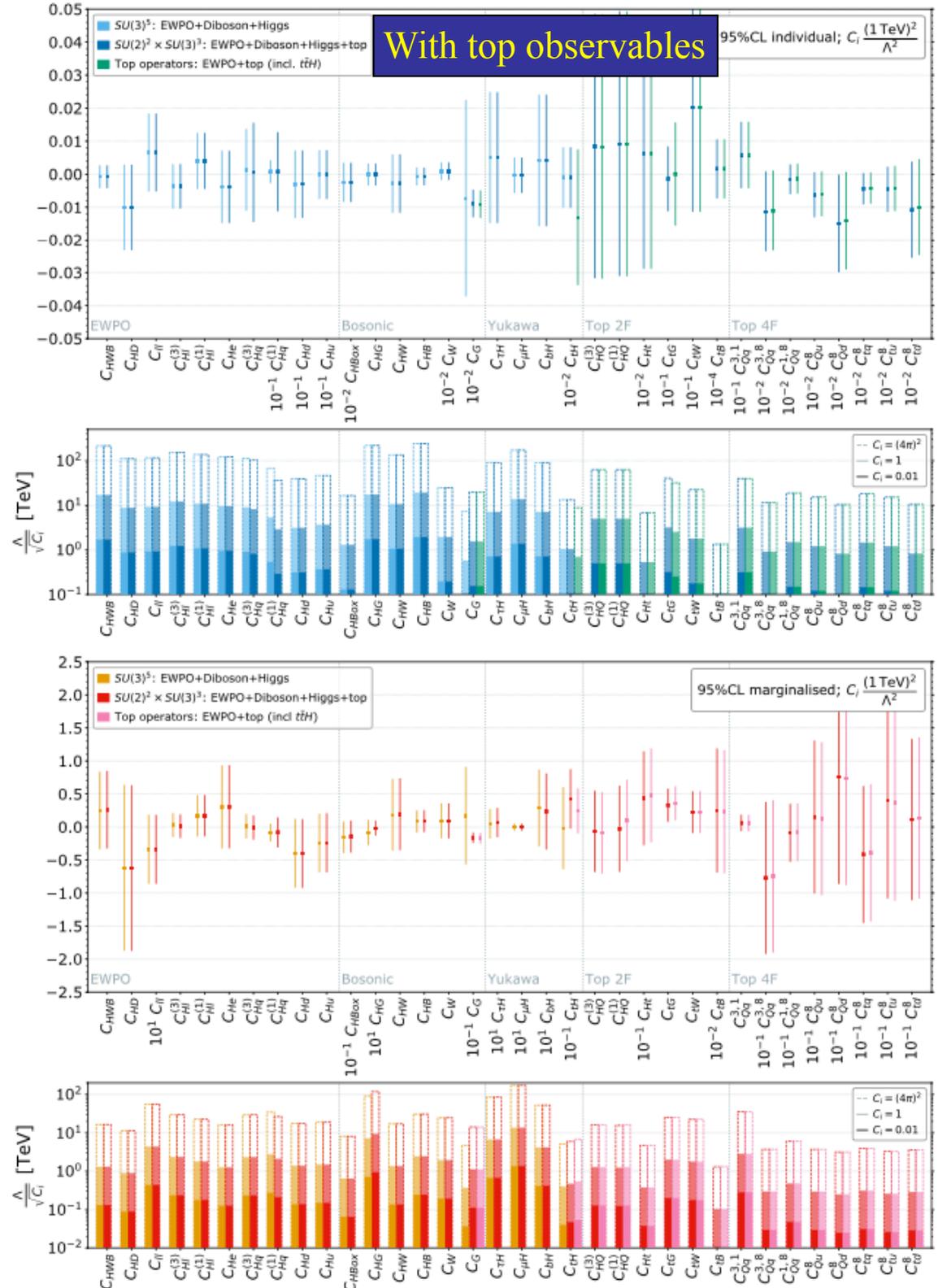
Dimension-6 Constraints with $SU(3)^5$ Symmetry

- Individual operator coefficients
- Marginalised over other operator coefficients



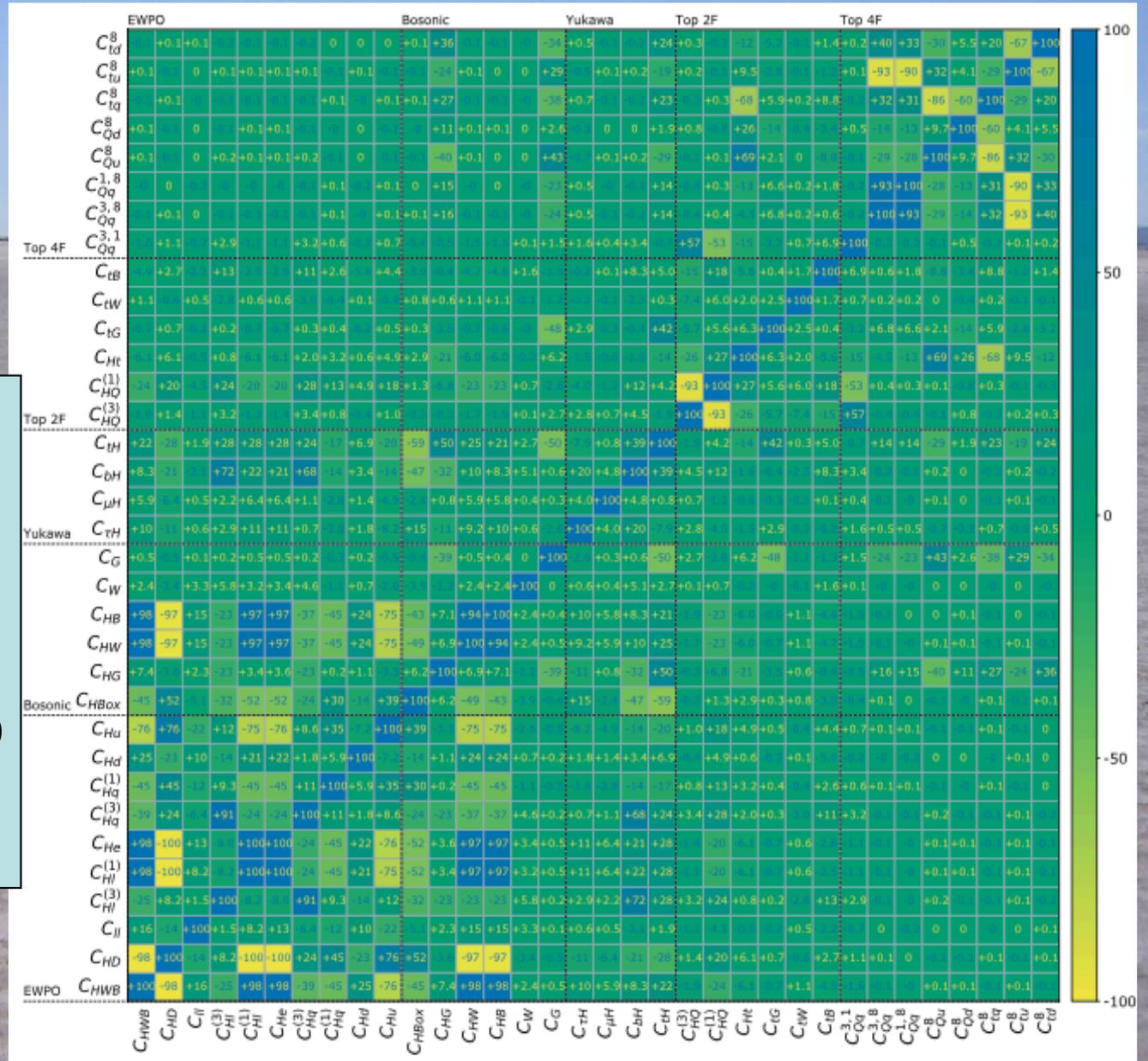
Dimension-6 Constraints with $SU(2)^2 \times SU(3)^3$

- Individual operator coefficients
- Marginalised over other operator coefficients



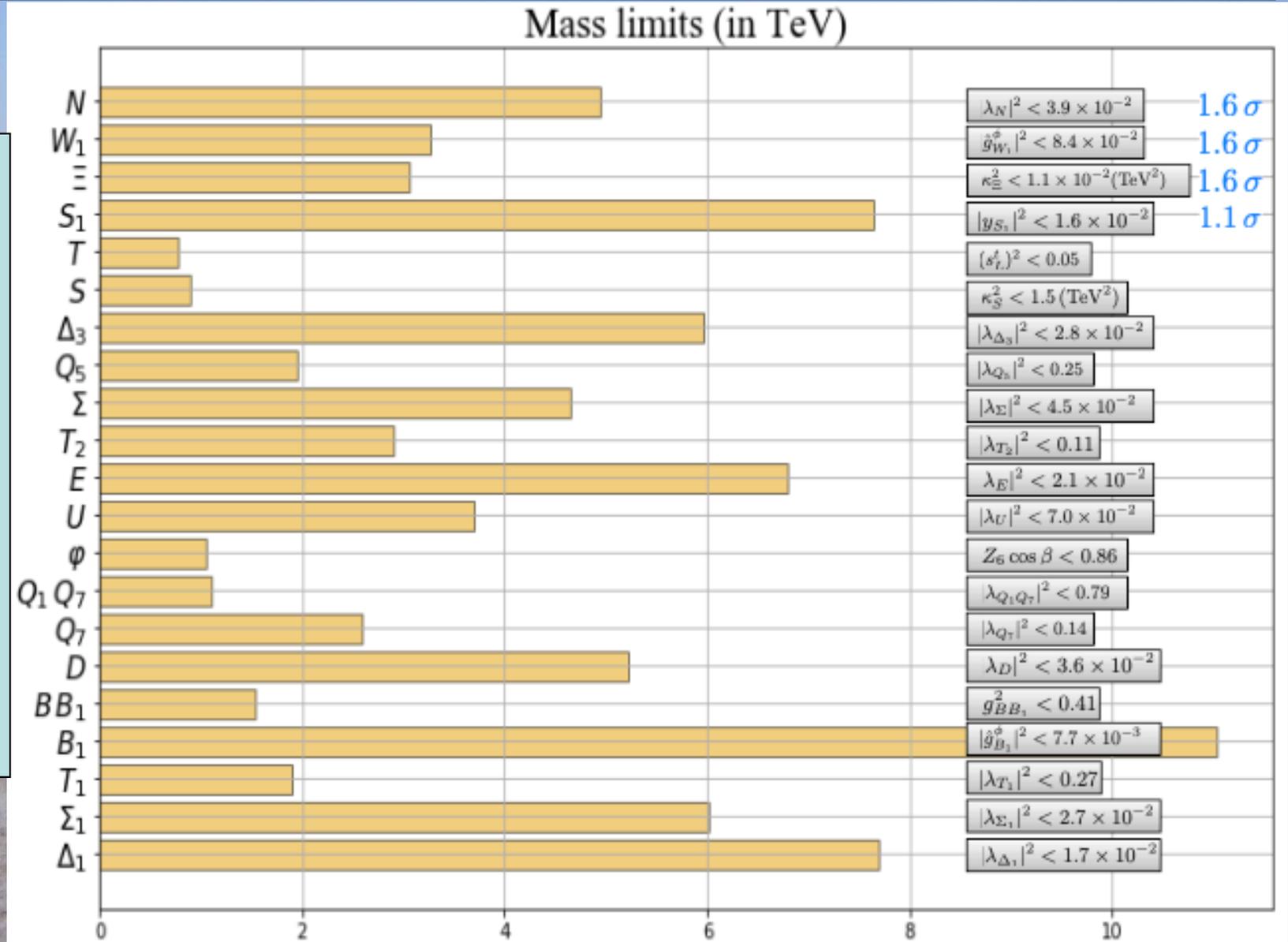
Correlation Analysis

- Main correlations within sectors
- Also significant correlations of top with other sectors

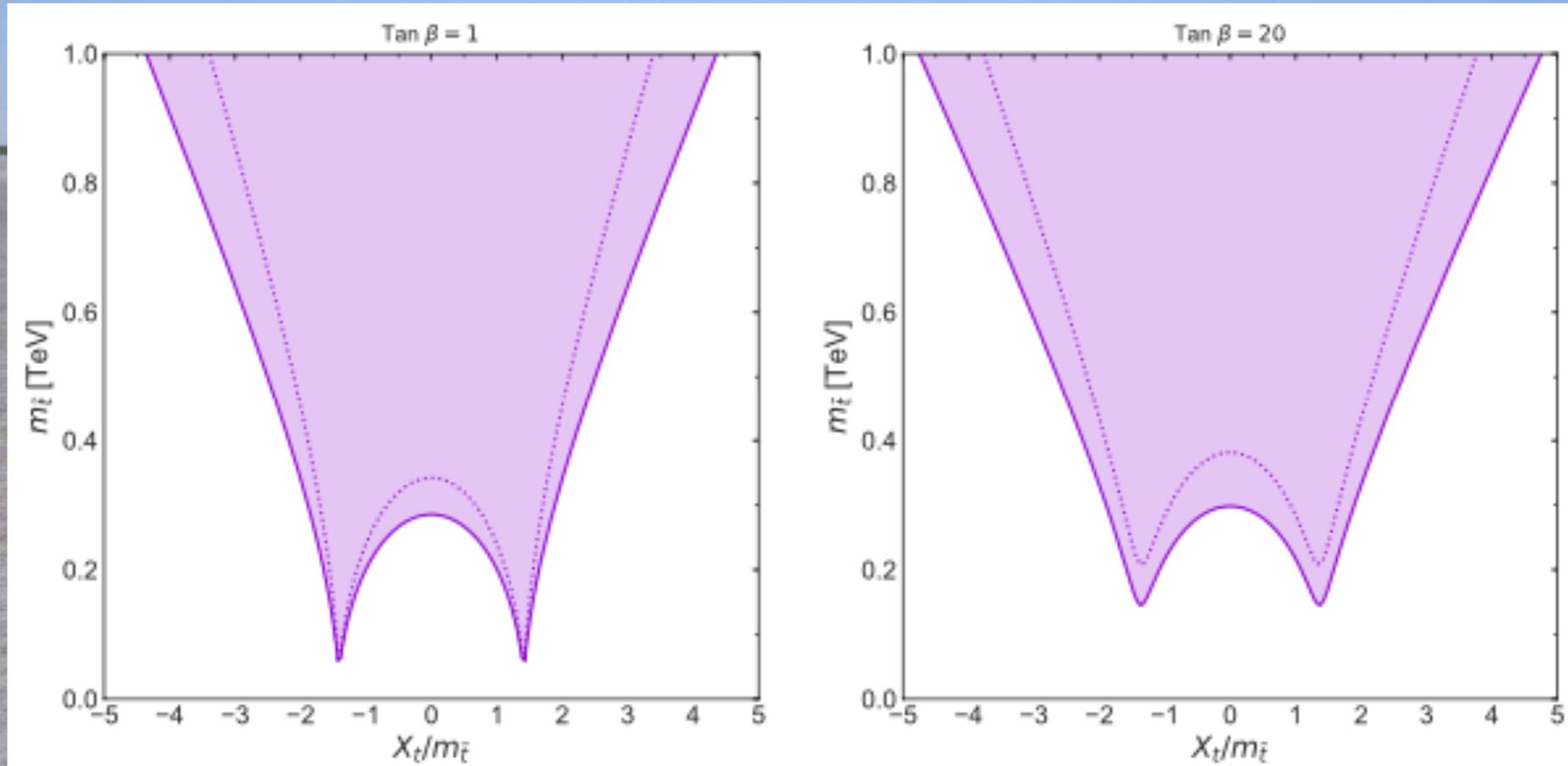


Constraints on Single-Field BSM Scenarios

- No significant pulls away from SM
- Any single-field extension of SM must have mass scale > 400 GeV if coupling = 1



SMEFT Constraints on Light Stops

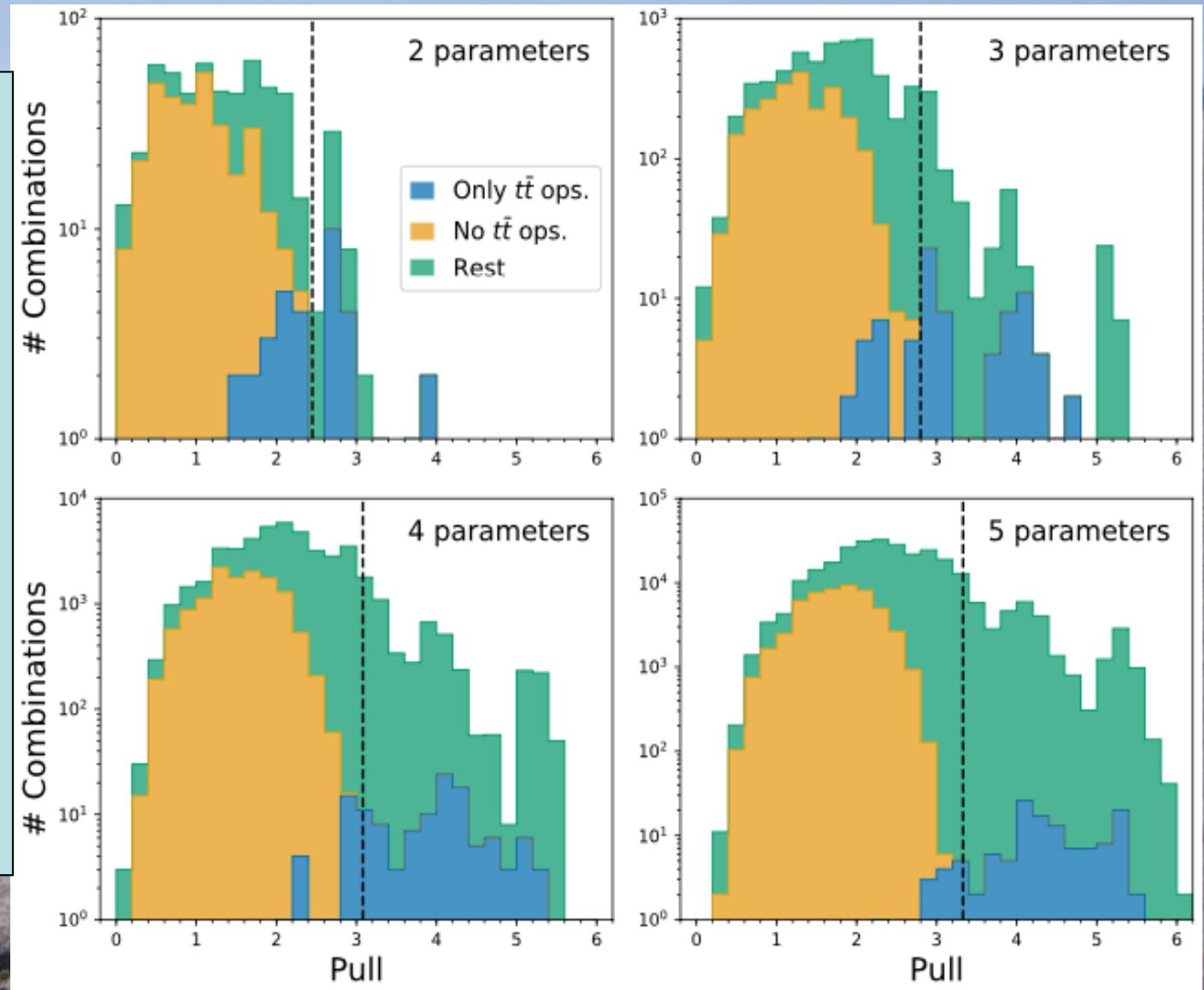


- Stops contribute to 4 SMEFT operators
- Must weigh > 300 GeV, except for mixing parameter $X_t \sim 1.5 m_{\text{stop}}$

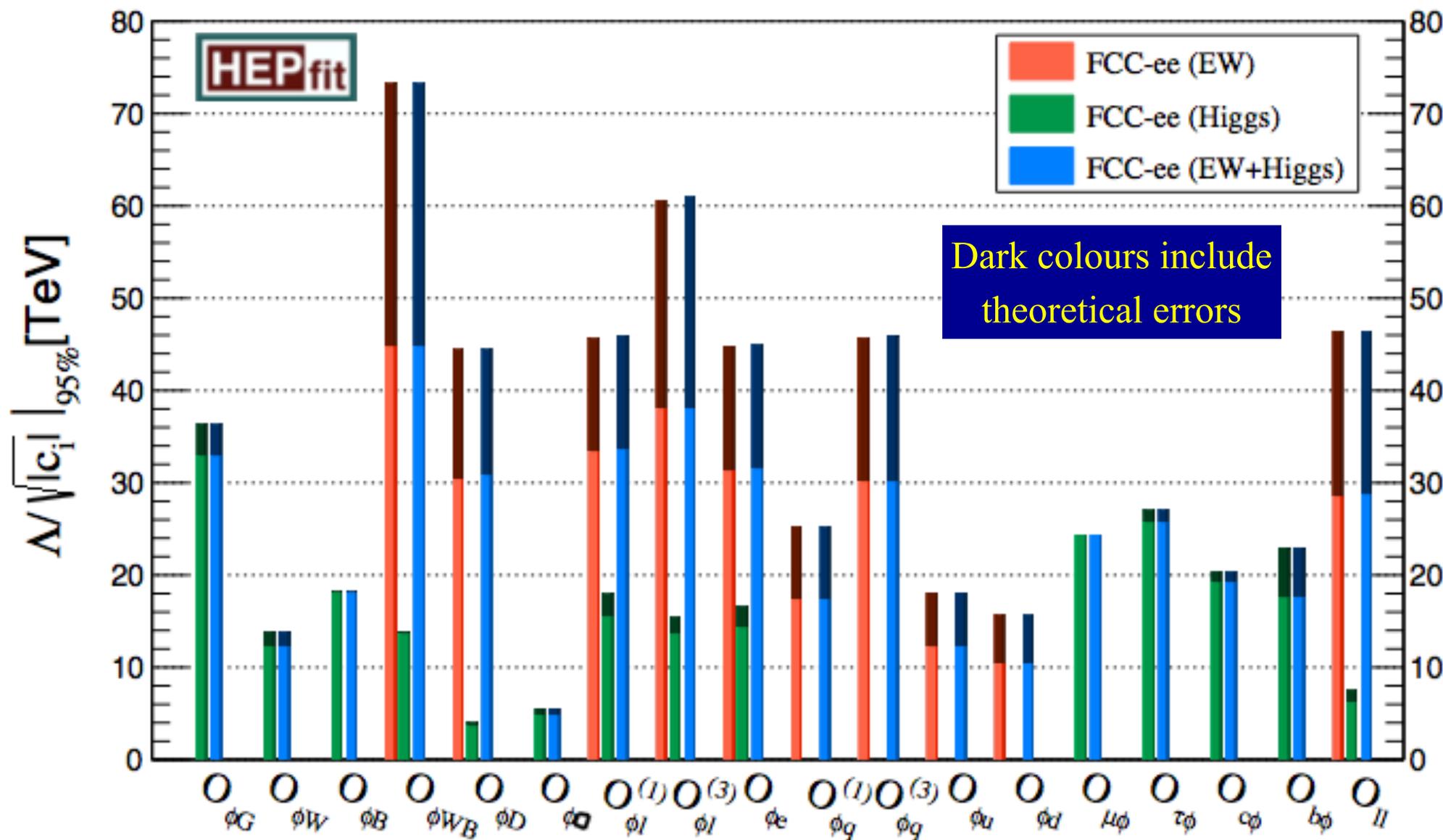
Model-Independent BSM Survey

- Top-less sector fits SM very well
- Top sector does not fit so well
- Overall, pulls not excessive
- No hint of BSM

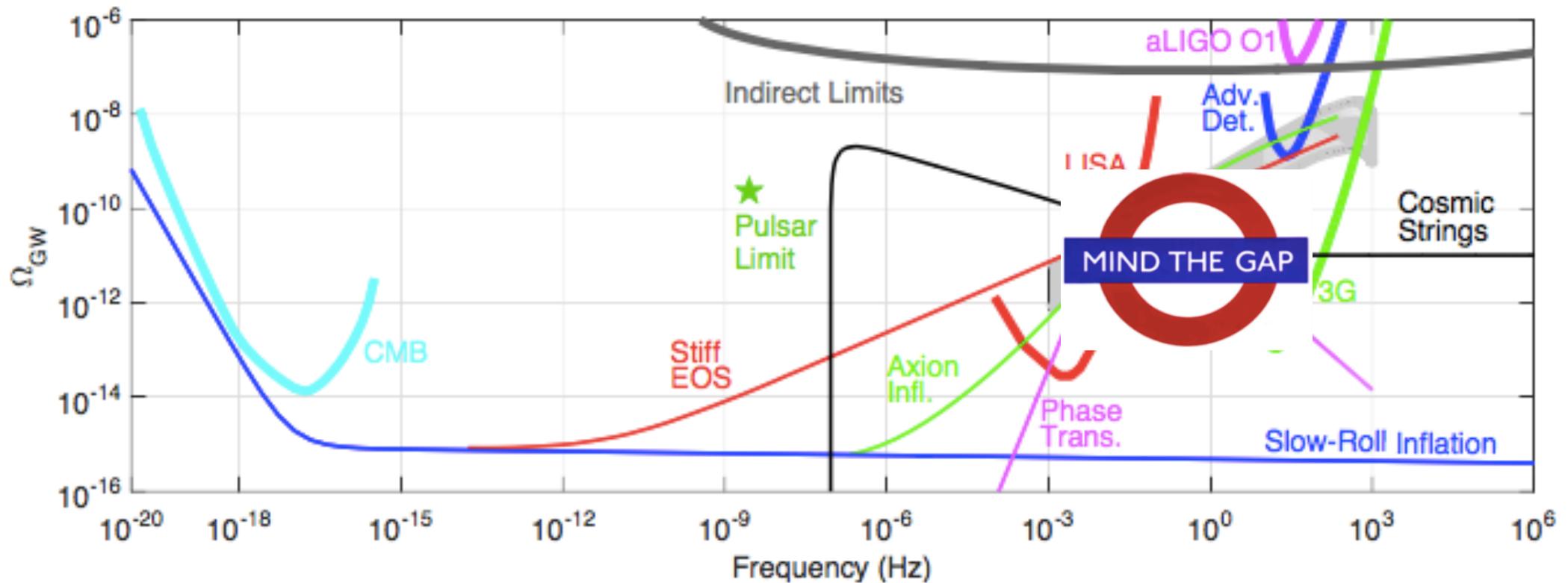
JE, Madigan, Mimasu, Sanz & You,
arXiv:2012.02779



Future EFT Constraints from Higgs and Electroweak Measurements



Gravitational Wave Spectrum

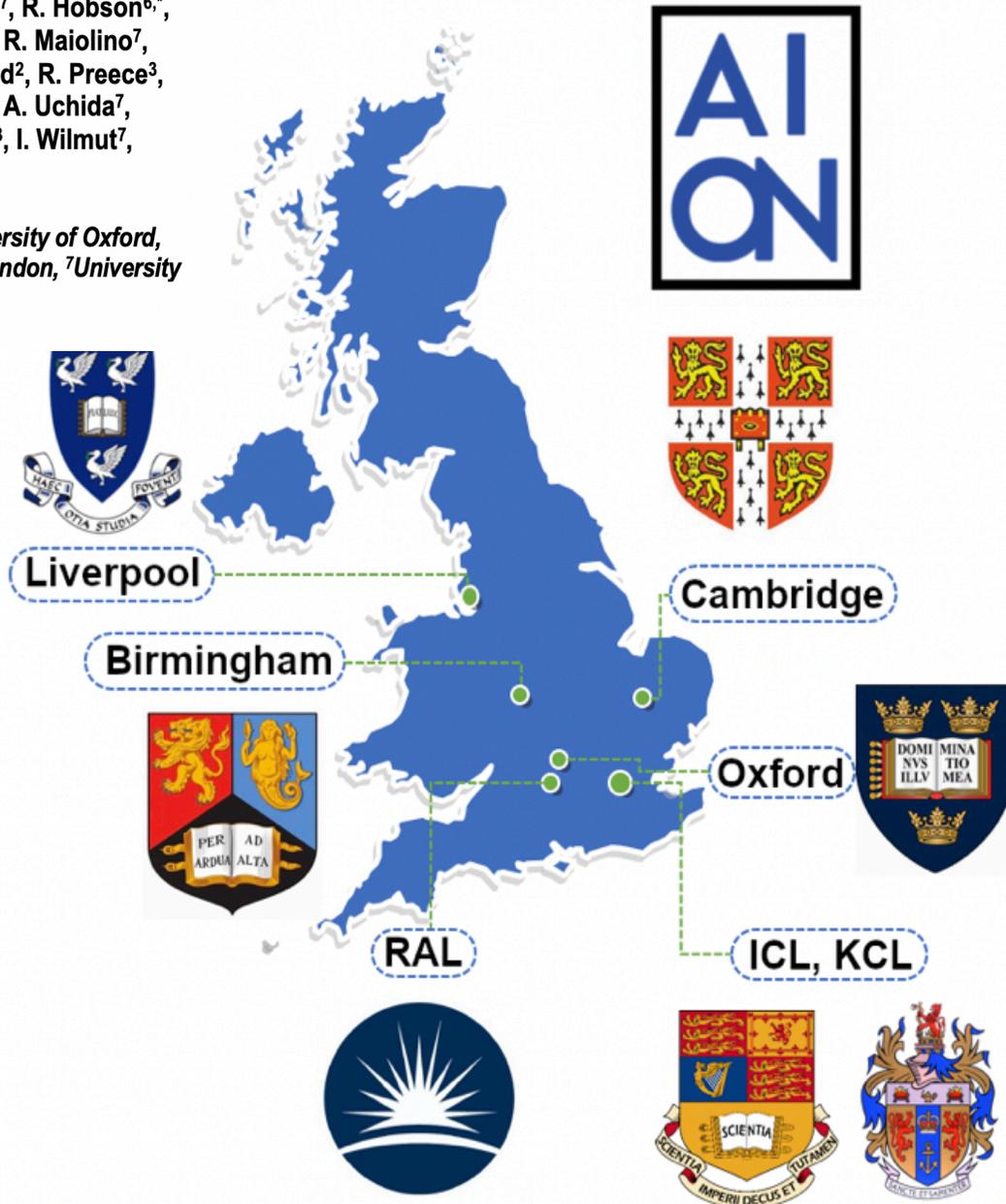
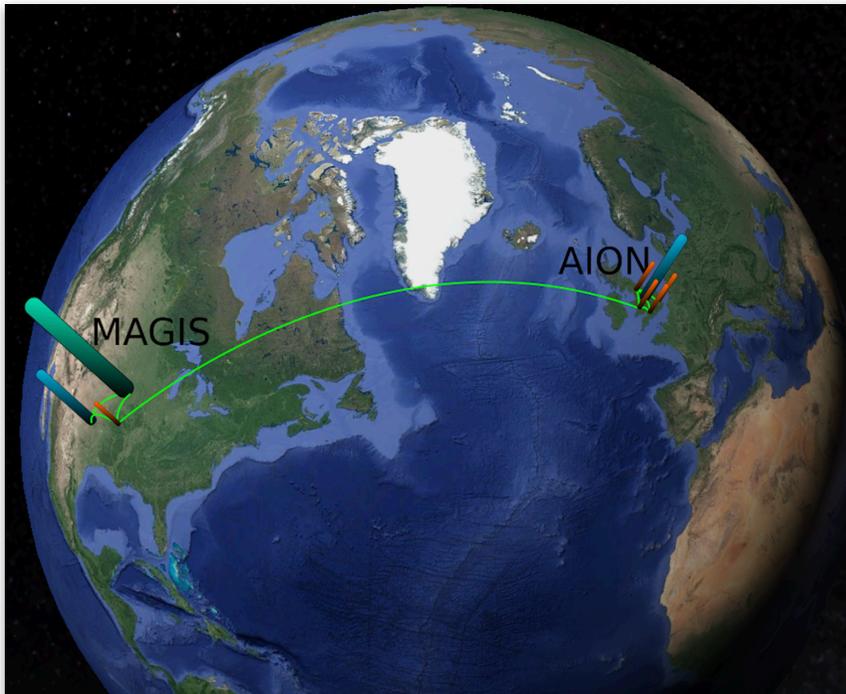


- Gap between ground-based optical interferometers & LISA
 - Formation of supermassive black holes (SMBHs)?
 - Electroweak phase transition? Cosmic strings?
- Gap between LISA & pulsar timing arrays (PTAs)

AION Atom Interferometer Collaboration

L. Badurina¹, S. Balashov², E. Bentine³, D. Blas¹, J. Boehm², K. Bongs⁴,
D. Bortoletto³, T. Bowcock⁵, W. Bowden^{6,*}, C. Brew², O. Buchmueller⁶, J. Coleman⁵,
G. Elertas¹, **J. Ellis^{1,*}**, C. Foot³, V. Gibson⁷, M. Haehnel⁷, T. Harte⁷, R. Hobson^{6,*},
M. Holynski¹, A. Khazov², M. Langlois⁴, S. Lellouch⁴, Y.H. Lien⁴, R. Maiolino⁷,
P. Majewski², S. Malik⁶, J. March-Russell³, C. McCabe¹, D. Newbold², R. Preece³,
B. Sauer⁶, U. Schneider⁷, I. Shipsey³, Y. Singh⁴, M. Tarbutt⁶, M. A. Uchida⁷,
T. V-Salazar², M. van der Grinten², J. Vosseveld⁴, D. Weatherill³, I. Wilmot⁷,
J. Zielinska⁶

¹Kings College London, ²STFC Rutherford Appleton Laboratory, ³University of Oxford,
⁴University of Birmingham, ⁵University of Liverpool, ⁶Imperial College London, ⁷University
of Cambridge

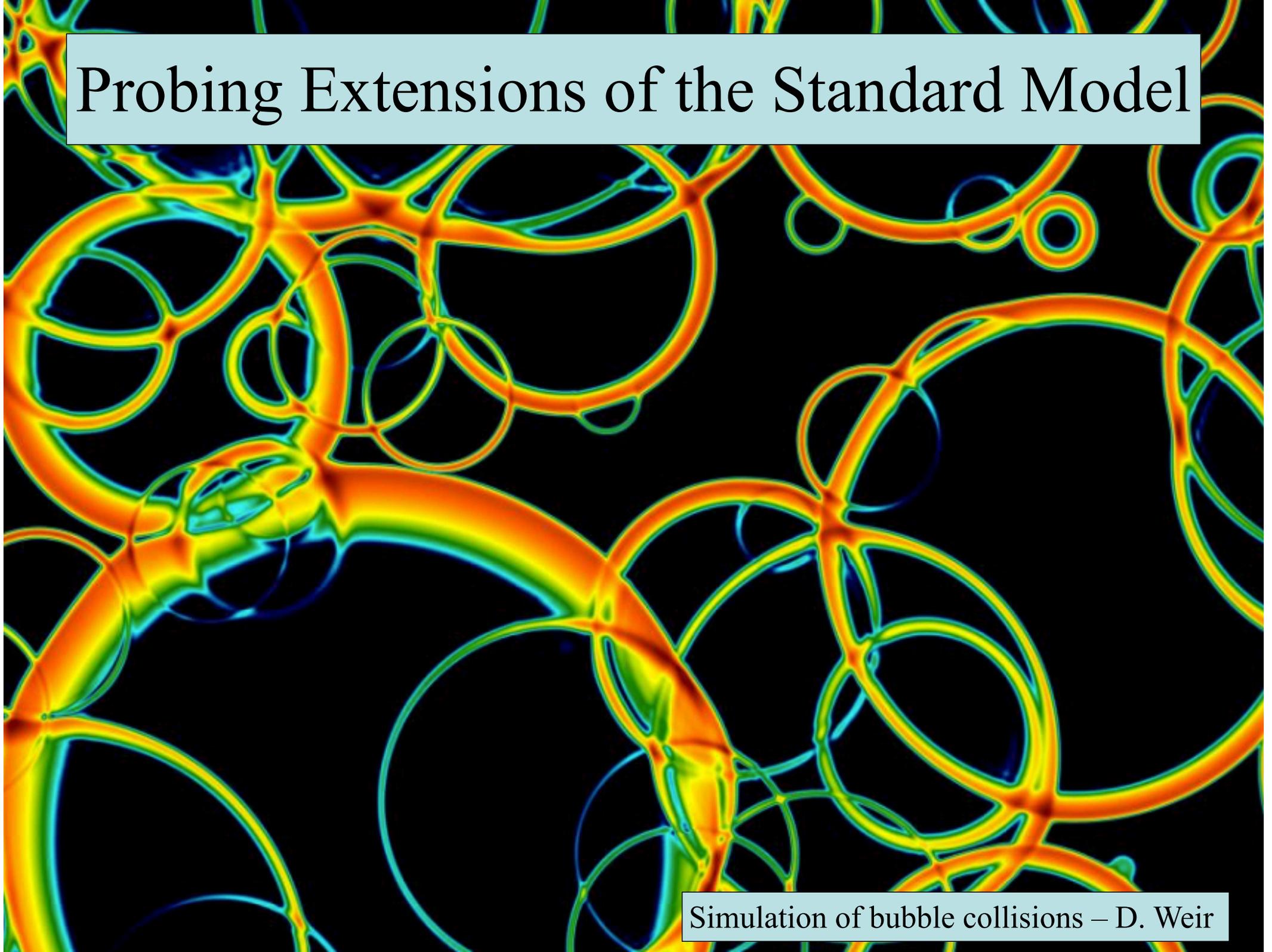


AION – Staged Programme

- AION-10: Stage 1 [year 1 to 3]
 - Strontium labs, 10 m interferometer & studies for 100m Baseline
- AION-100: Stage 2 [year 3 to 6]
 - 100m Construction & Commissioning
- AION-KM: Stage 3 [> year 6]
 - Operating AION-100 and planning for 1 km & beyond
- AEDGE (AION-SPACE): Stage 4 [after AION-KM]
 - Space-based version

Initial funding from UK STFC

Probing Extensions of the Standard Model



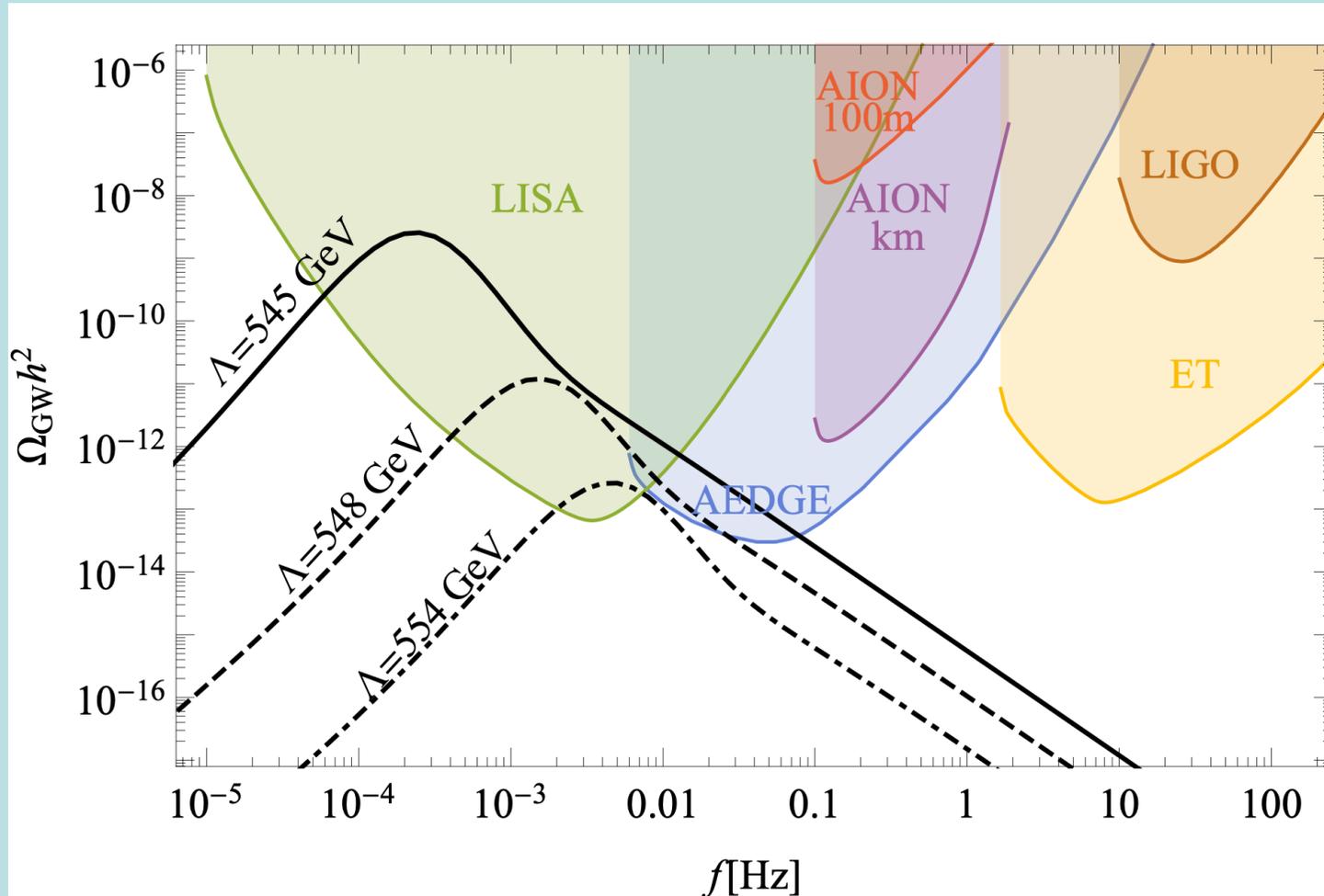
Simulation of bubble collisions – D. Weir

GWs from First-Order Phase Transition

- Transition by percolation of bubbles of new vacuum
- Bubbles grow and collide
- Possible sources of GWs:
 - Bubble collisions
 - Turbulence and sound waves in plasma
- Models studied:
 - Standard Model + H^6/Λ^2 interaction
 - Standard Model + $U(1)_{B-L}$ Z'
- These also have prospective collider signatures

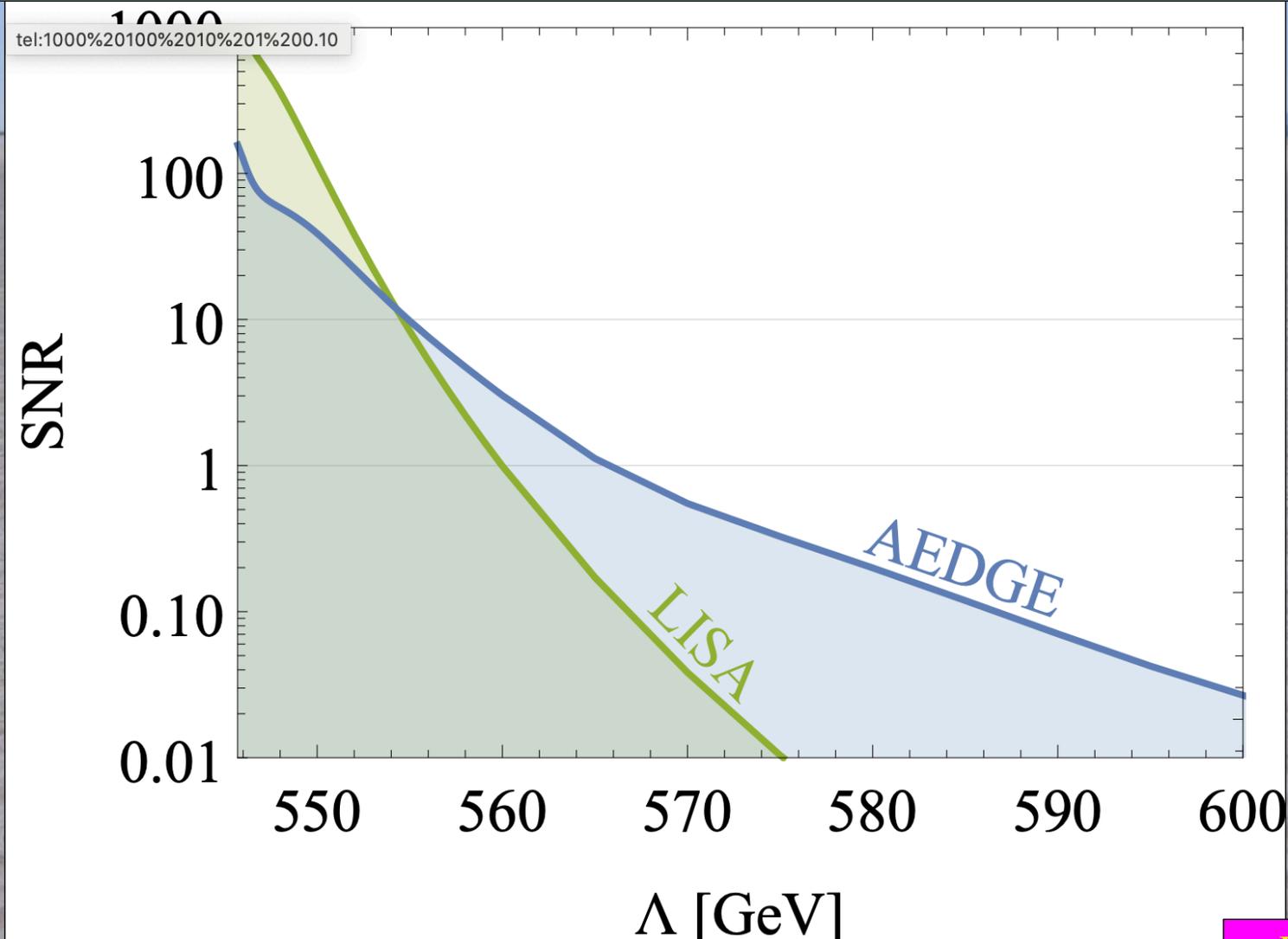
GW Signal in H^6 Model

- Strongest signal for which percolation is assured



- AEDGE and LISA SNR = 8 sensitivities very similar

Gravitational Wave Sensitivity to Scale of H^6 Interaction

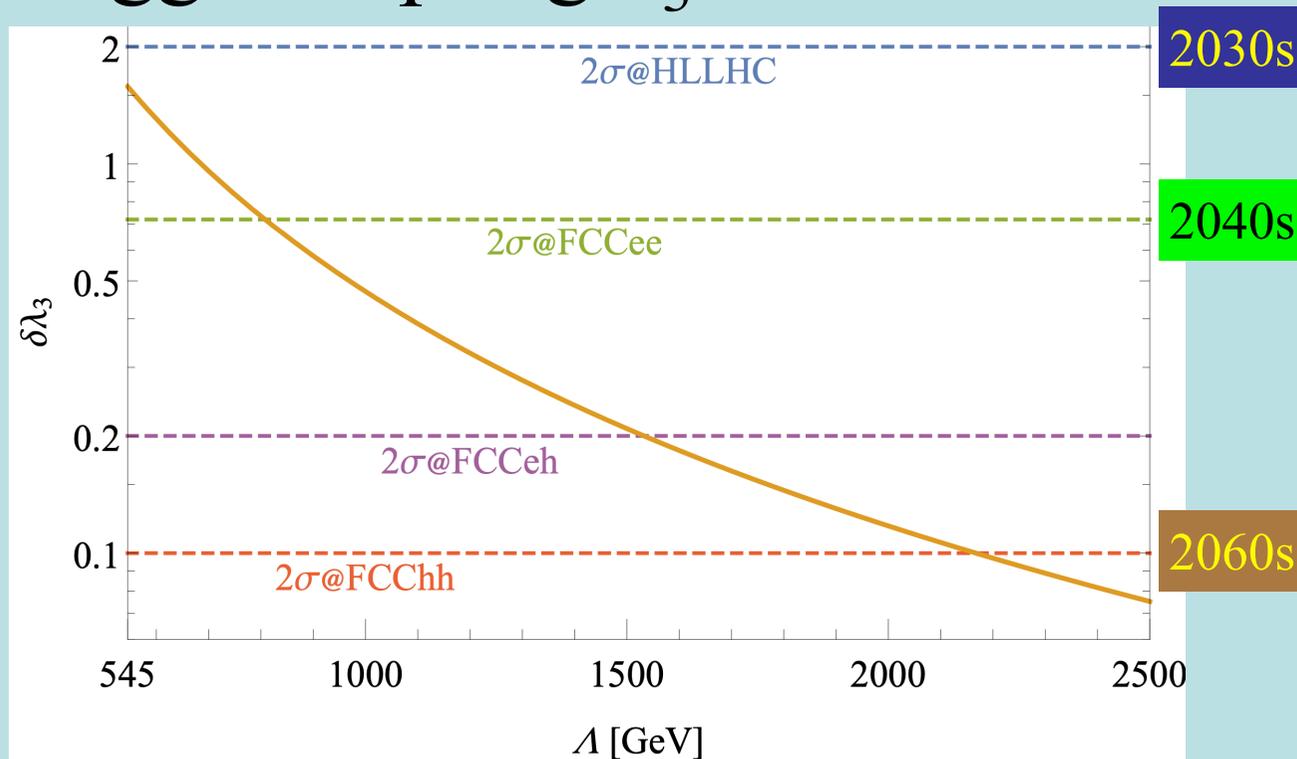


Gravitational wave sensitivity to Λ

Updated from
JE, Lewicki & No,
arXiv:1809.08242

Modification of Triple-H Coupling

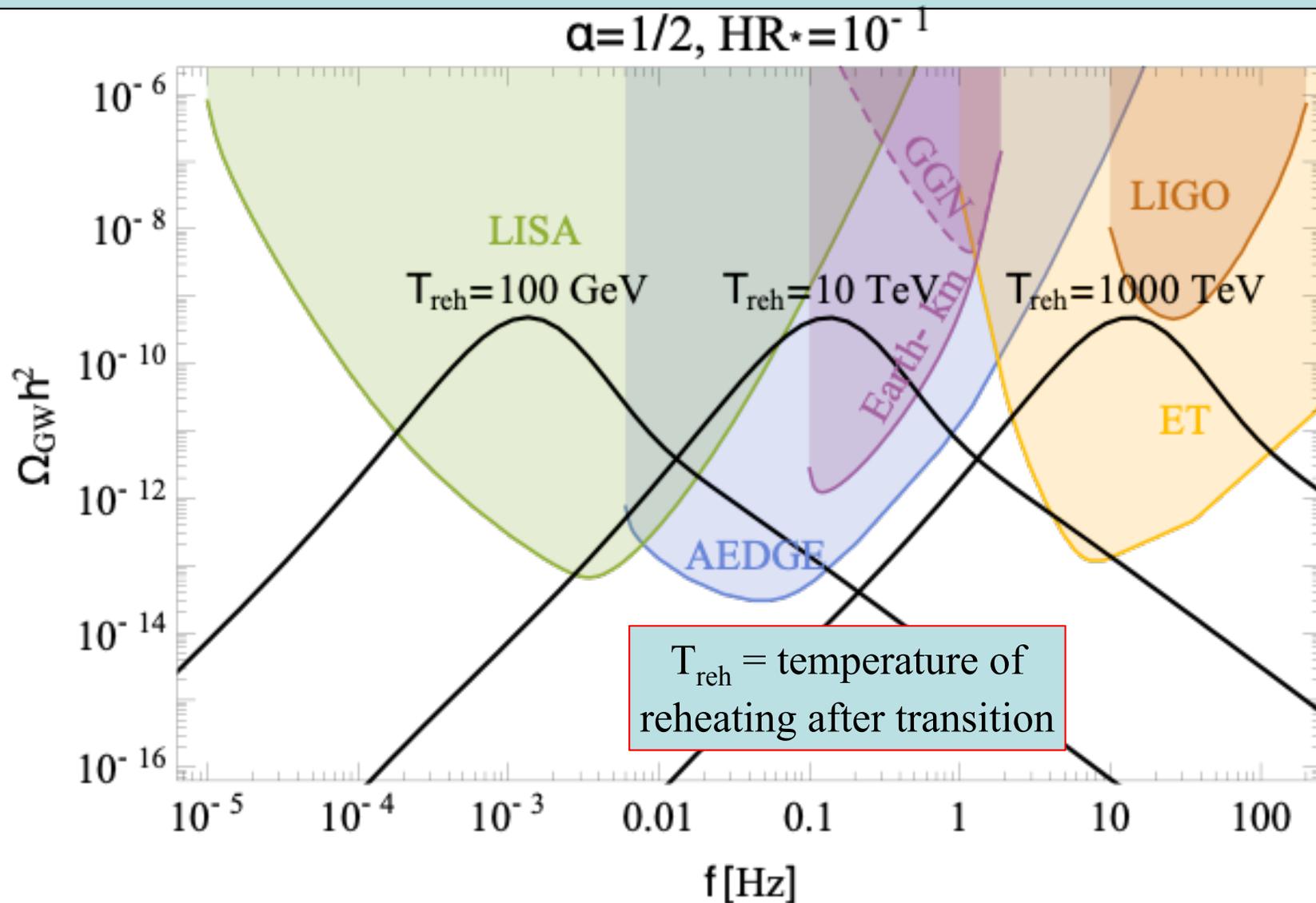
- Current LHC data insensitive to H^6/Λ^2 coupling
- Future collider sensitivity via modification of triple-Higgs coupling λ_3



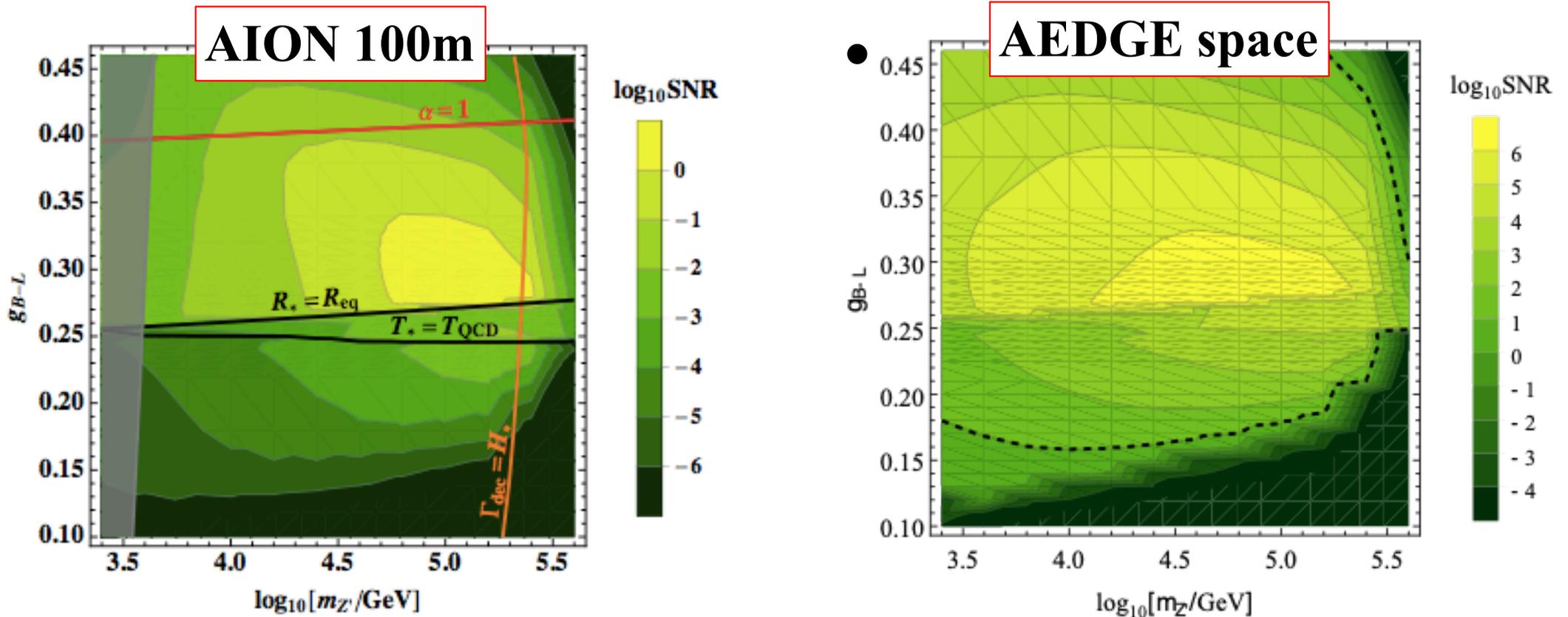
No collider sensitivity now, will eventually be $>$ gravitational waves

Updated from JE, Lewicki & No, arXiv:1809.08242

Gravitational Waves from $U(1)_{B-L}$ Phase Transition



AION GW SNR in Z' Model



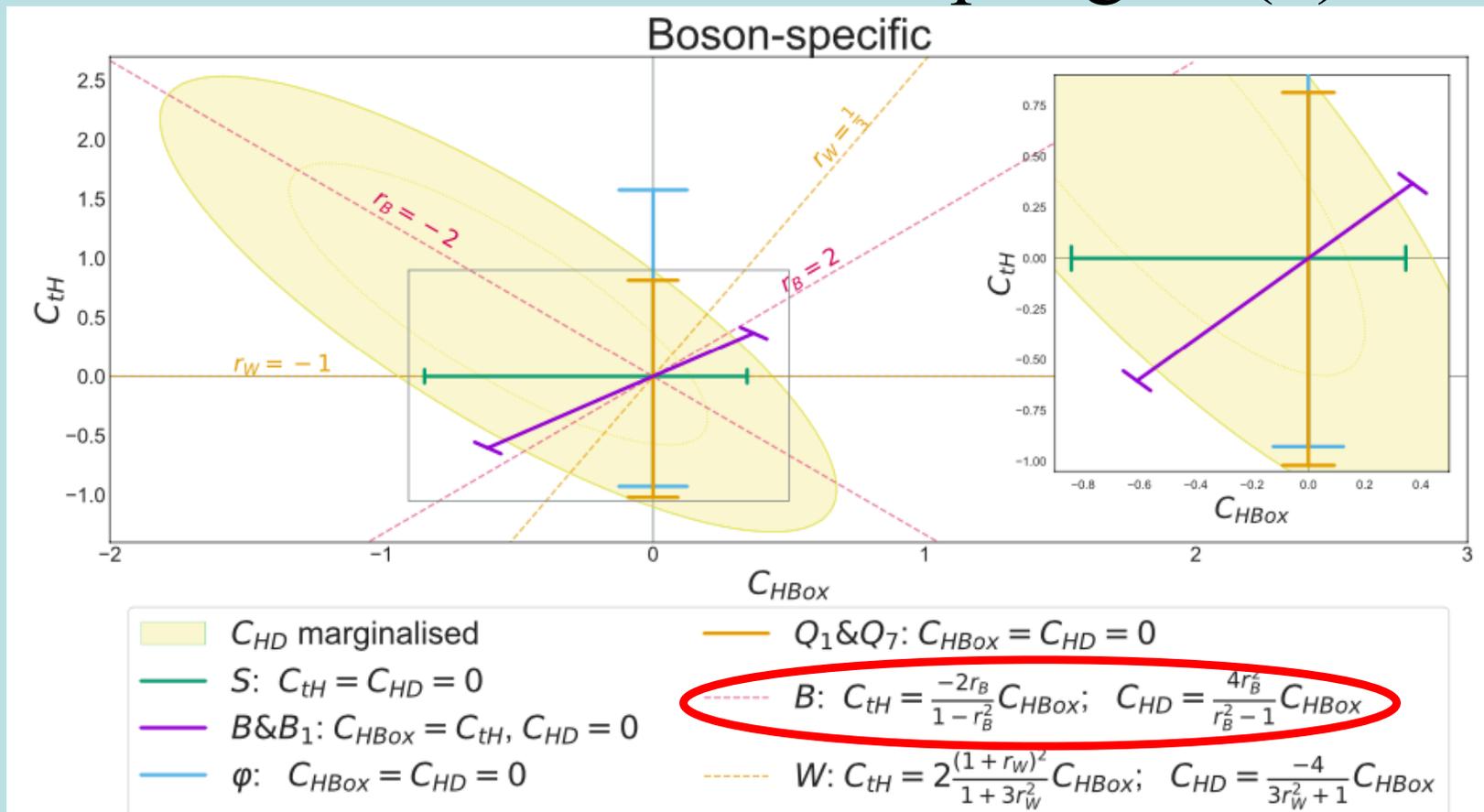
Discovery of GW possible with AION 1km
Mass reach beyond LHC, FCC, SppC

Above red line: transition before vacuum energy dominates
 Right of orange line: period of matter domination

JE, Lewicki, No & Vaskonen, arXiv:1903.09642

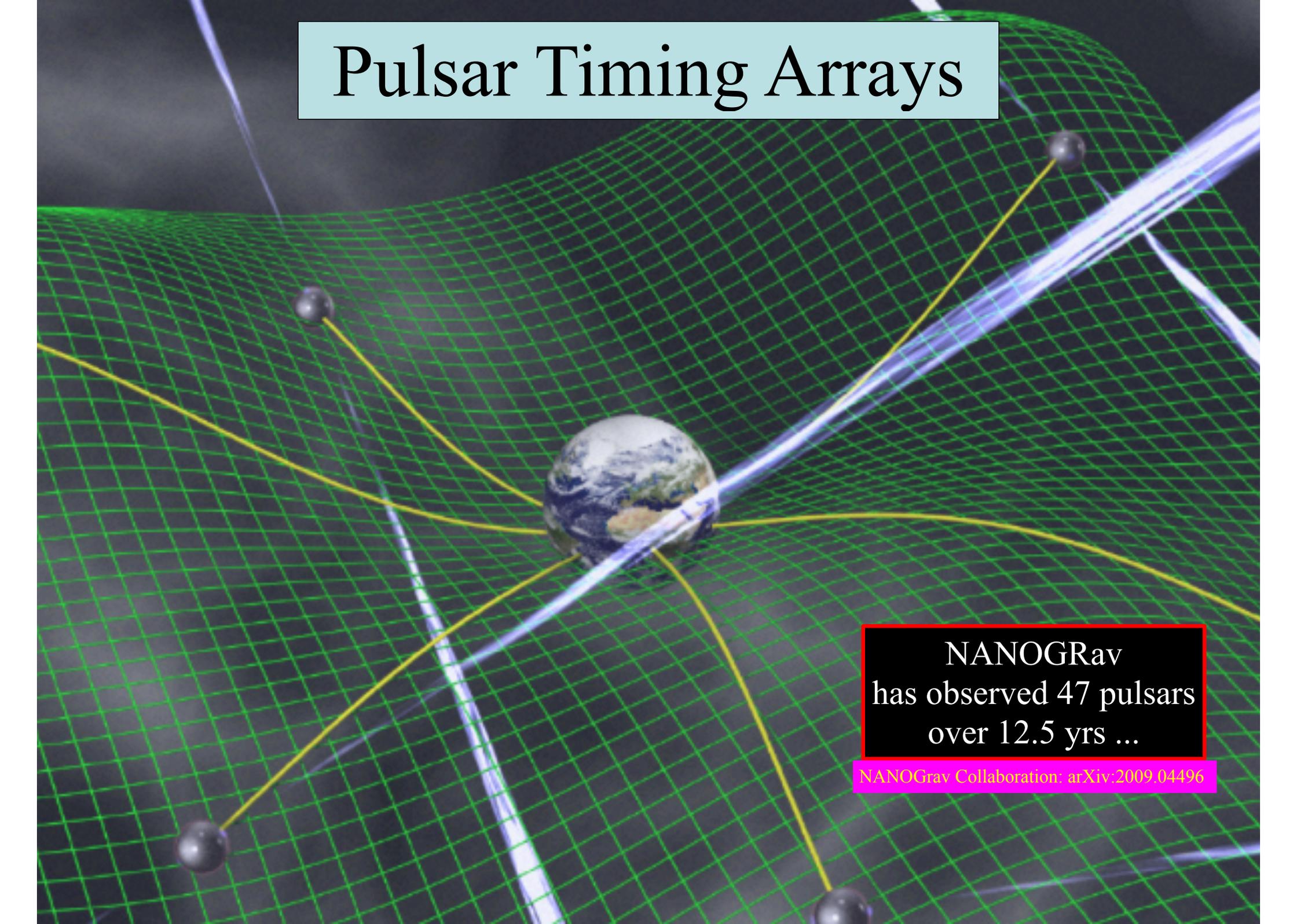
Collider Sensitivities to Z' Models

- Direct limit > 3.5 TeV
- Indirect limit > 1 TeV for couplings $O(1)$



Collider sensitivity will be $<$ gravitational waves

Pulsar Timing Arrays

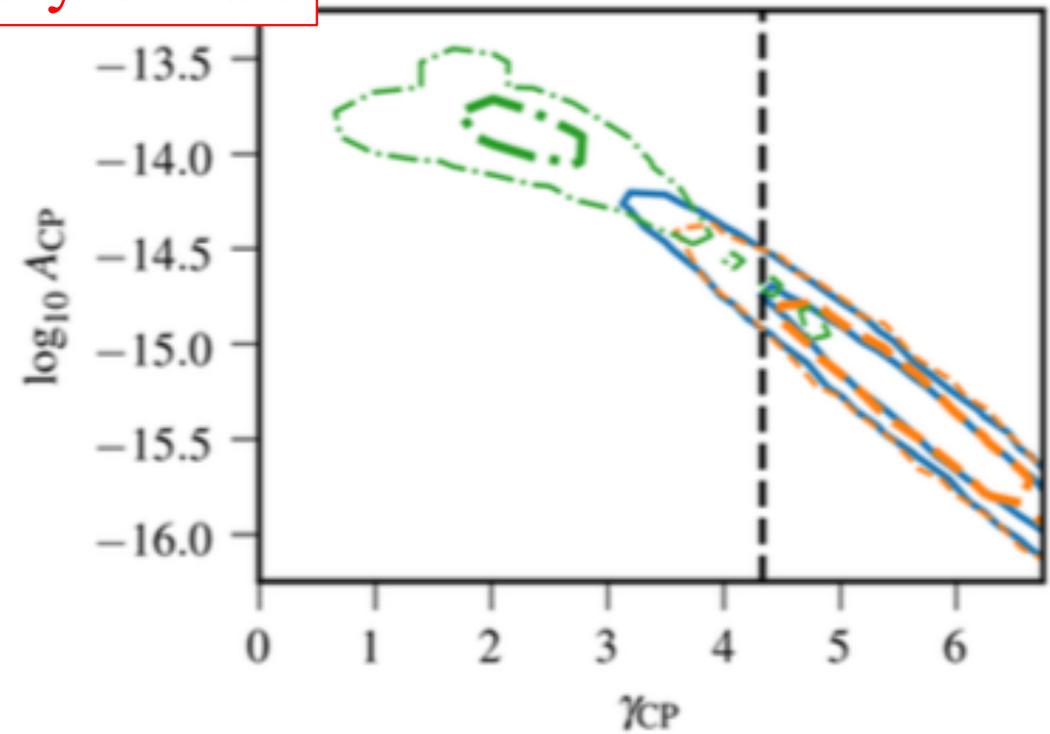
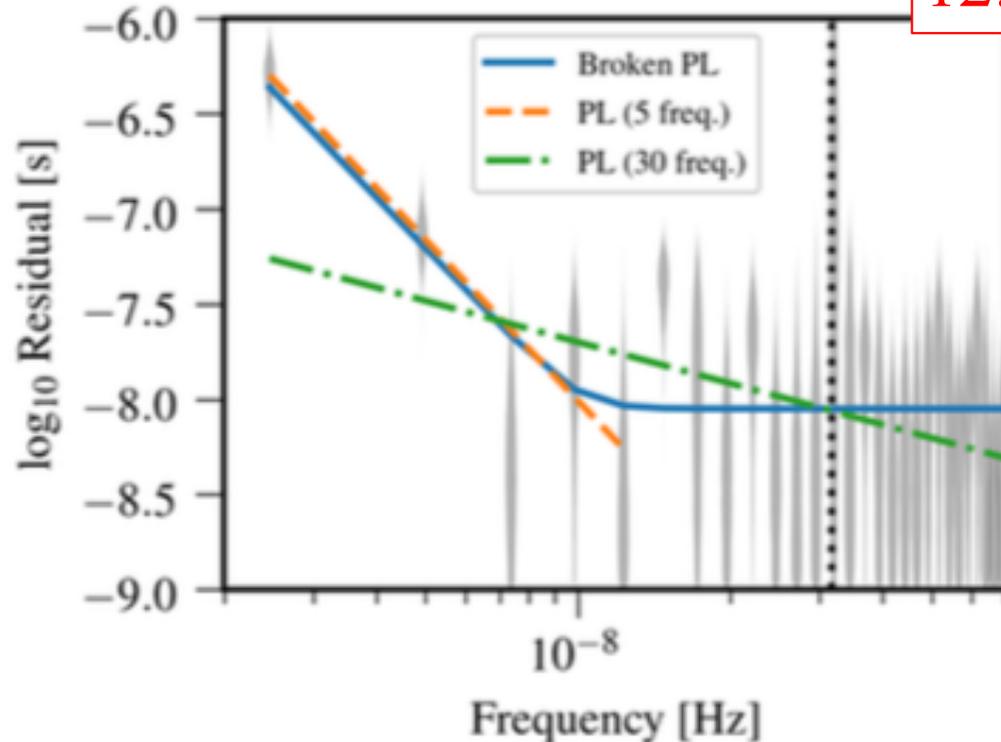


NANOGRav
has observed 47 pulsars
over 12.5 yrs ...

NANOGrav Collaboration: [arXiv:2009.04496](https://arxiv.org/abs/2009.04496)

Pulsar Timing Data from NANOGrav

12.5-year data

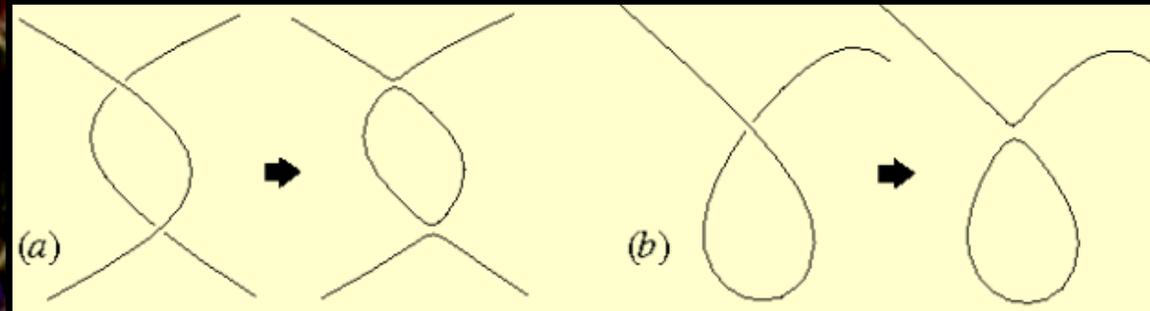


NANOGrav reports
 “strong evidence for a stochastic
 common-spectrum process”
 at frequencies $< 10^{-8}$ Hz
 No dipole or quadrupole
 signal detected

Fits to amplitude of signal
 Focus on simple power law
 Amplitude $A \sim 10^{-15}$
 Slope $\gamma \sim 5$
 Vertical dashed line: expected
 Default model in models of mergers
 of supermassive BHs

Probing Cosmic Strings

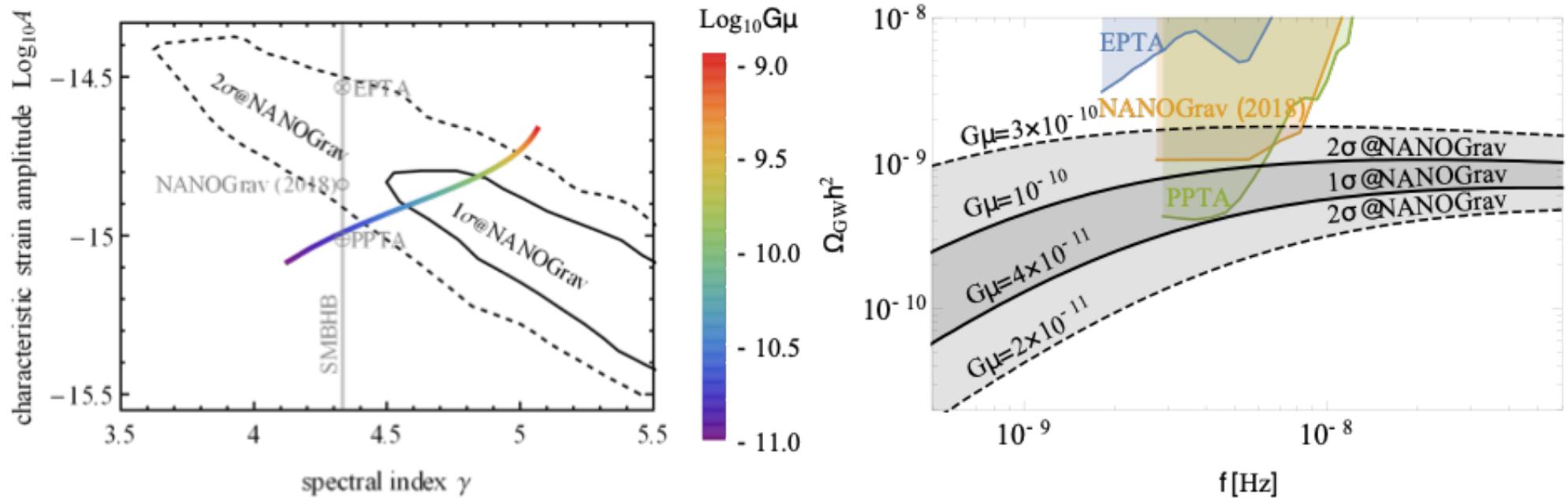
Hint from the NANOGrav pulsar timing array?



GW emission from string loops

Simulation of cosmic string network – Cambridge cosmology group

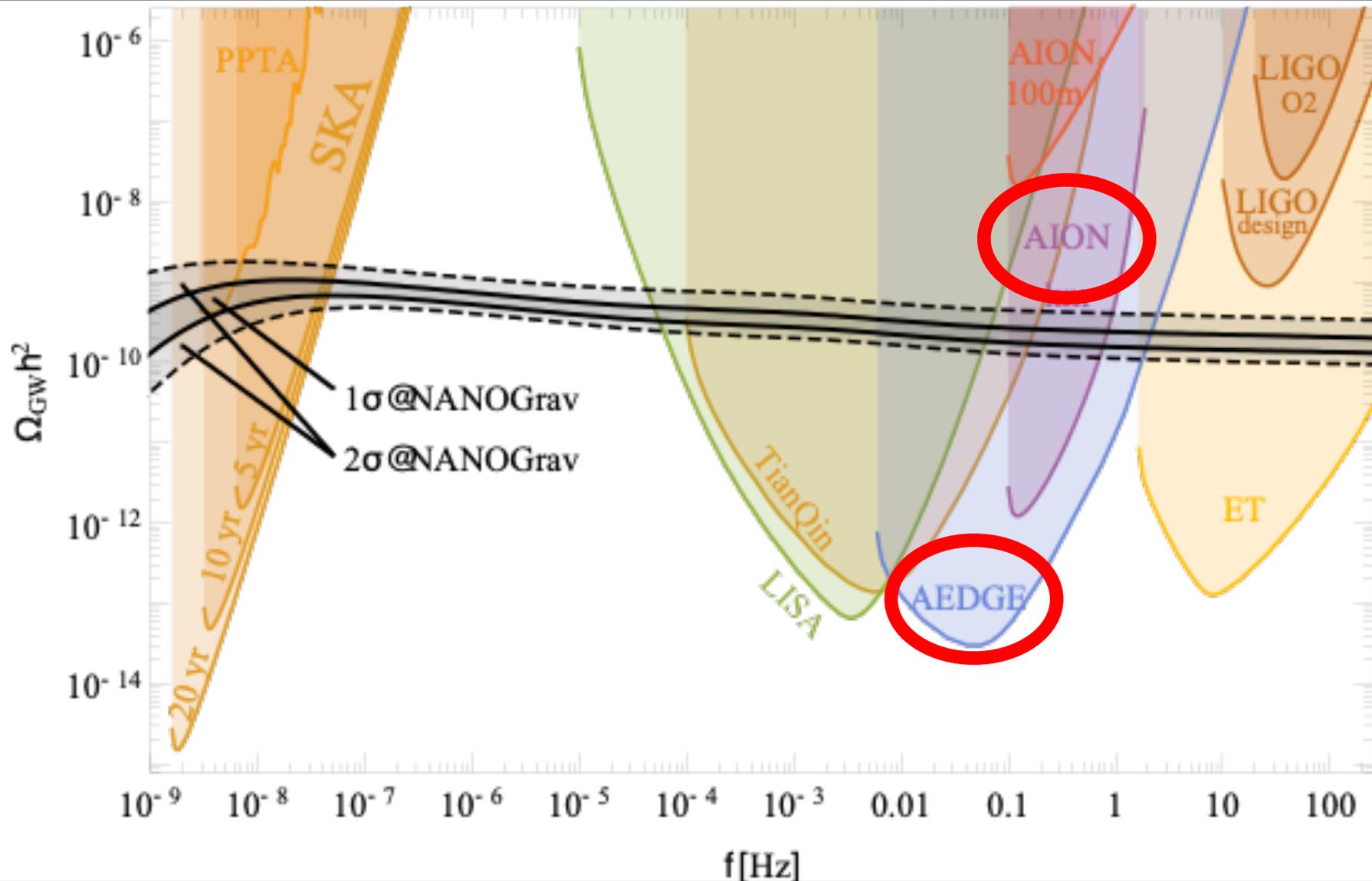
Cosmic String Interpretation of NANOGrav



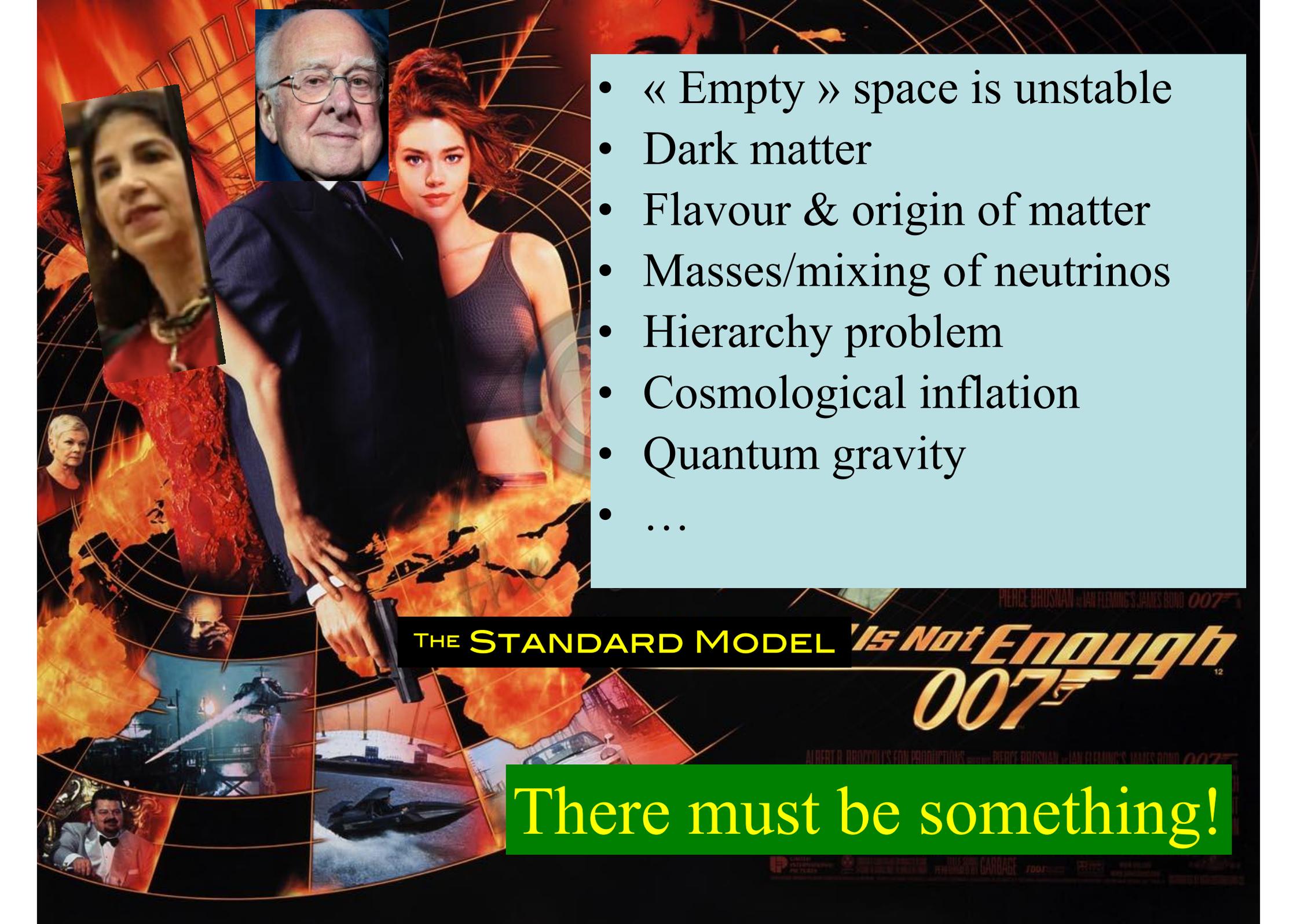
“Rainbow curve”
 is cosmic string prediction as a
 function of the cosmic string tension $G\mu$
 Vertical line is naïve SMBH merger prediction
 Previous PTA upper limits for
 this value of γ

Fits to NANOGrav signal
 at 1σ (68%), 2σ (95%) levels
 Compared to previous
 upper limits
 (previous NANOGrav superseded)

Cosmic String Interpretation of NANOGrav



Cosmic string prediction can be tested in several upcoming experiments (not LIGO)

- 
- « Empty » space is unstable
 - Dark matter
 - Flavour & origin of matter
 - Masses/mixing of neutrinos
 - Hierarchy problem
 - Cosmological inflation
 - Quantum gravity
 - ...

THE STANDARD MODEL *Is Not Enough*
007[™]

There must be something!