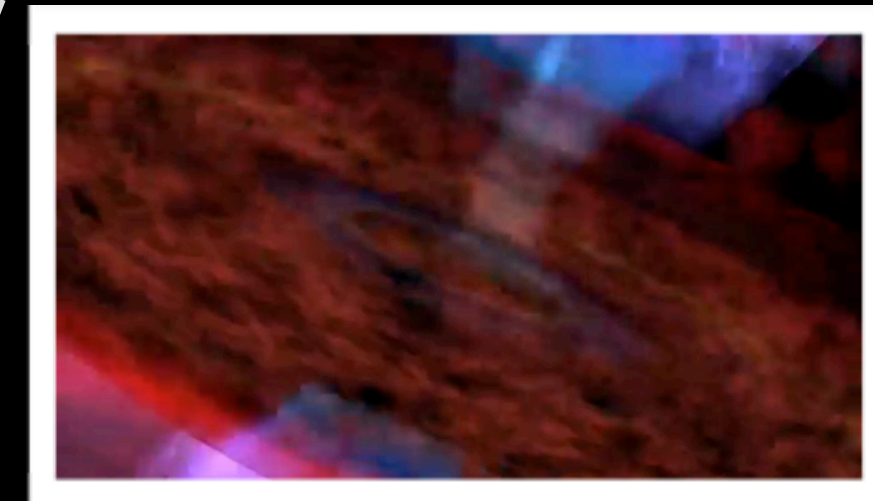


Theoretical Overview of Black Hole Accretion and Jet



a journey to the
horizon scale



Hung-Yi Pu (卜宏毅)

Oct 22nd 2020

NCTS Workshop: Multiscale Feedback on Galaxy Evolution



國立臺灣師範大學
NATIONAL TAIWAN NORMAL UNIVERSITY

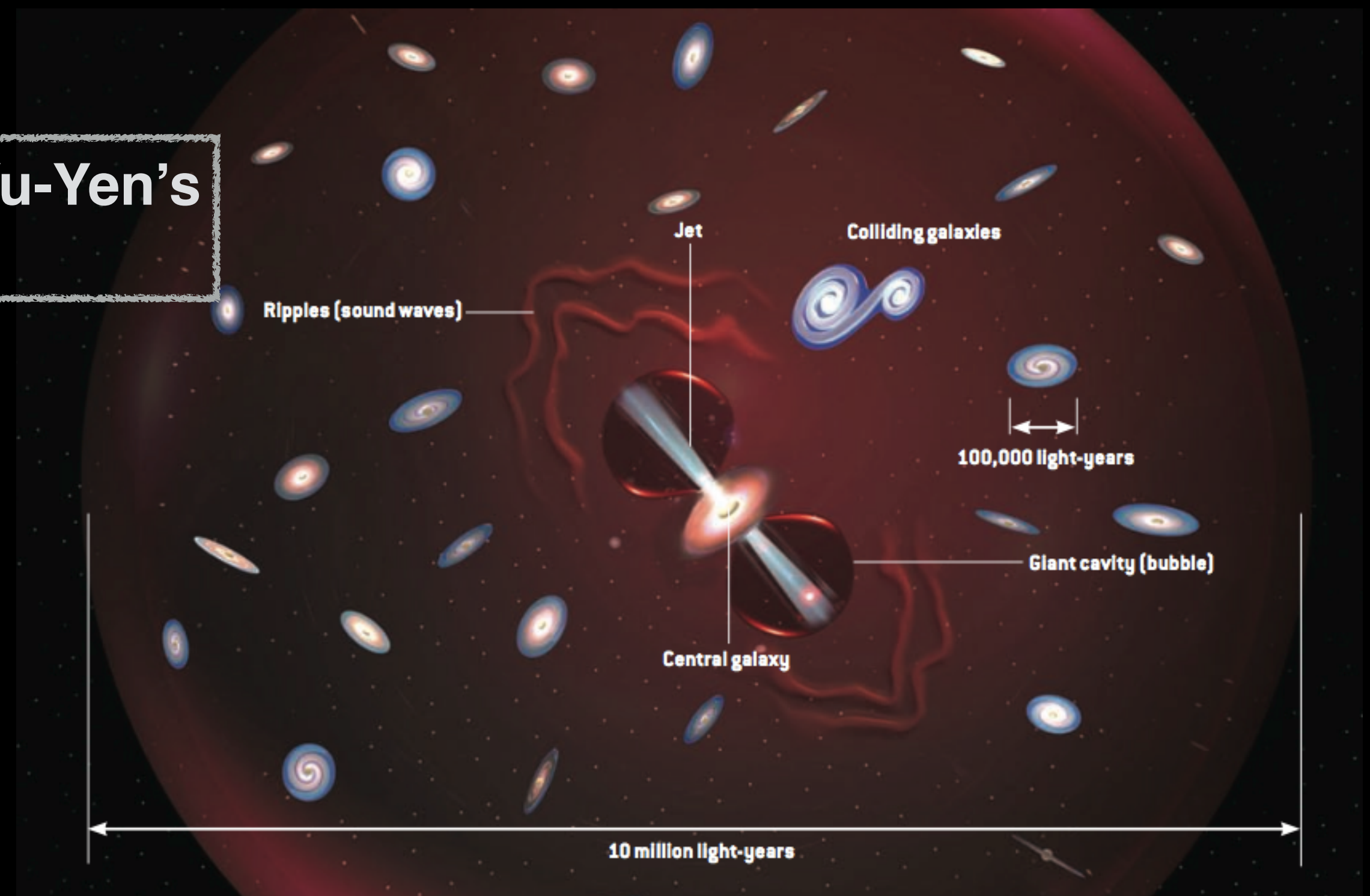
black holes: compact, yet powerful

quasar/radiative mode



Karen's + Yu-Yen's
talk

radio/kinetic mode



But.... how?

outline

- understanding the central engine: black hole (BH)
 - how gravity works in general relativity?
 - BH as spacetime structure
- BH accretion and jet physics:
 - theory
 - (selected) simulation
- final remarks

how gravity works? why spacetime?

strong gravity



weak gravity

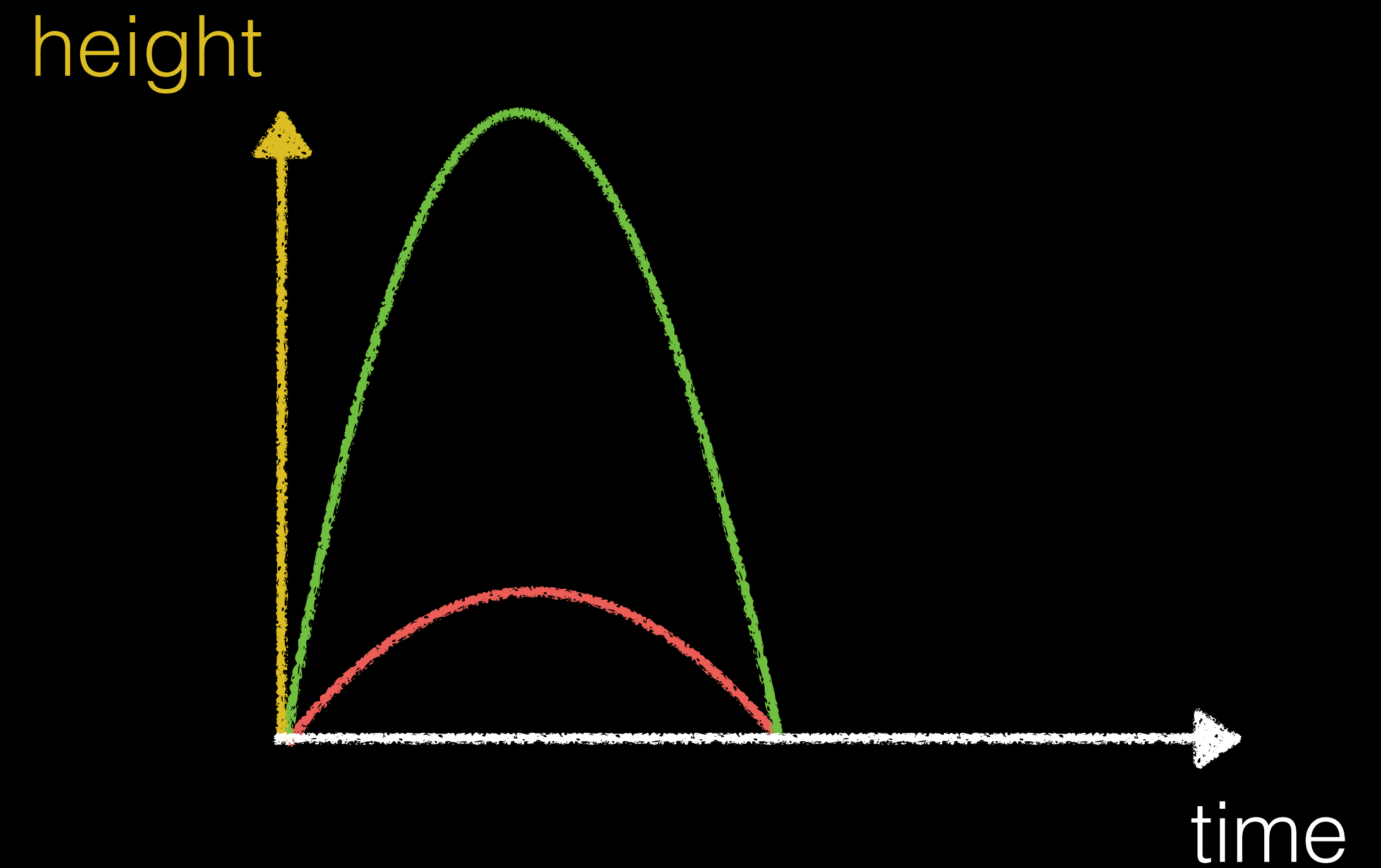


how gravity works? why spacetime?

strong gravity



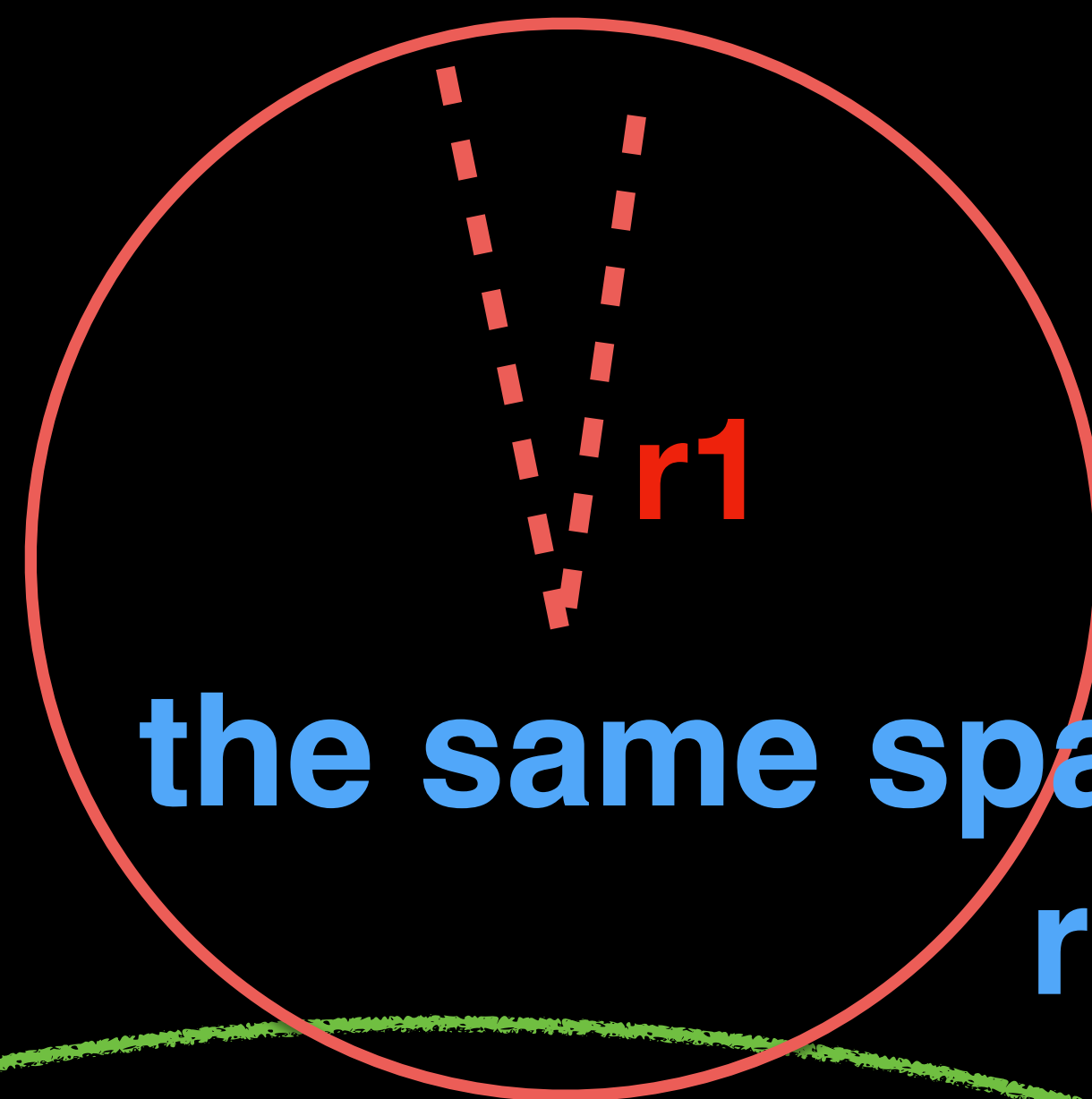
weak gravity



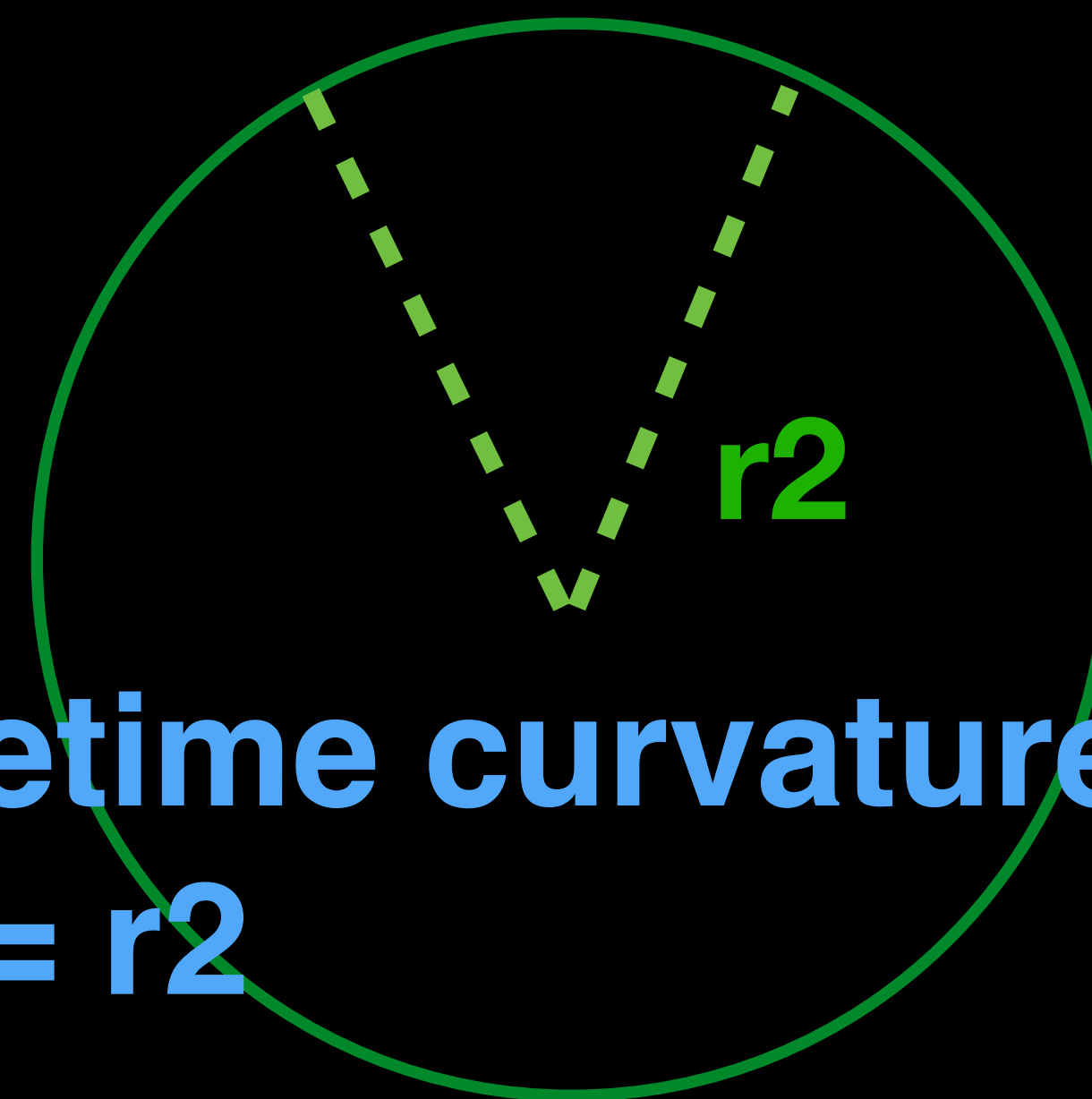
height



the same spacetime curvature
 $r1 = r2$

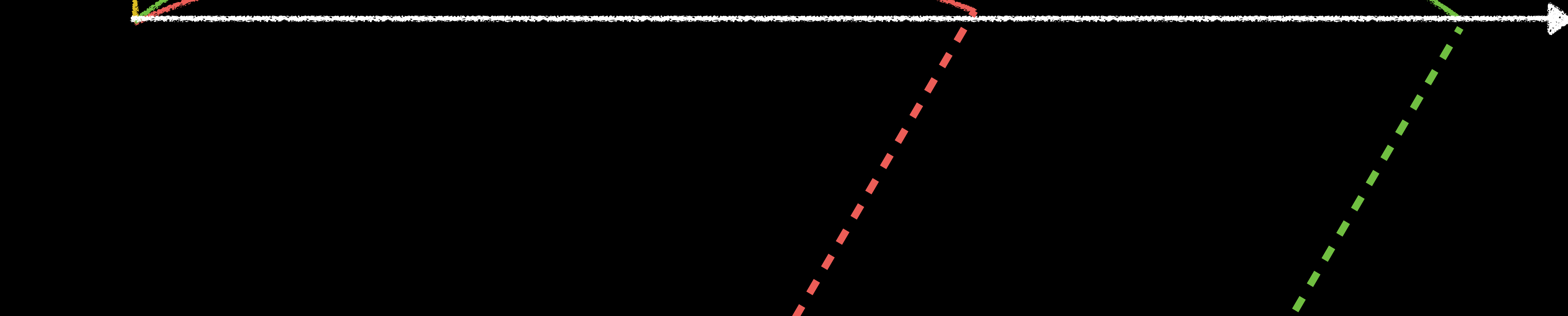


$r1$



$r2$

time x
speed of light



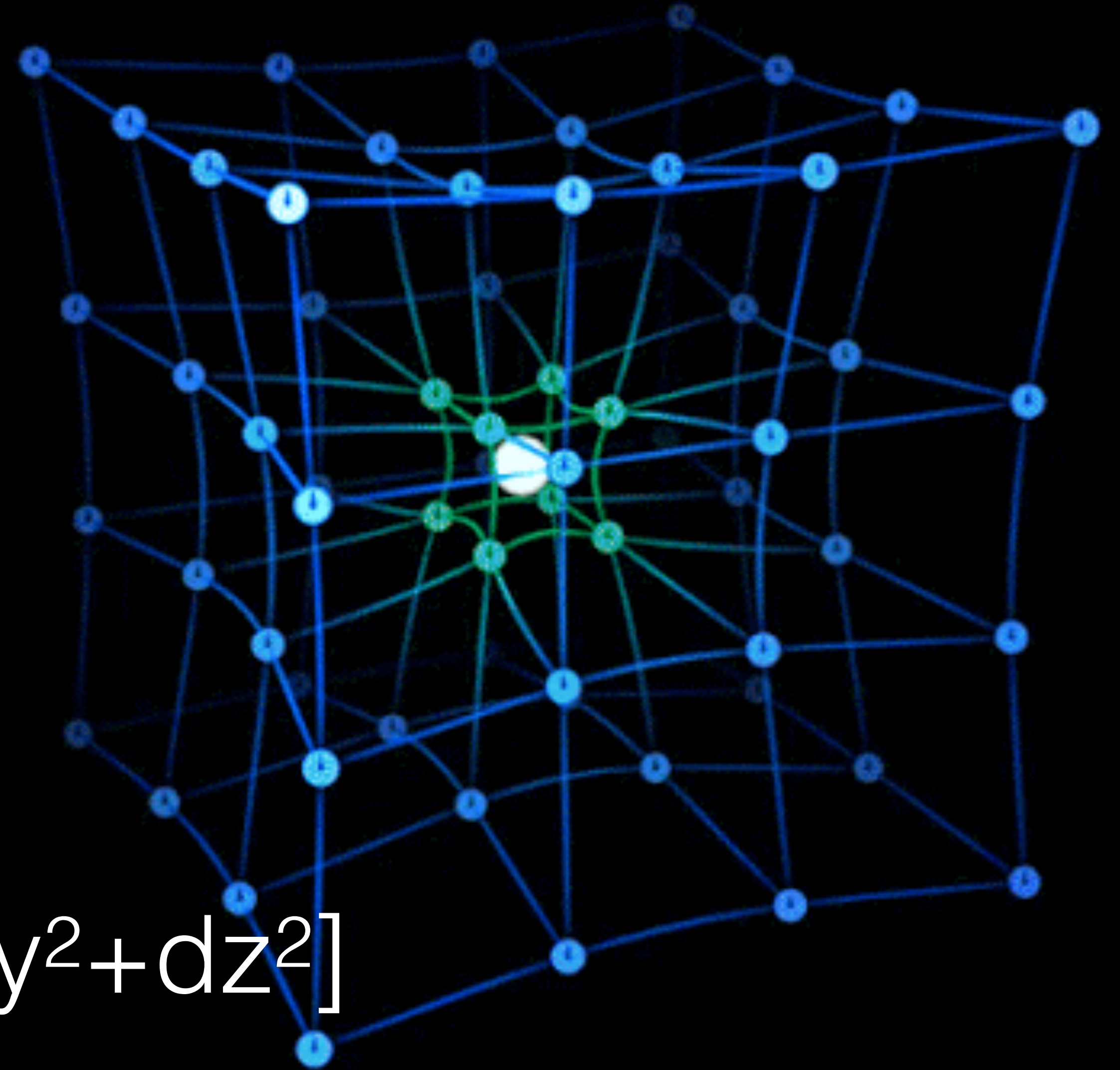
Theory of General Relativity:

gravity
= curved **spacetime**

described as **geometry**

e.g. $ds^2 = -f(r)dt^2 + f'(r)[dx^2 + dy^2 + dz^2]$

(pseudo-Riemannian)



black hole: spacetime structure

Non-rotating BH:

described by **Schwarzschild geometry (1916)**

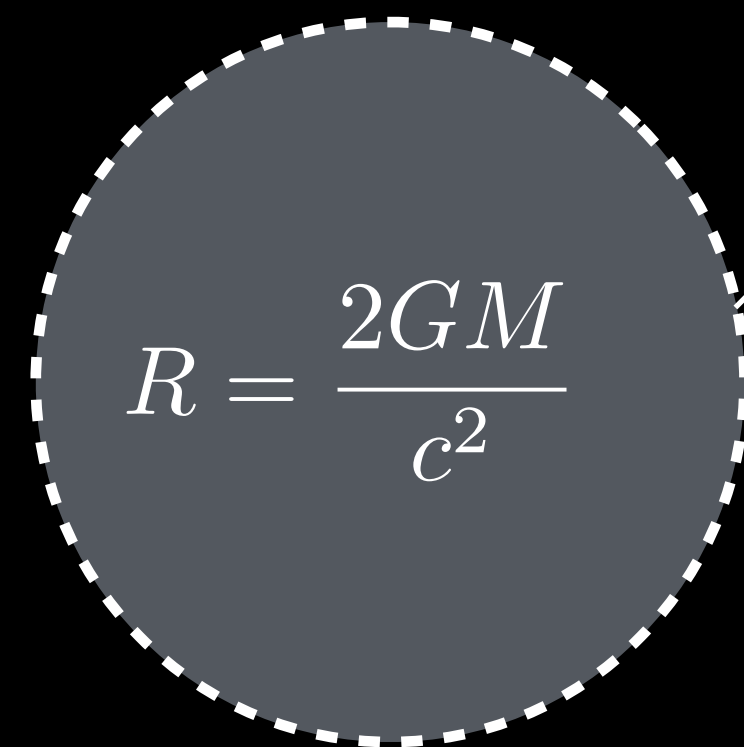


cosmic censorship: "nature forbids naked singularity"

black hole: spacetime structure

Non-rotating BH:

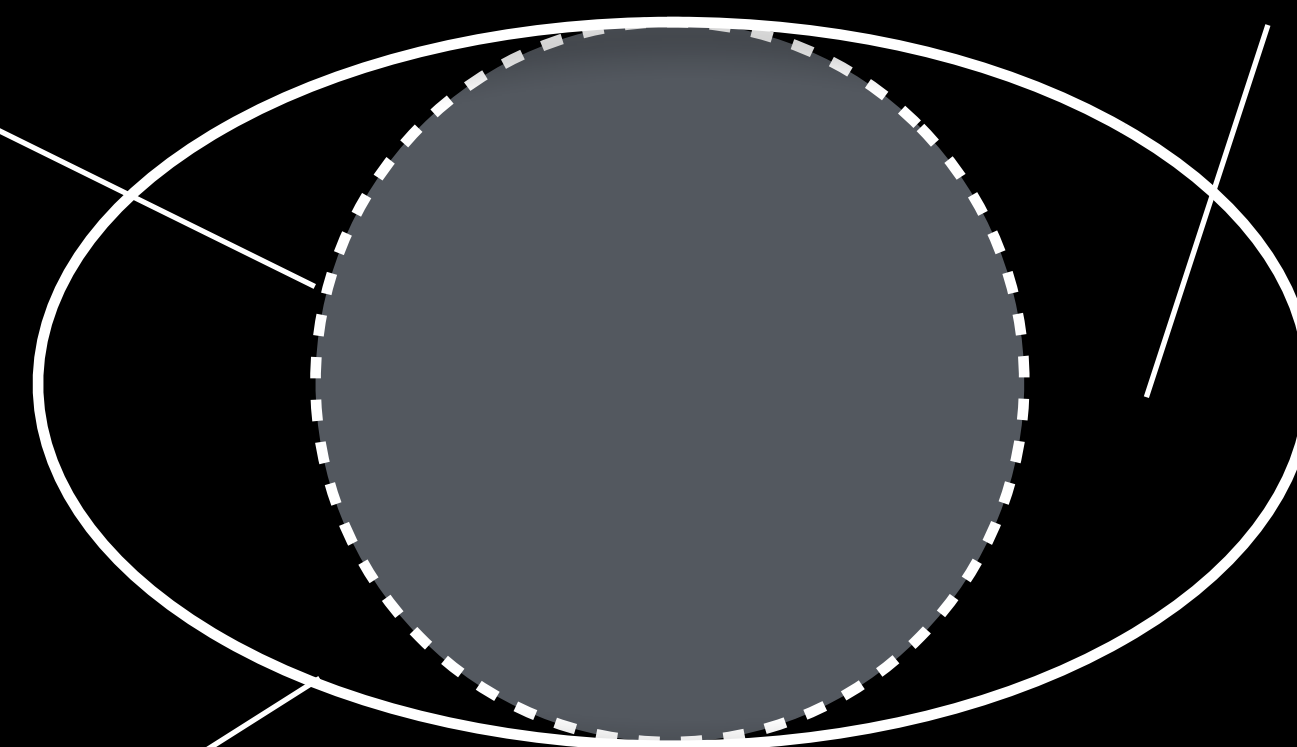
described by **Schwarzschild geometry (1916)**



event horizon

Rotating BH:

described by **Kerr geometry (1963)**

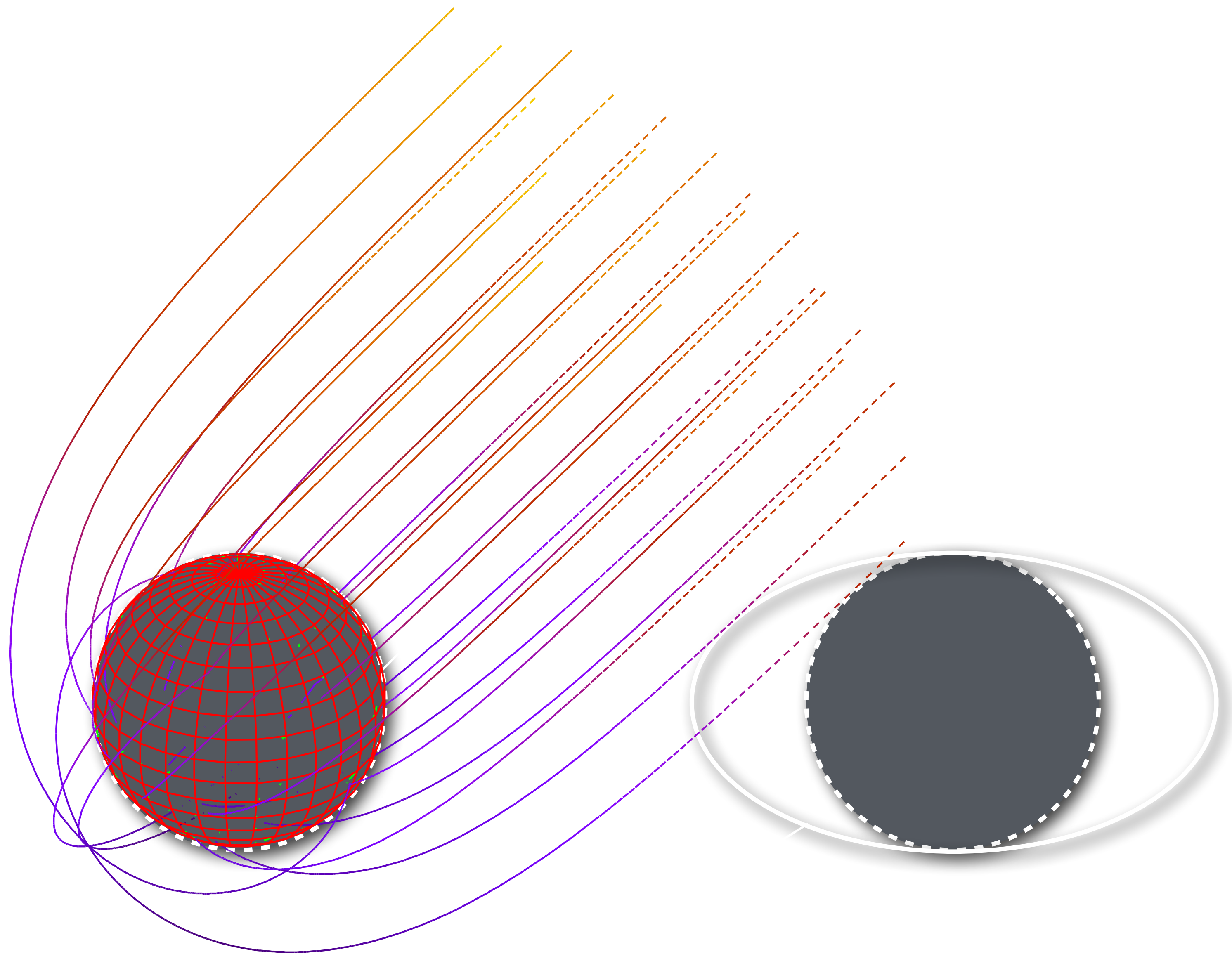


ergosphere

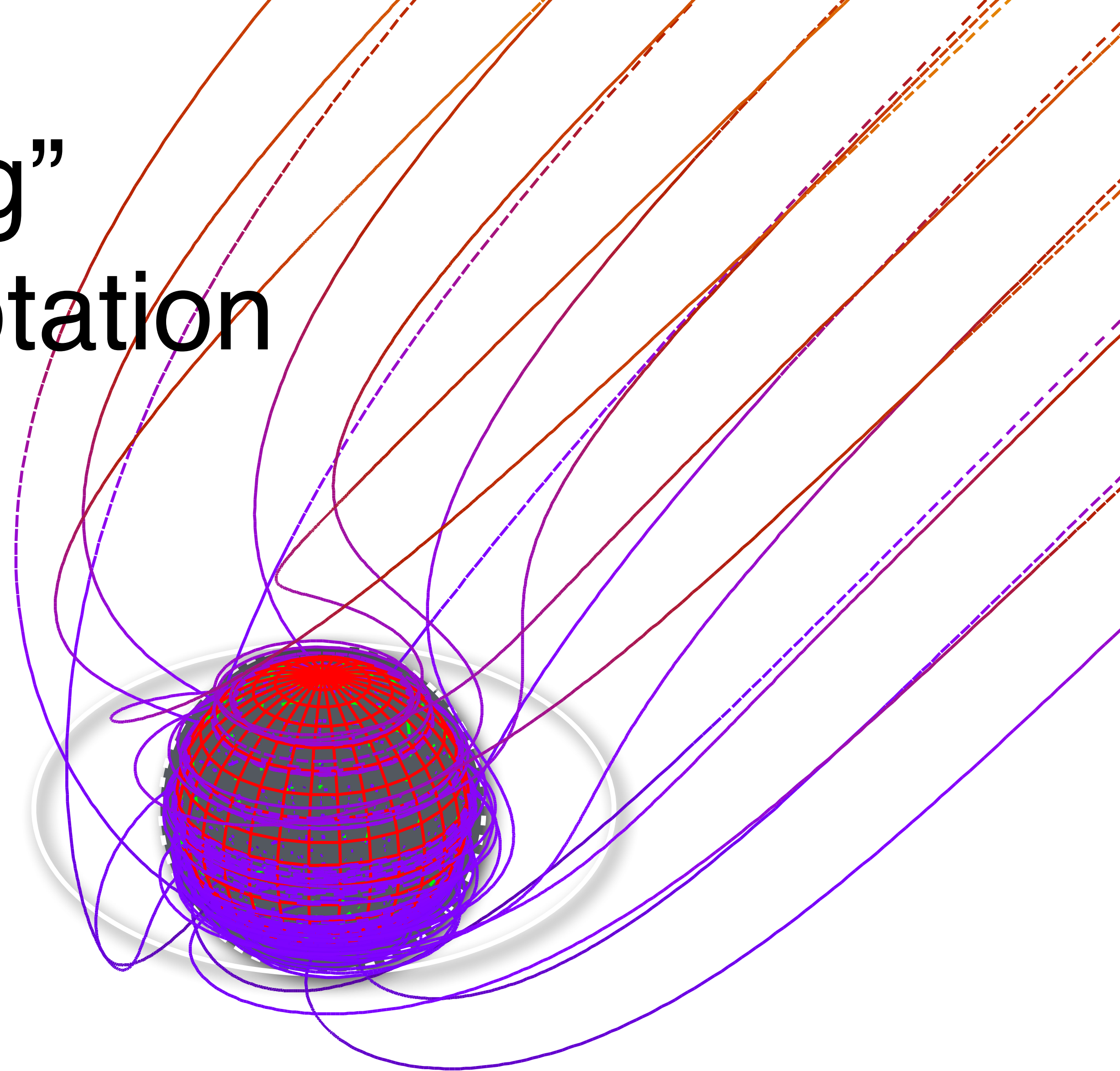
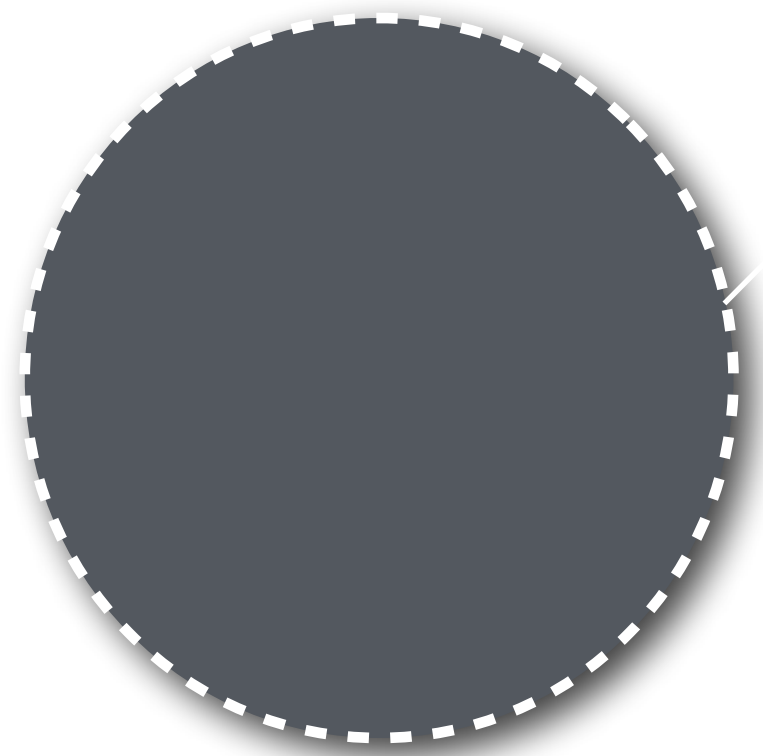
static limit

$$-1 < a^* = (J/M_{\text{BH}}c)/M_{\text{BH}} < 1$$

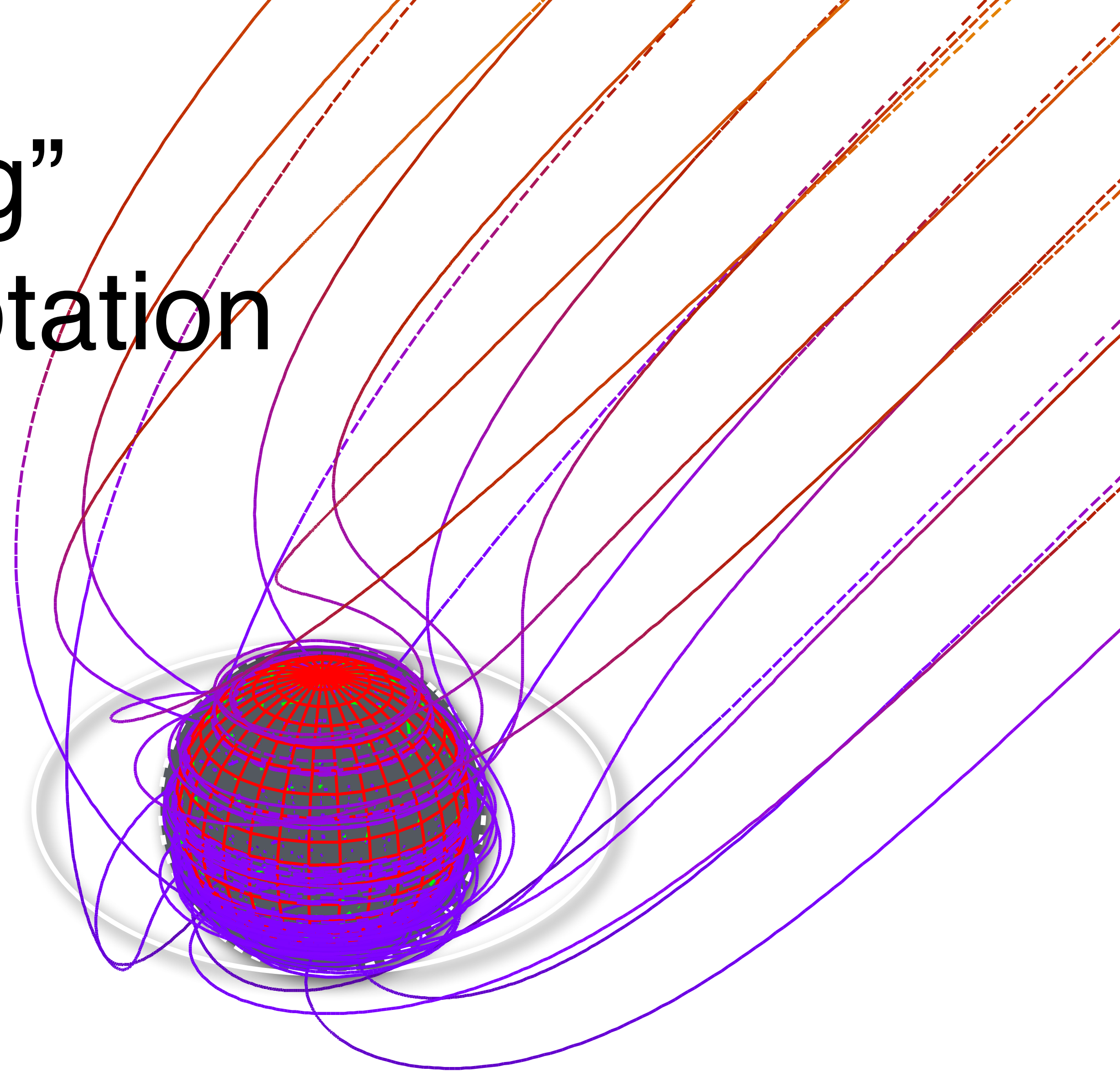
Kerr hypothesis: “astronomical black holes are described by the Kerr metric”



“frame dragging”
due to spacetime rotation

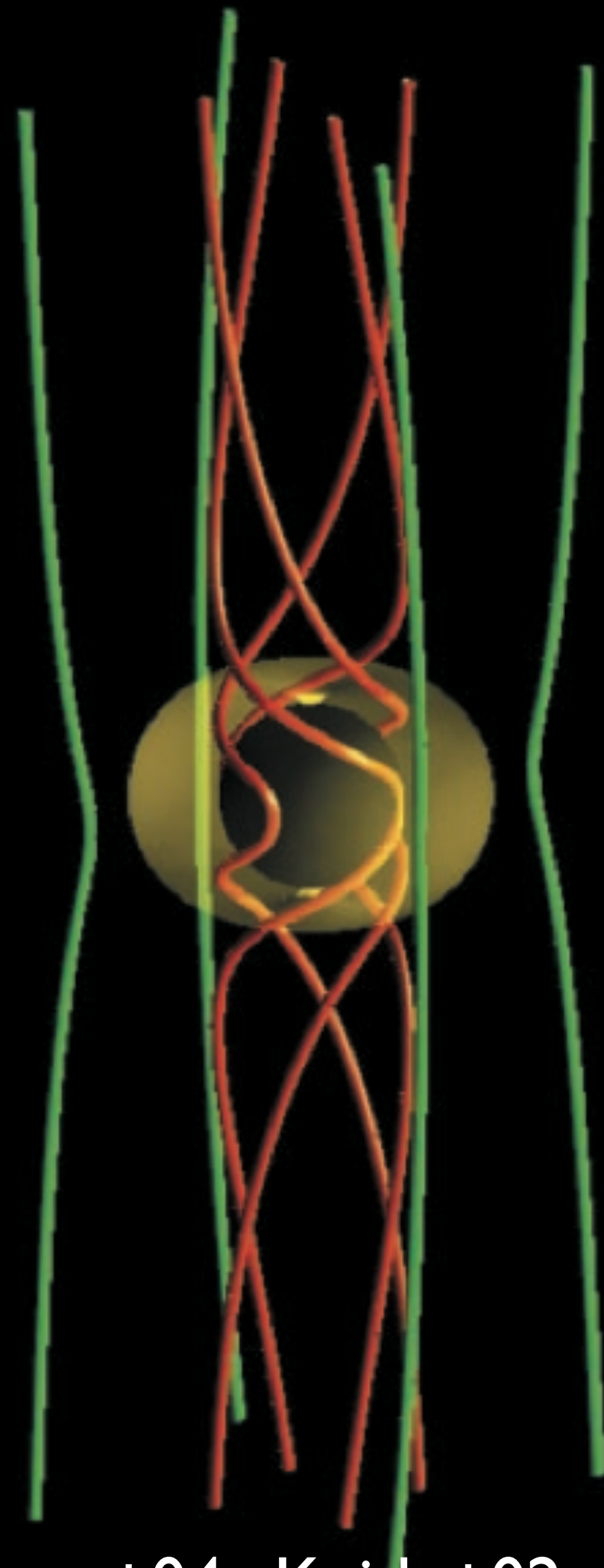


“frame dragging”
due to spacetime rotation



extraction of BH rotational energy by magnetic fields

Penrose71,
Blanford&Znajek+04,
Takahashi+90

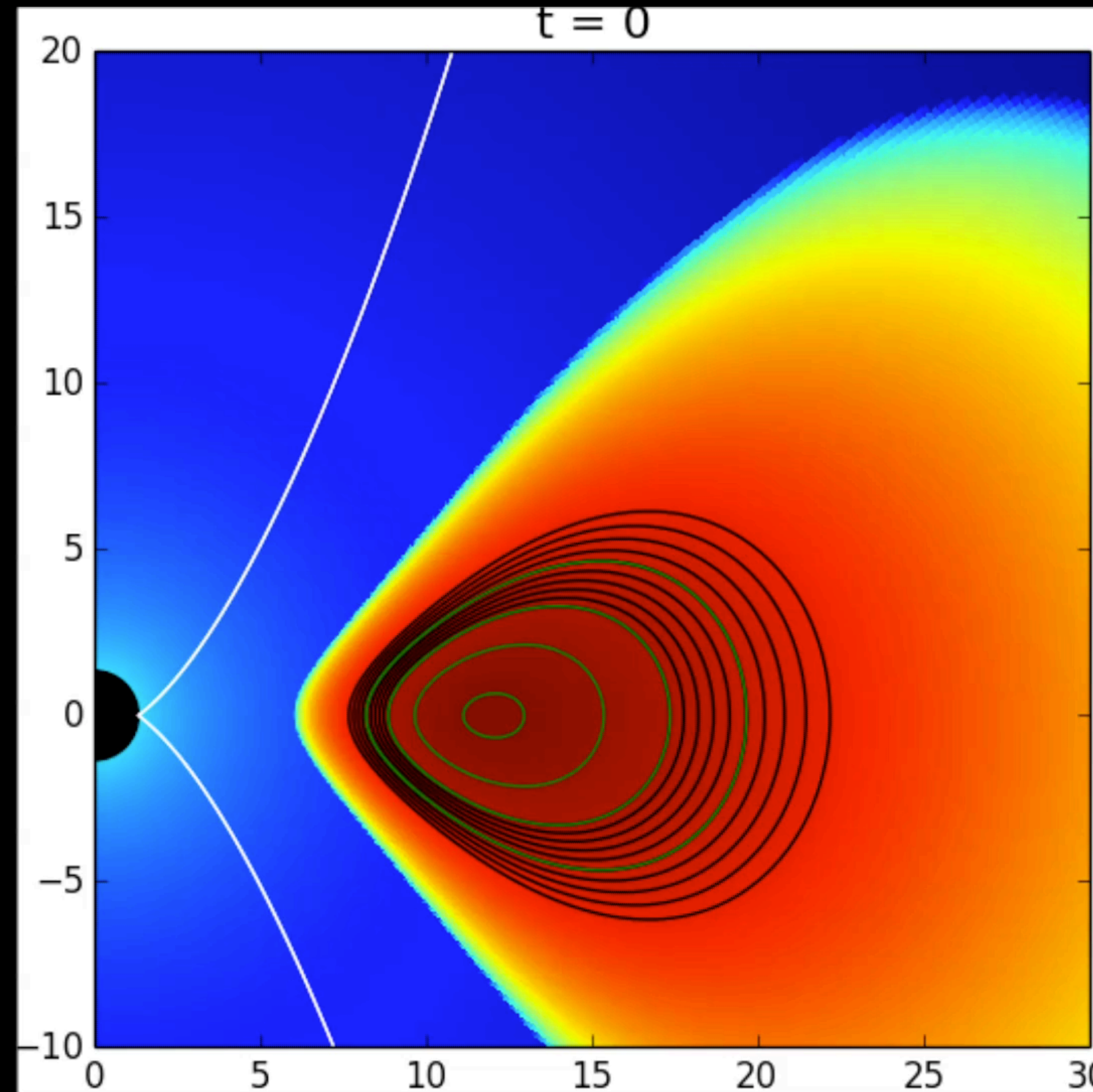
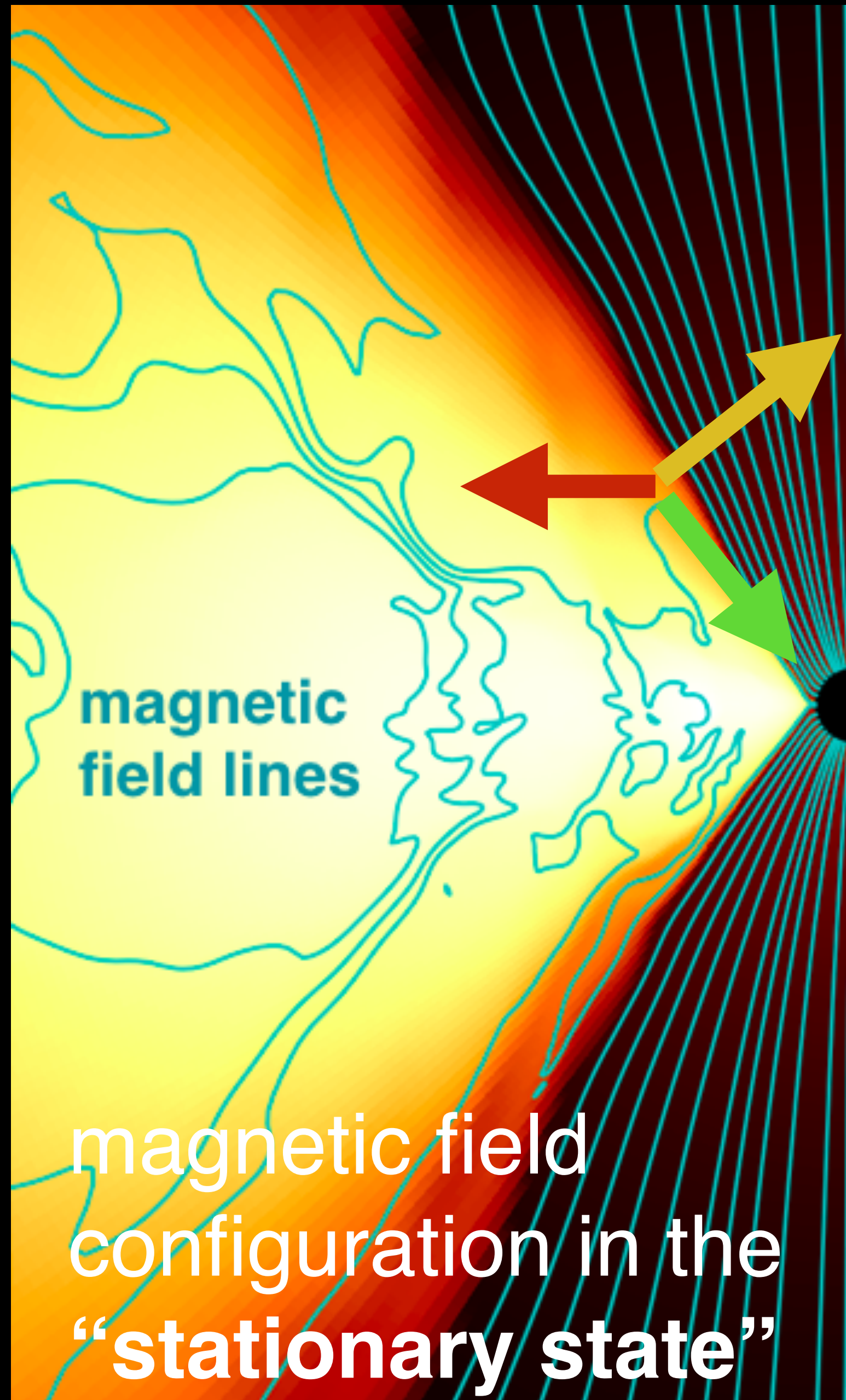


Semenov+04, Koide+02

few plasma (nearly vacuum)



General Relativistic MagnetoHydroDynamics simulation



more plasma —> accretion flow

magnetic field

strong

weak

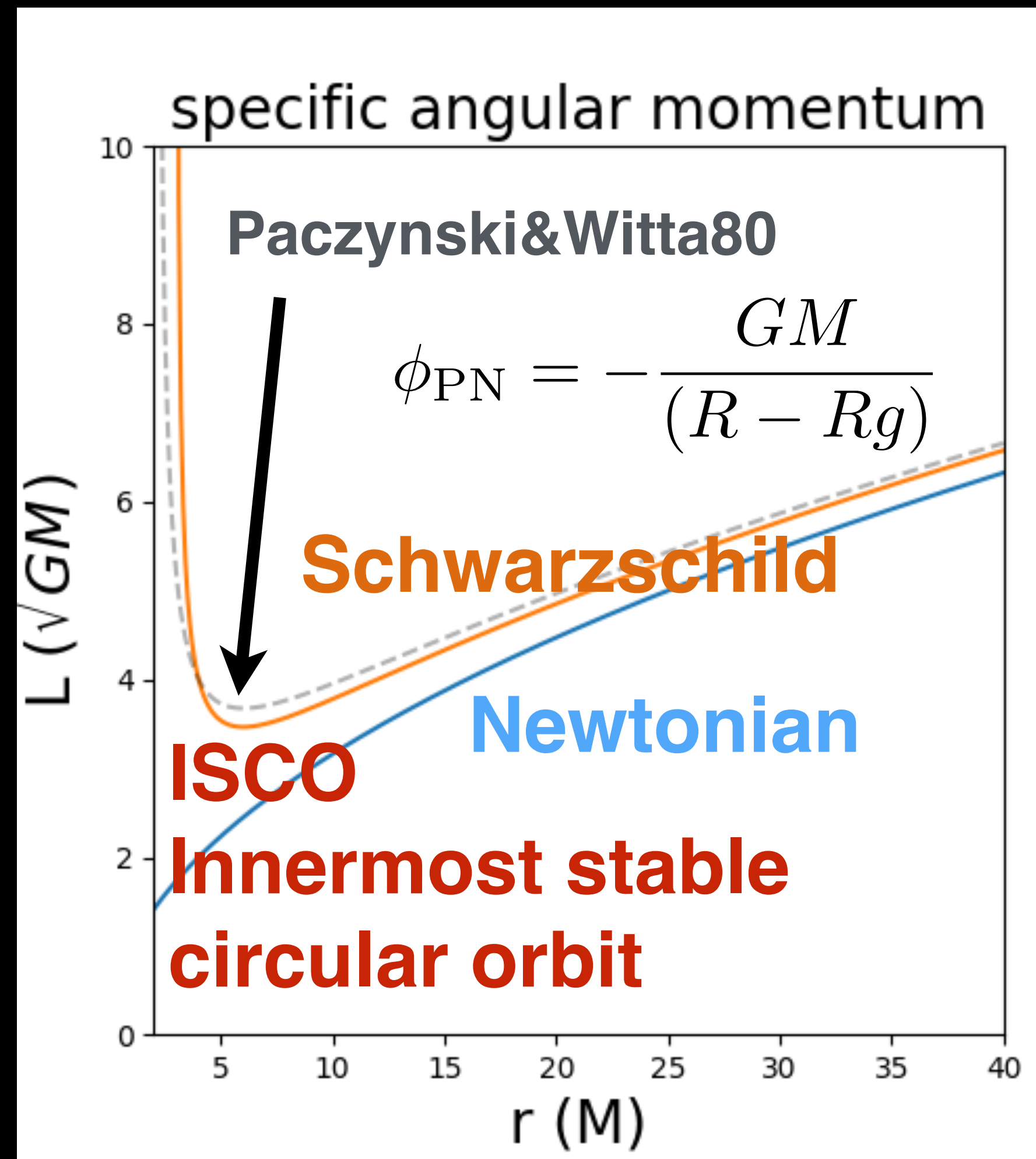
braking

Magneto-
Rotational
Instability

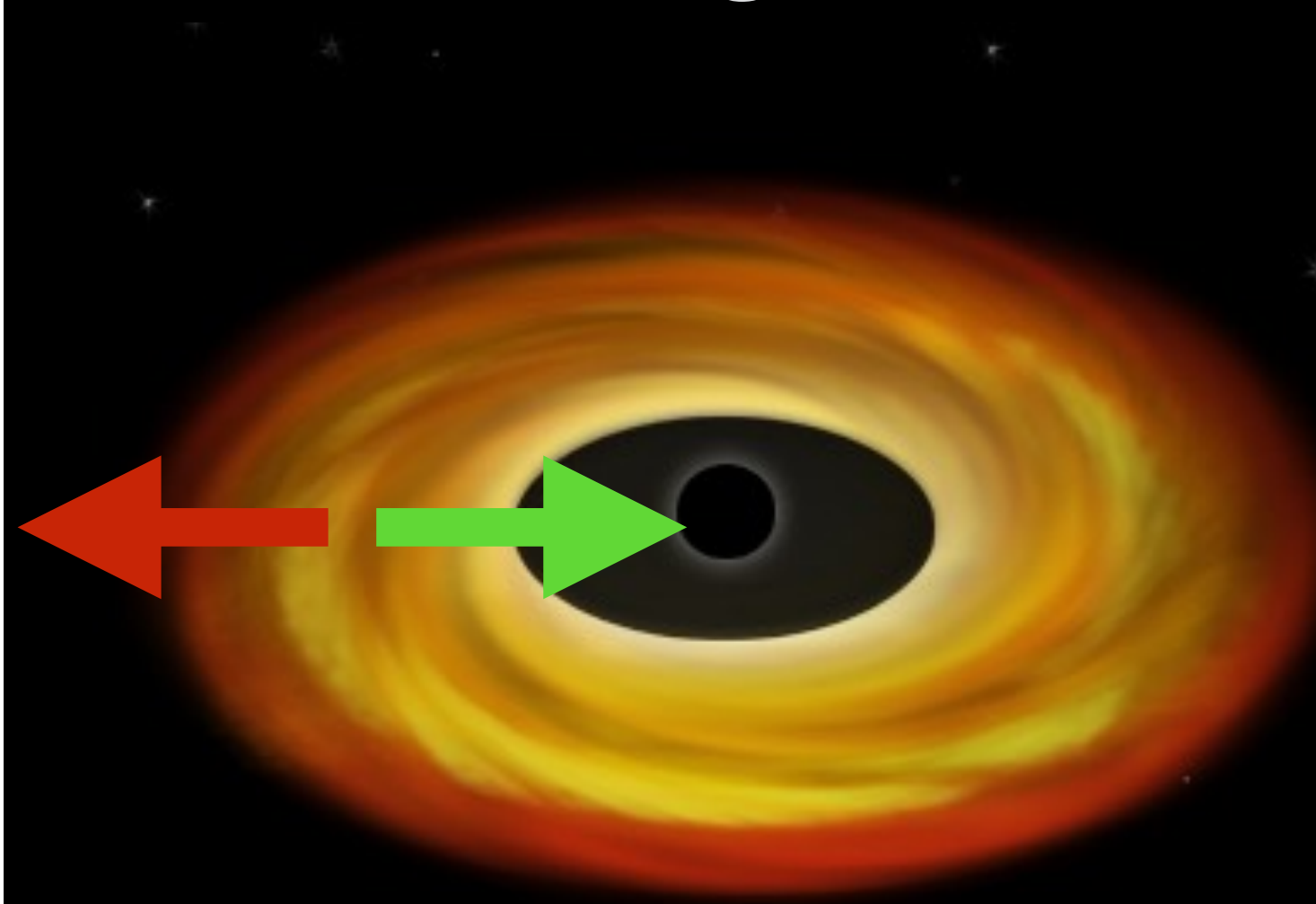
(Bulbus & Hawley 91)

$$R = \frac{2GM}{c^2}$$

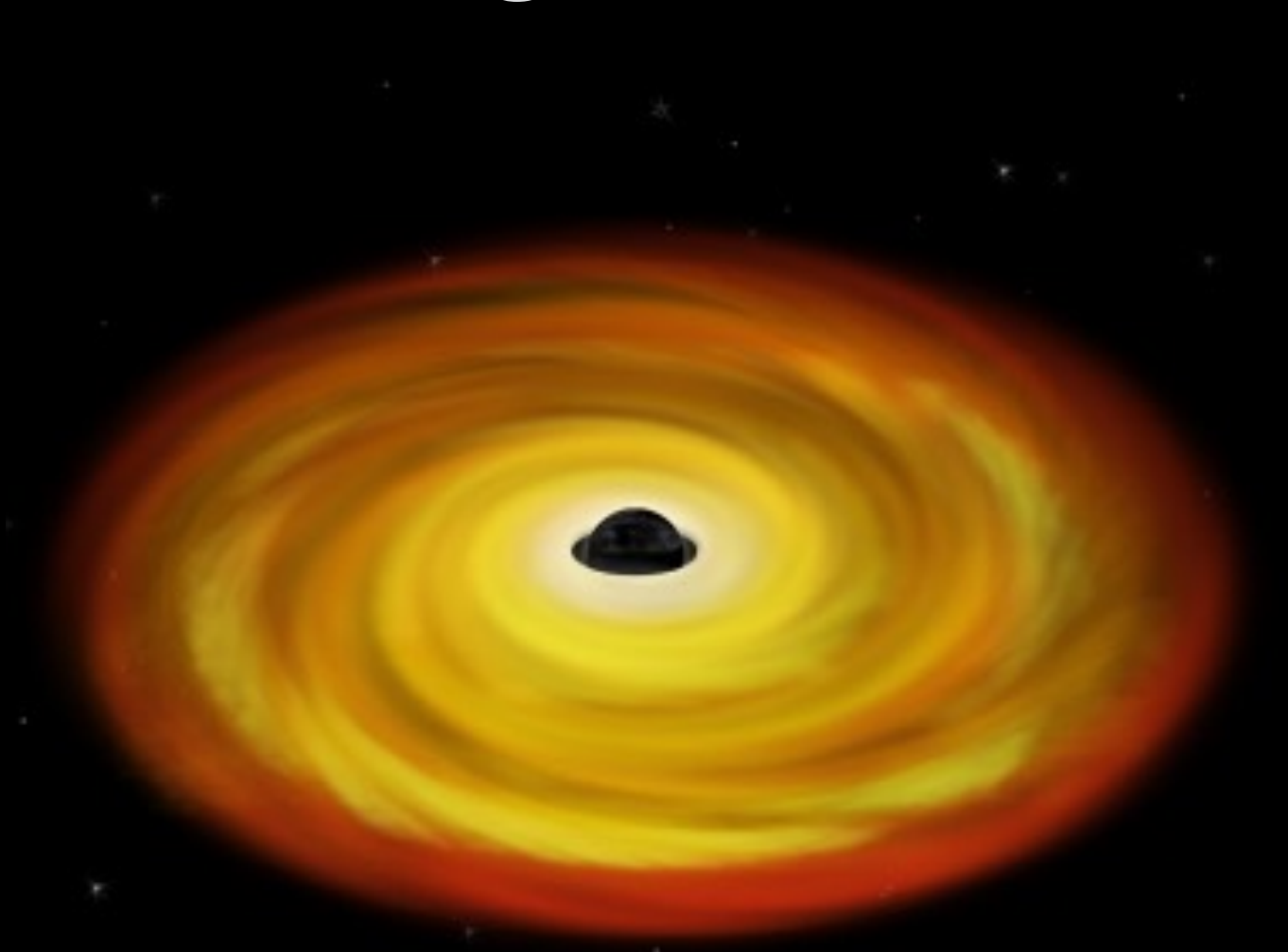
$$\Delta E \approx \frac{GMm}{R} = 0.5mc^2$$

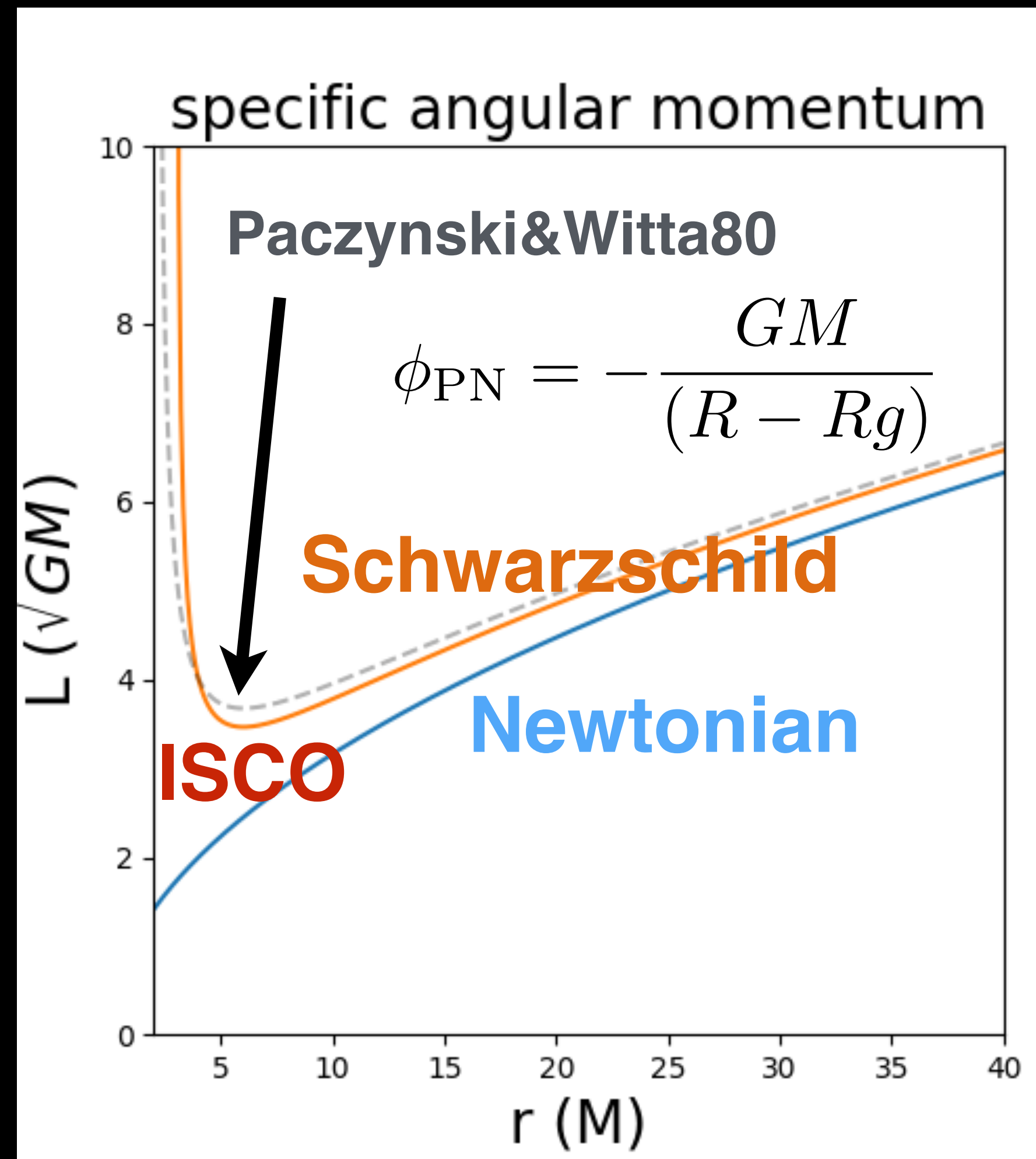


non-rotating black hole

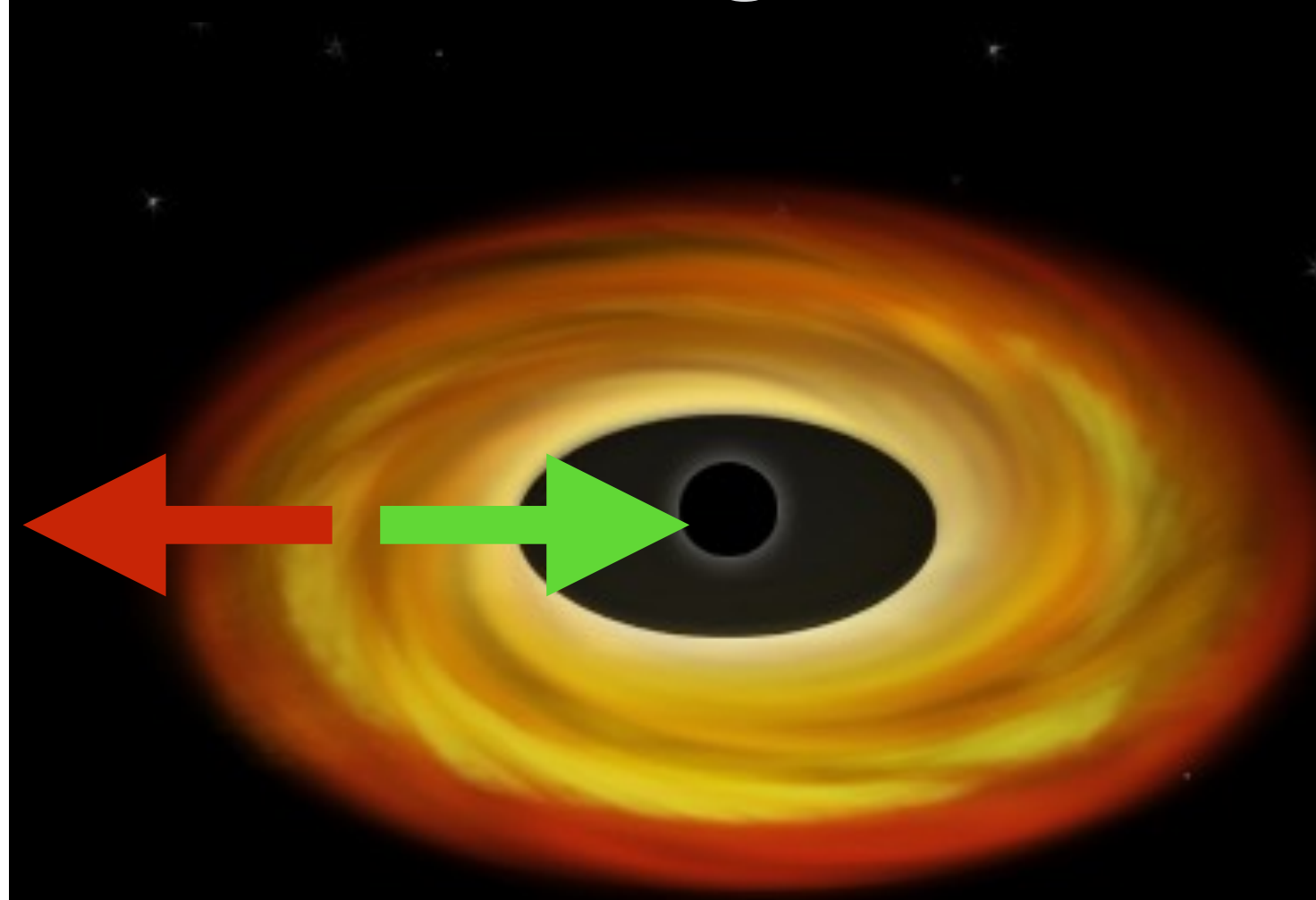


rotating black hole



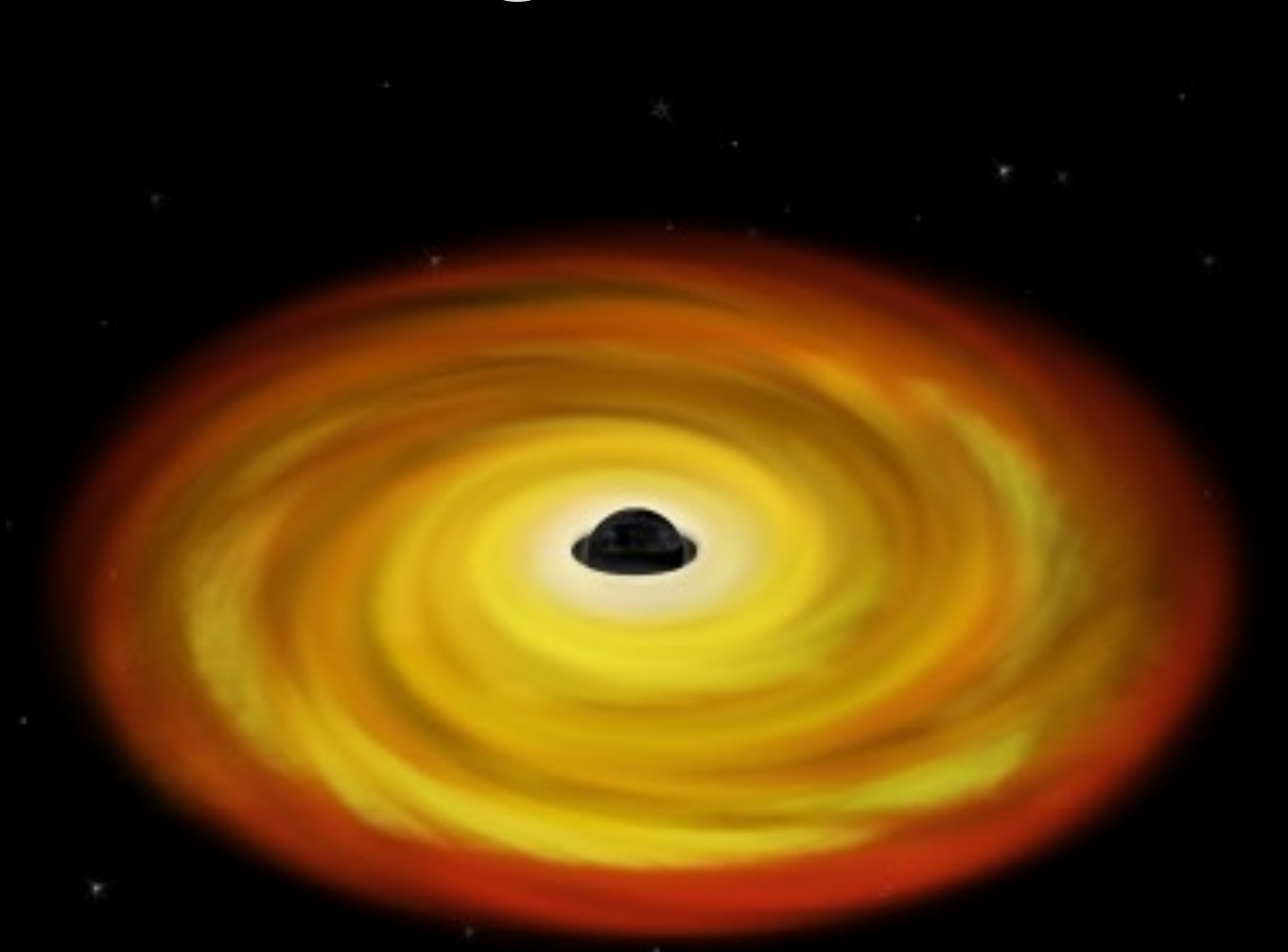


non-rotating black hole



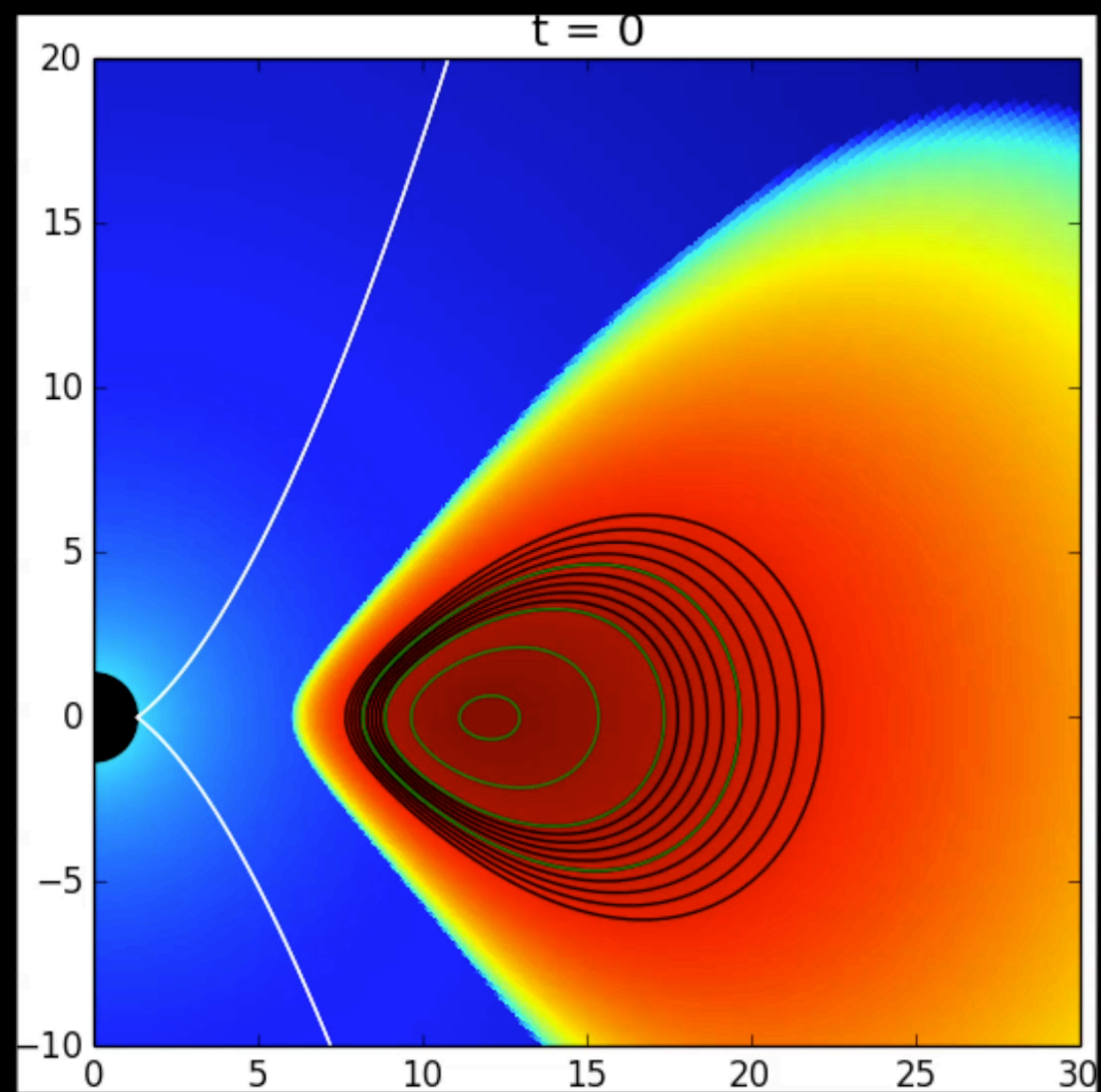
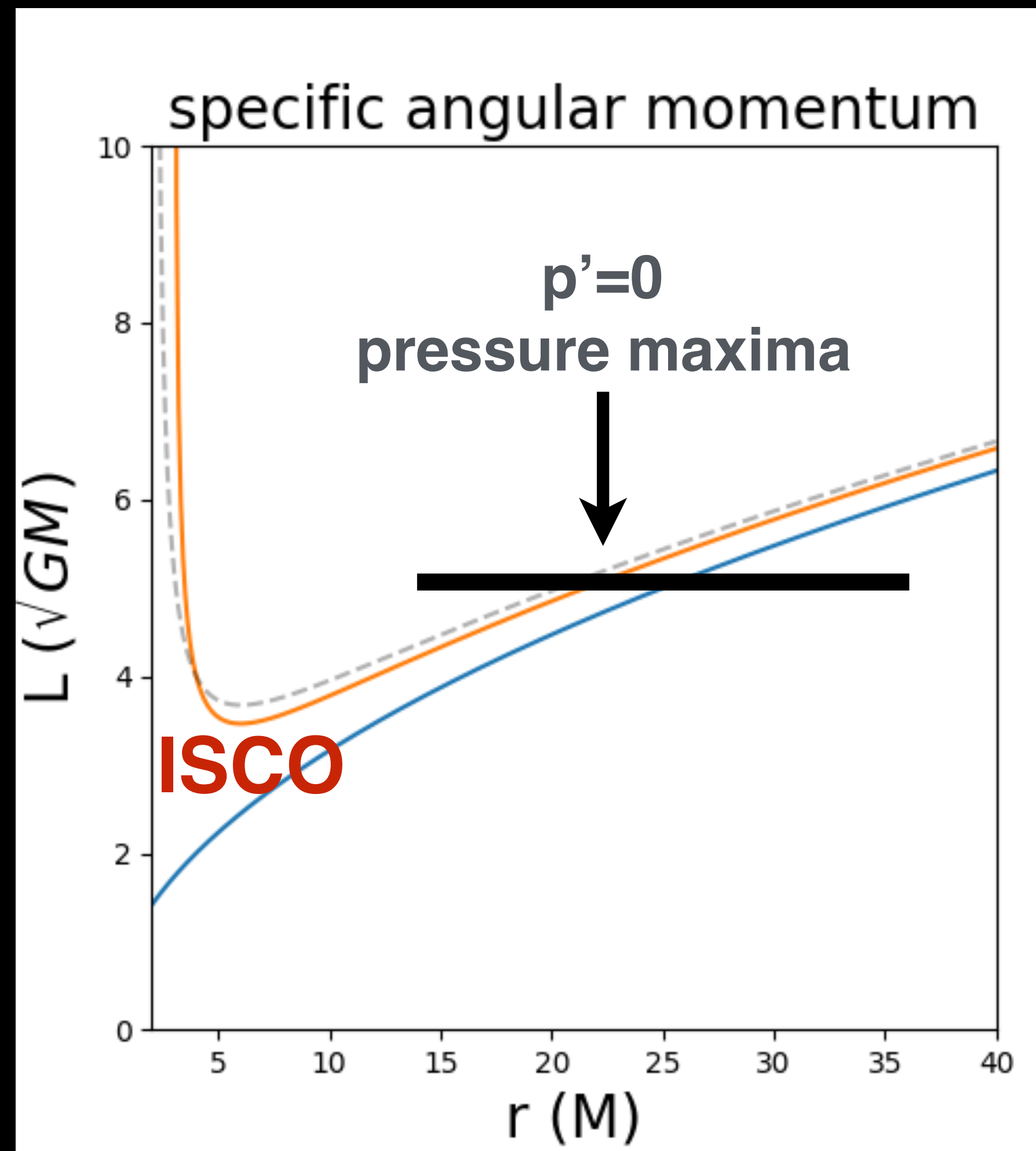
$$E|_{\infty} - E|_{\text{ISCO}} = 0.06 \dot{m}c^2$$

rotating black hole



$$E|_{\infty} - E|_{\text{ISCO}} = 0.42 \dot{m}c^2$$

BH accretion:
most powerful stable power factory in the
Universe



$$\frac{l^2}{r^3} = \frac{GM}{r^2}$$

centrifugal
force

gravity
force

centrifugal force barrier:

$$r_{\text{barrier}} = \frac{l^2}{GM}$$

angular momentum problem for
object with $R > r_{\text{barrier}}$

ways to accretion: (1) get rid of angular momentum (2) shock



inevitable plasma heating
=> where does those energy go?

$$v_r \rho T \frac{ds}{dr} = q^+ - q^- = q^{\text{adv}}$$

$$v_r \rho T \frac{ds}{dr} = q^+ - q^- = q^{\text{adv}}$$

viscous
heating

radiative
cooling

advection
cooling

thin disk

(Shakura-Sunyaev 1973, Novikov-Throne 1973)

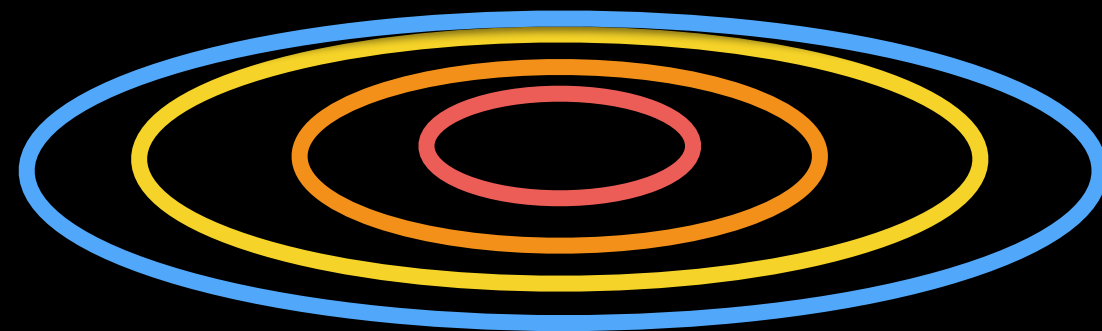
Yu-Yen's talk

radiative cooling dominated:

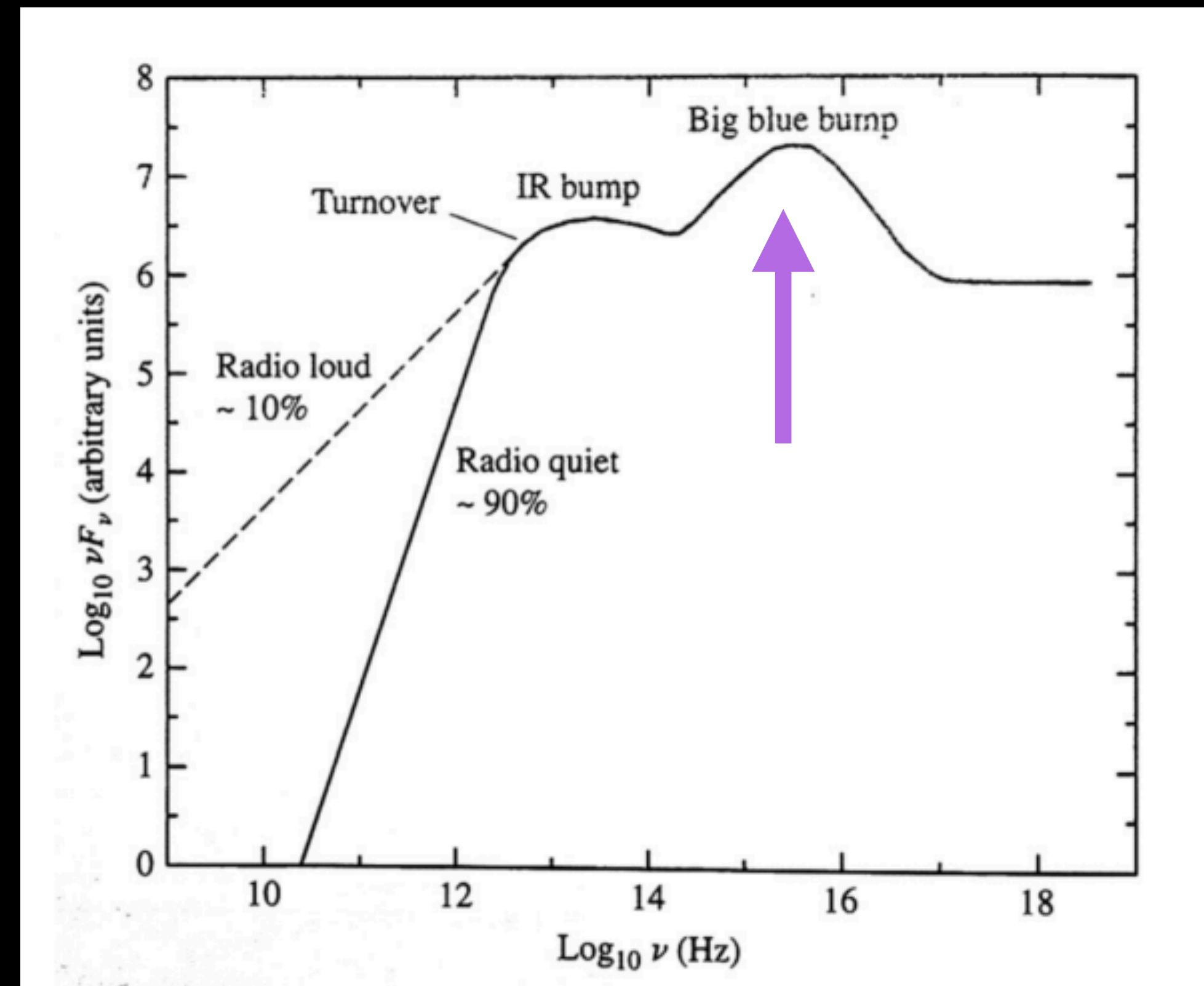
$$q^+ \approx q^- (\gg q^{\text{adv}})$$

Teff(r): multi-color

$$T \sim 10^{5-7} \text{ K}$$



luminous quasar, Seyferts, BHXB in
thermal high/soft state



$$v_r \rho T \frac{ds}{dr} = \underbrace{q^+}_{\text{viscous heating}} - \underbrace{q^-}_{\text{radiative cooling}} = \underbrace{q^{\text{adv}}}_{\text{advection cooling}}$$

ADAF

advection cooling dominated:

(Ichimaru77; Narayan & Yi 94, 95; Abramowicz+95, Yuan & Narayan 14)

(Begelman78; Abramowicz+89; Sadowski+14)

$$q^+ \approx q^{\text{adv}} (\gg q^-)$$

(radiatively inefficient accreting flow)

heat are stored inside the flow due to:

optically thin

low density,
collisionless
($T_i \sim T_{\text{virial}} \gg T_e$)

LLAGN, BHXB in thermal low/hard state

optically thick

high density,
photon trapping

Tidal disruption events, Ultra Luminous X-ray binaries

$$v_r \rho T \frac{ds}{dr} = q^+ - q^- = q^{\text{adv}}$$

**viscous
heating**

**radiative
cooling**

**advection
cooling**

ADAF

advection cooling dominated:

(Ichimaru77; Narayan & Yi 94,
95; Abramowicz+95, Yuan &
Narayan 14)

(Begelman78; Abramowicz+
89; Sadowski+14)

$$q^+ \approx q^{\text{adv}} (\gg q^-)$$

(radiatively inefficient accreting flow)

★another choice: outflow

ADIOS

(advection-dominated
inflow-outflow solutions;
Blandford & Begelman 99)

optically thin

low density,
collisionless
($T_i \sim T_{\text{virial}} \gg T_e$)

**LLAGN, BHXB in thermal
low/hard state**

optically thick

high density,
photon trapping

**Tidal disruption events,
Ultra Luminous X-ray
binaries**

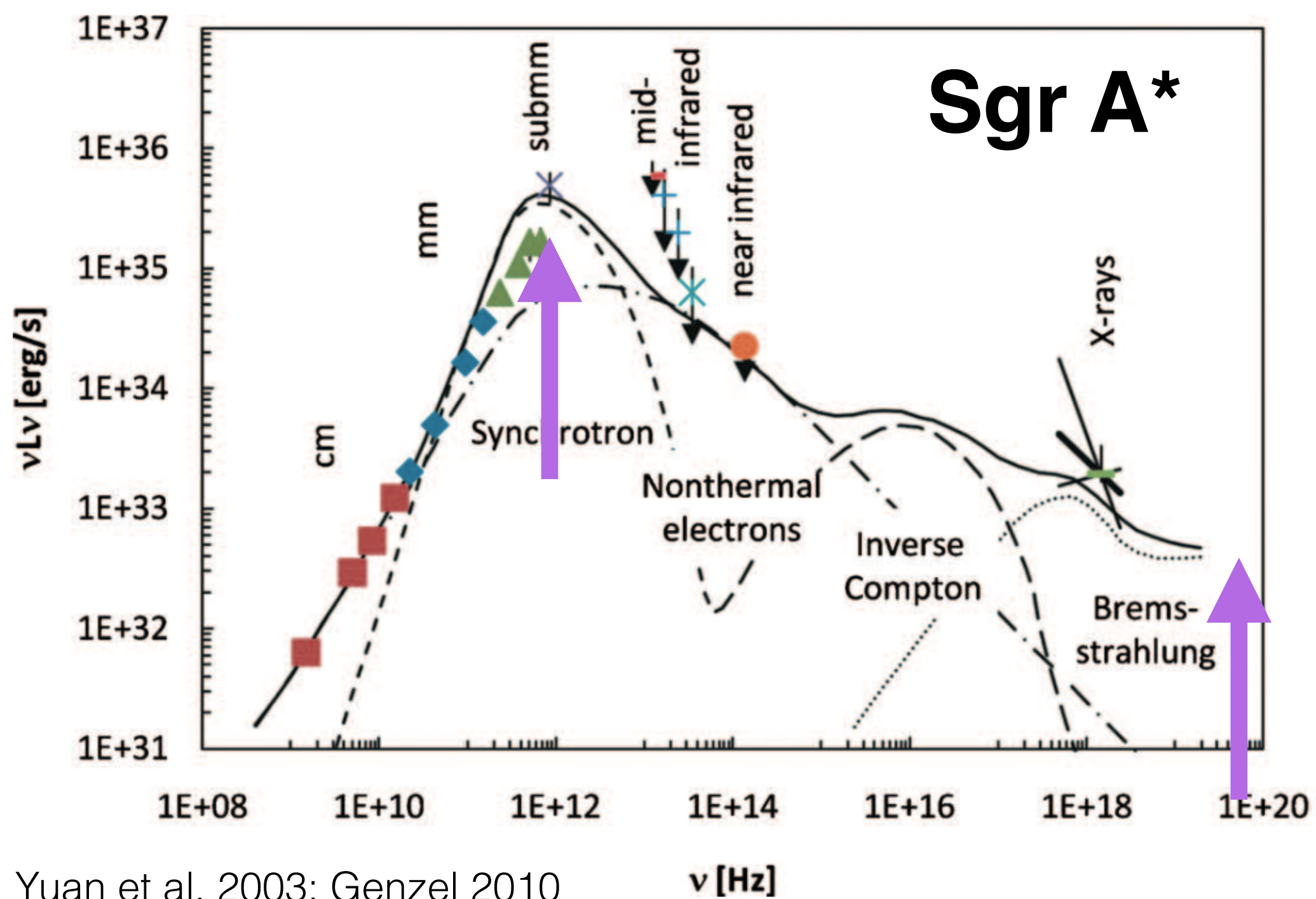
$$v_r \rho T \frac{ds}{dr} = q^+ - q^- = q^{\text{adv}}$$

**viscous
heating**

**radiative
cooling**

**advection
cooling**

ADAF



Yuan et al. 2003; Genzel 2010

we can see BH shadow!

optically thin

$T_i \sim 10^{11-12} \text{ K}$

$T_e < 10^9-11 \text{ K}$

**including primary EHT
tagets: Sgr A*, M87**

**mm/sub-mm
observation for M87
(from syn. emission)**

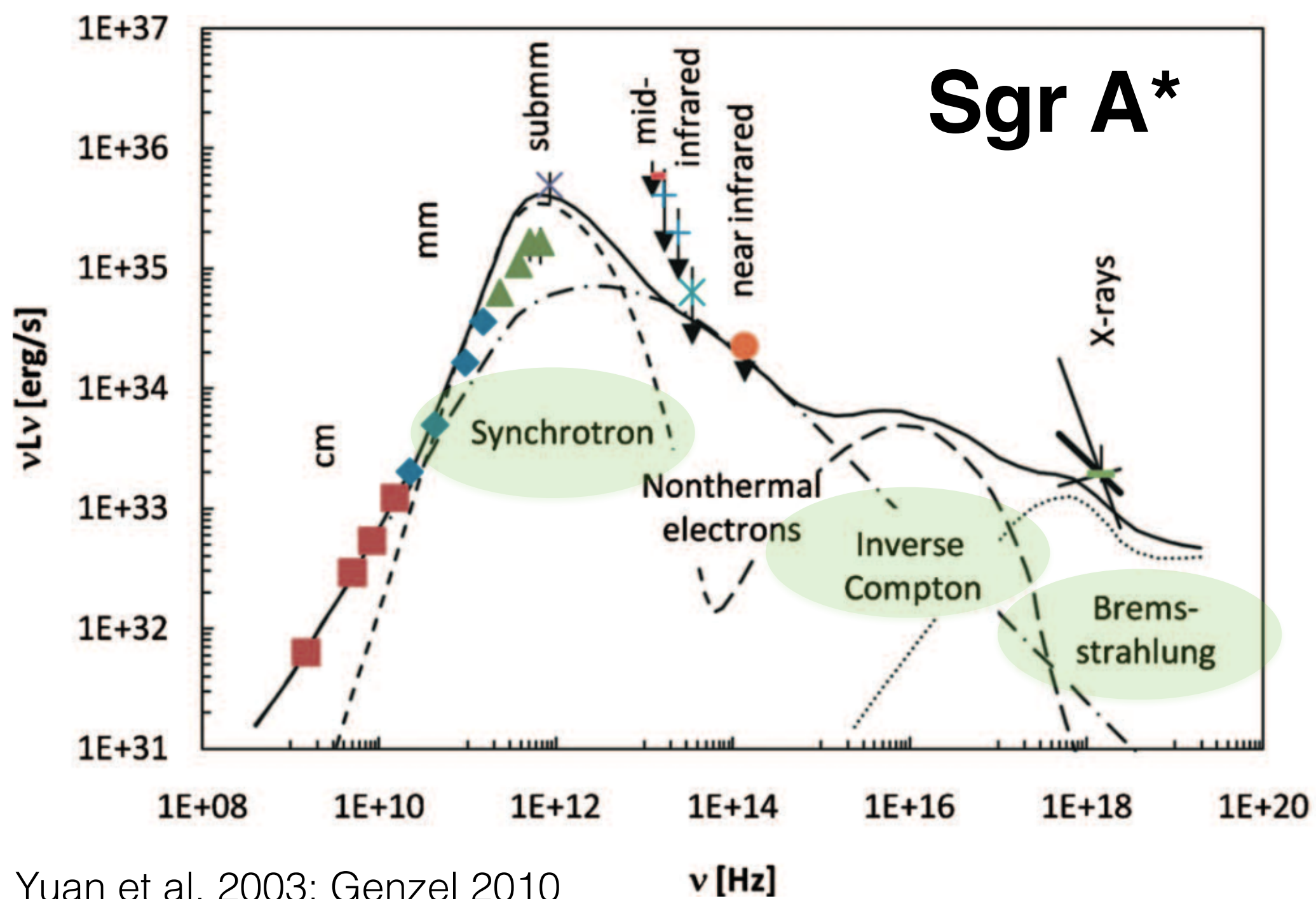
$$v_r \rho T \frac{ds}{dr} = q^+ - q^- = q^{\text{adv}}$$

**viscous
heating**

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ADAF



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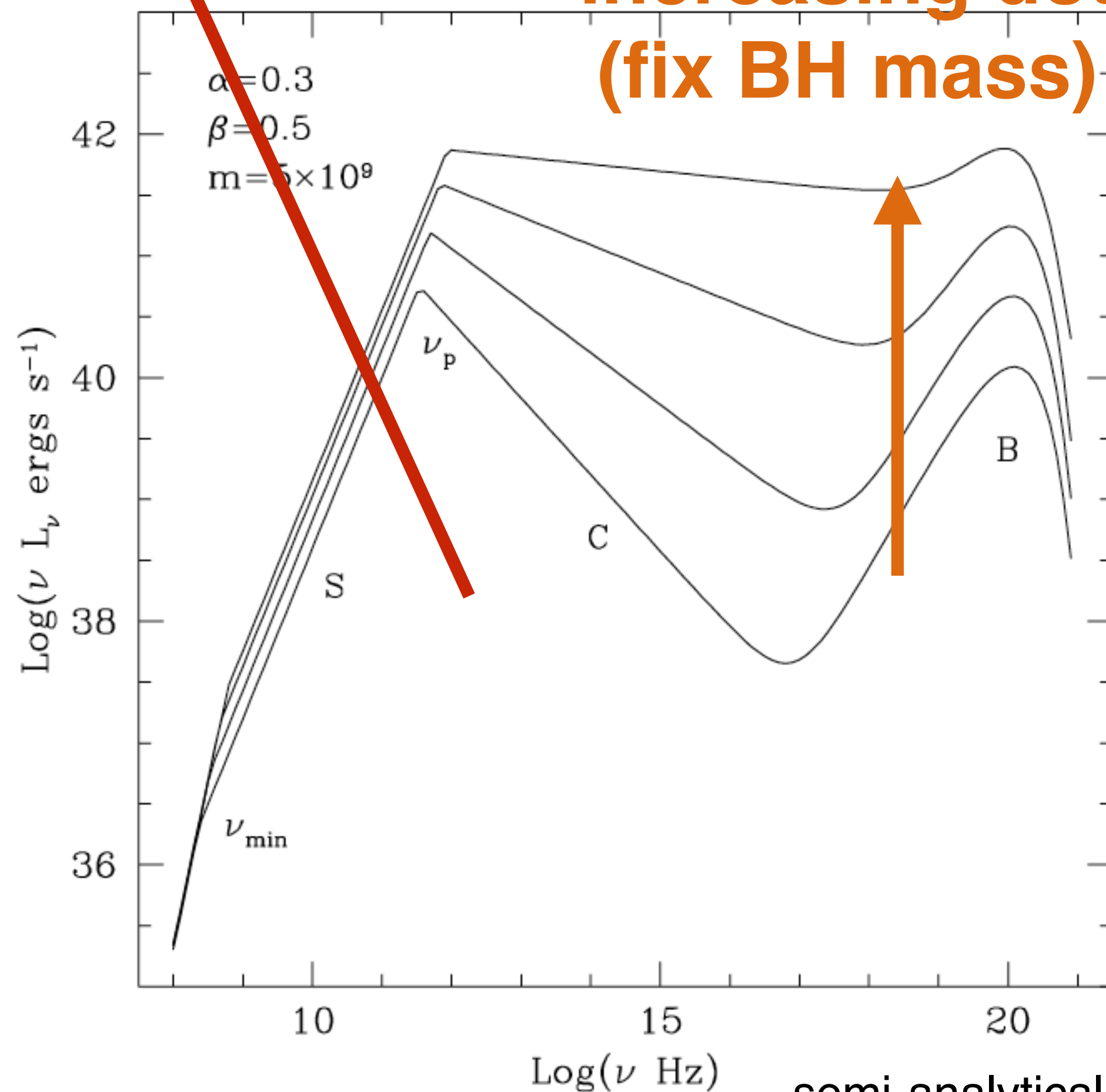
**mm/sub-mm
observation for M87
(from syn. emission)**

increasing BH mass
(fix mdot)

BHs: big and small

— Eddington accretion rate

increasing dot
(fix BH mass)



$$L_{\text{Edd}} = 1.26 \times 10^{38} \frac{M_{\text{BH}}}{M_{\odot}} \text{ erg/sec}$$

$$\dot{M}_{\text{Edd}} = \frac{L_{\text{Edd}}}{\eta_{\text{eff}} c^2} = 2 \times 10^{-8} \frac{M_{\text{BH}}}{M_{\odot}} M_{\odot}/\text{yr}$$

$$\dot{M}_{\text{BH}} = \dot{m} \dot{M}_{\text{Edd}}$$

$$\dot{M}_{\text{BH}} / \dot{M}_{\text{Edd}}$$

cf. Ken's talk

accretion rate

optically-thick ADAF: slim disk

**(advection cooling)
due to photon trapping**

1

thin disk

(radiation cooling)

0.01

optically-thin ADAF, hot accretion flow

**(advection cooling)
due to hot ions**

$$\dot{M}_{\text{BH}} / \dot{M}_{\text{Edd}}$$

accretion rate

optically-thick ADAF: slim disk

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1

thin disk

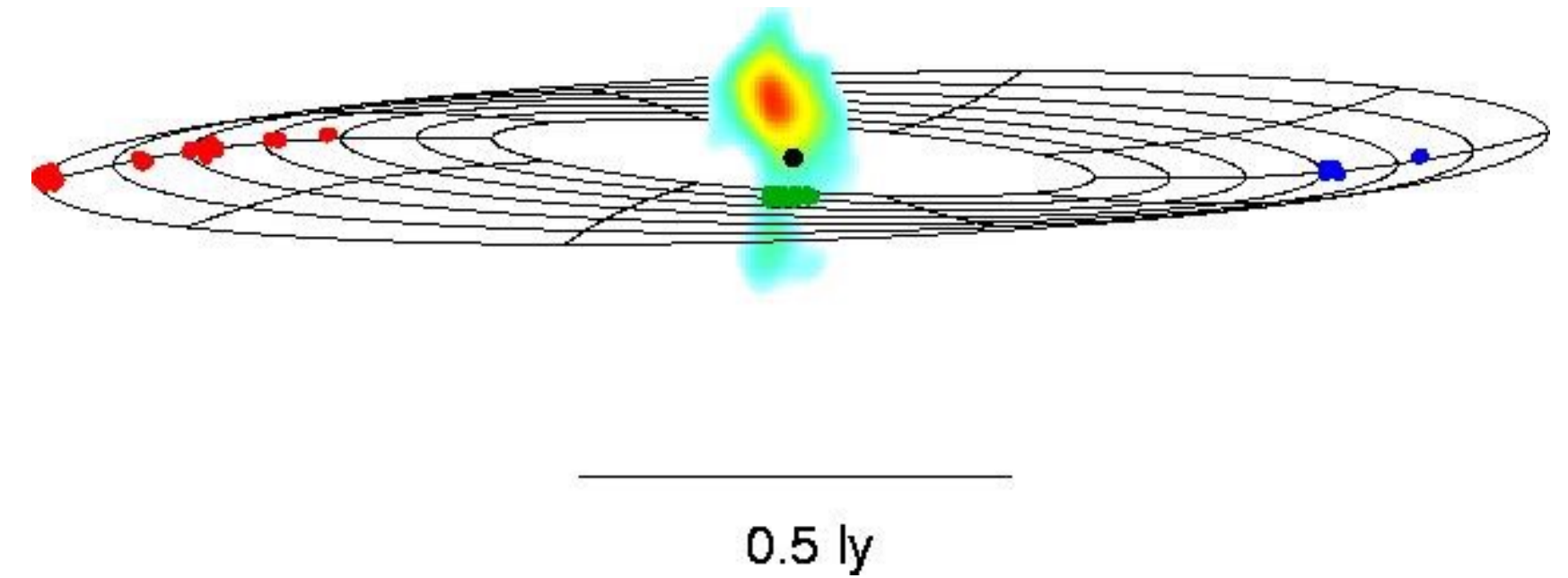
(radiation cooling)

0.01

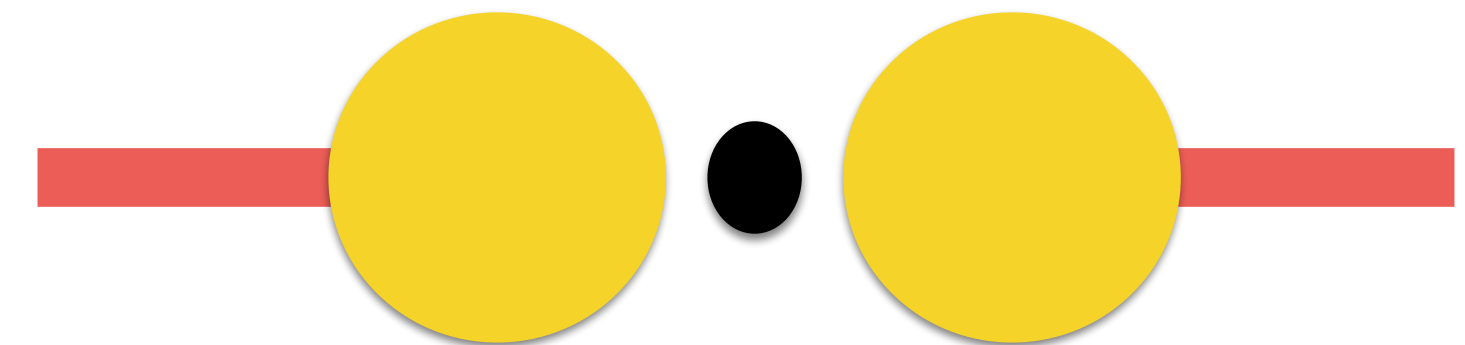
optically-thin ADAF, hot accretion flow

**(advection cooling)
due to hot ions**

Cheng-Yu's talk



e.g. NGC 4258; maser measurement confirms
the **thin disk** part



$$\dot{M}_{\text{BH}} / \dot{M}_{\text{Edd}}$$

accretion rate

optically-thick ADAF: slim disk

**(advection cooling)
due to photon trapping**

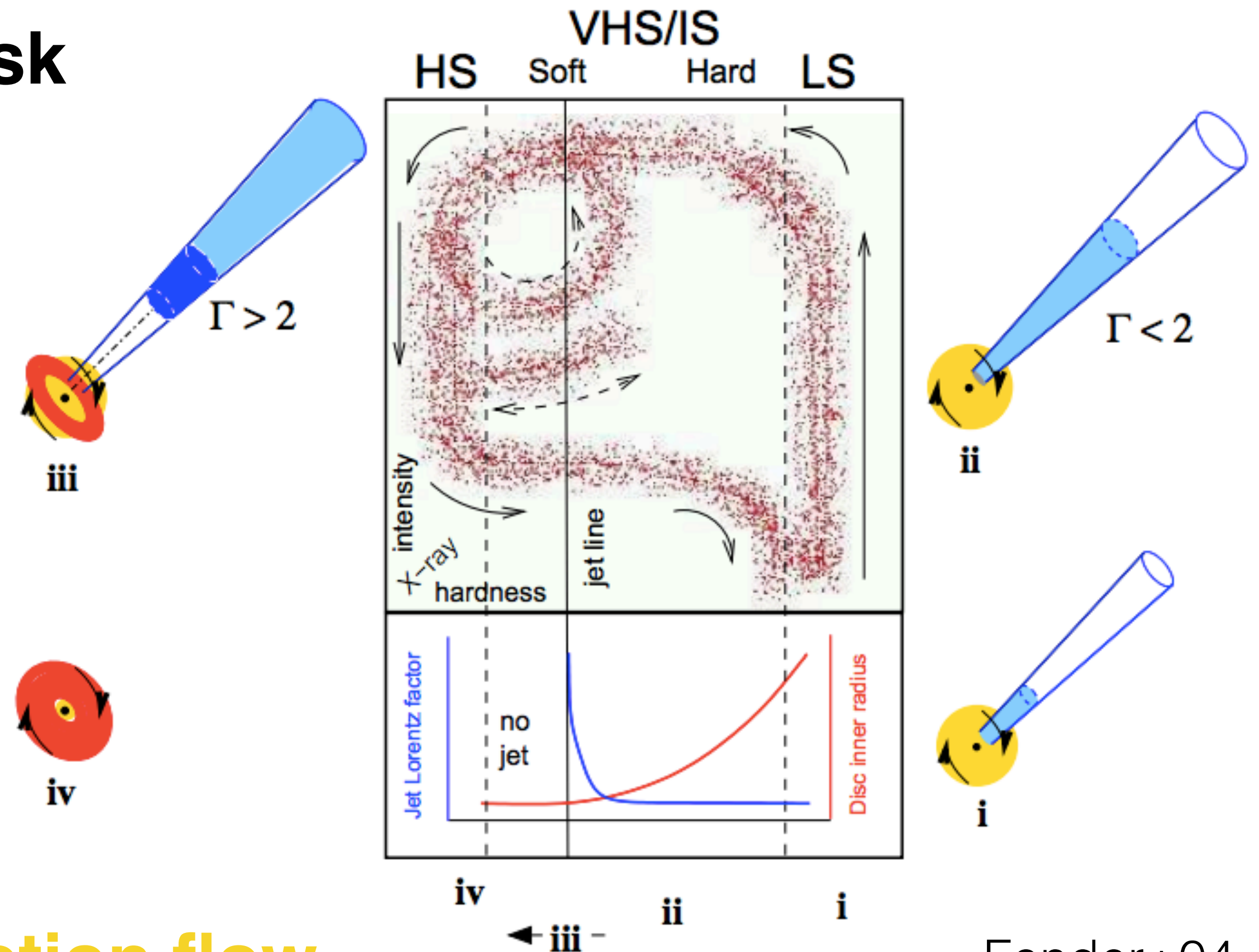
thin disk

(radiation cooling)

optically-thin ADAF, hot accretion flow

**(advection cooling)
due to hot ions**

a “unified model” from BHXB
suggests disk-jet coping



Holger's talk

$$\dot{M}_{\text{BH}} / \dot{M}_{\text{Edd}}$$

accretion rate

optically-thick ADAF: slim disk

**(advection cooling)
due to photon trapping**

1

thin disk

(radiation cooling)

0.01

optically-thin ADAF, hot accretion flow

**(advection cooling)
due to hot ions**

corresponding jet activity:

with jet + wind

no jet (maybe wind)?!

with jet + wind

(see also Pu+ 12 for a possible explanation)

$$\dot{M}_{\text{BH}} / \dot{M}_{\text{Edd}}$$

accretion rate

optically-thick ADAF: slim disk

**(advection cooling)
due to photon trapping**

corresponding jet activity:



with jet + wind

thin disk

(radiation cooling)

vertically integrated
analytical approach
cannot resolve jet
and winds:
need simulations!

no jet (maybe wind)?!

optically-thin ADAF, hot accretion flow

**(advection cooling)
due to hot ions**



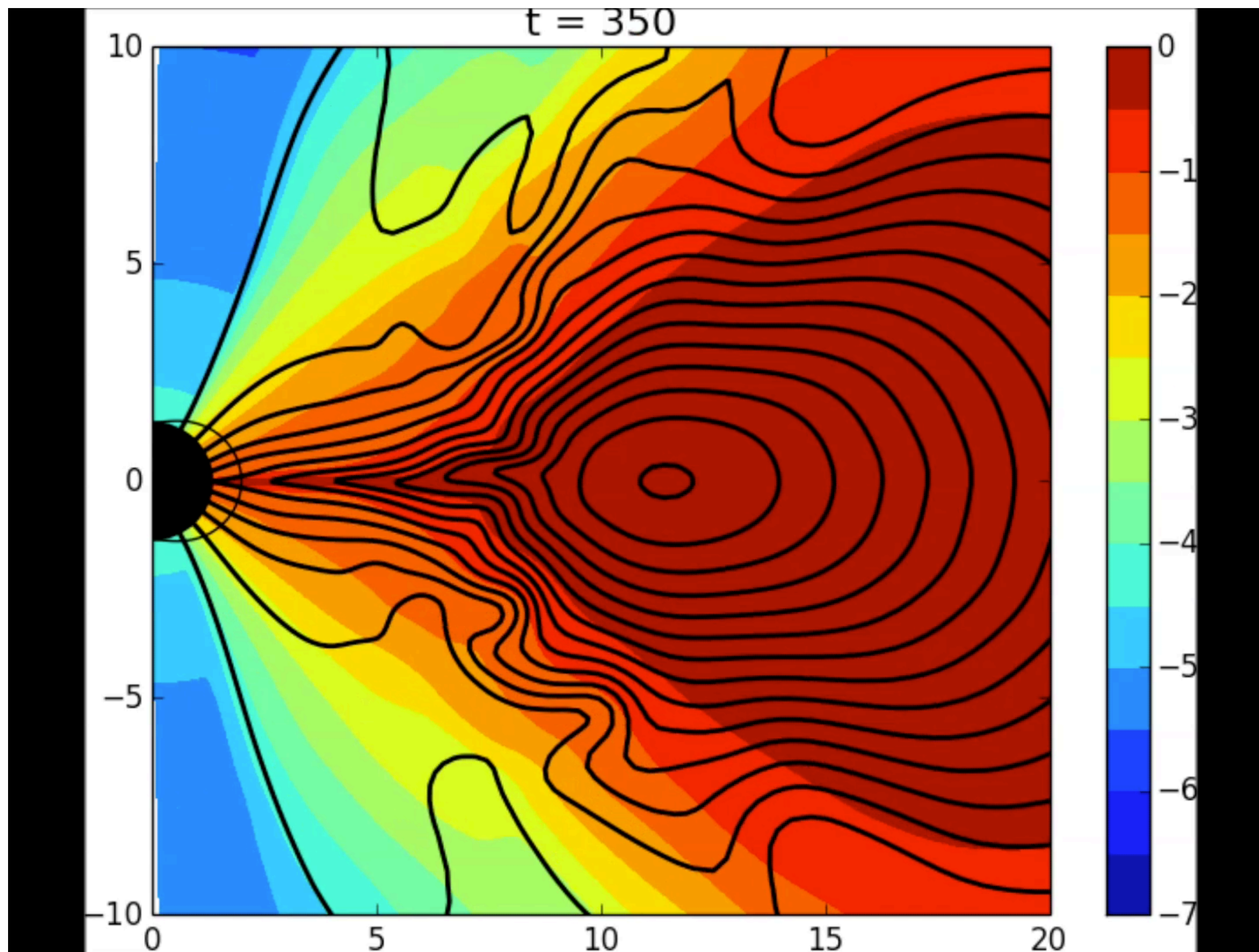
with jet + wind

1

0.01

GRMHD numerical simulation for RIAF

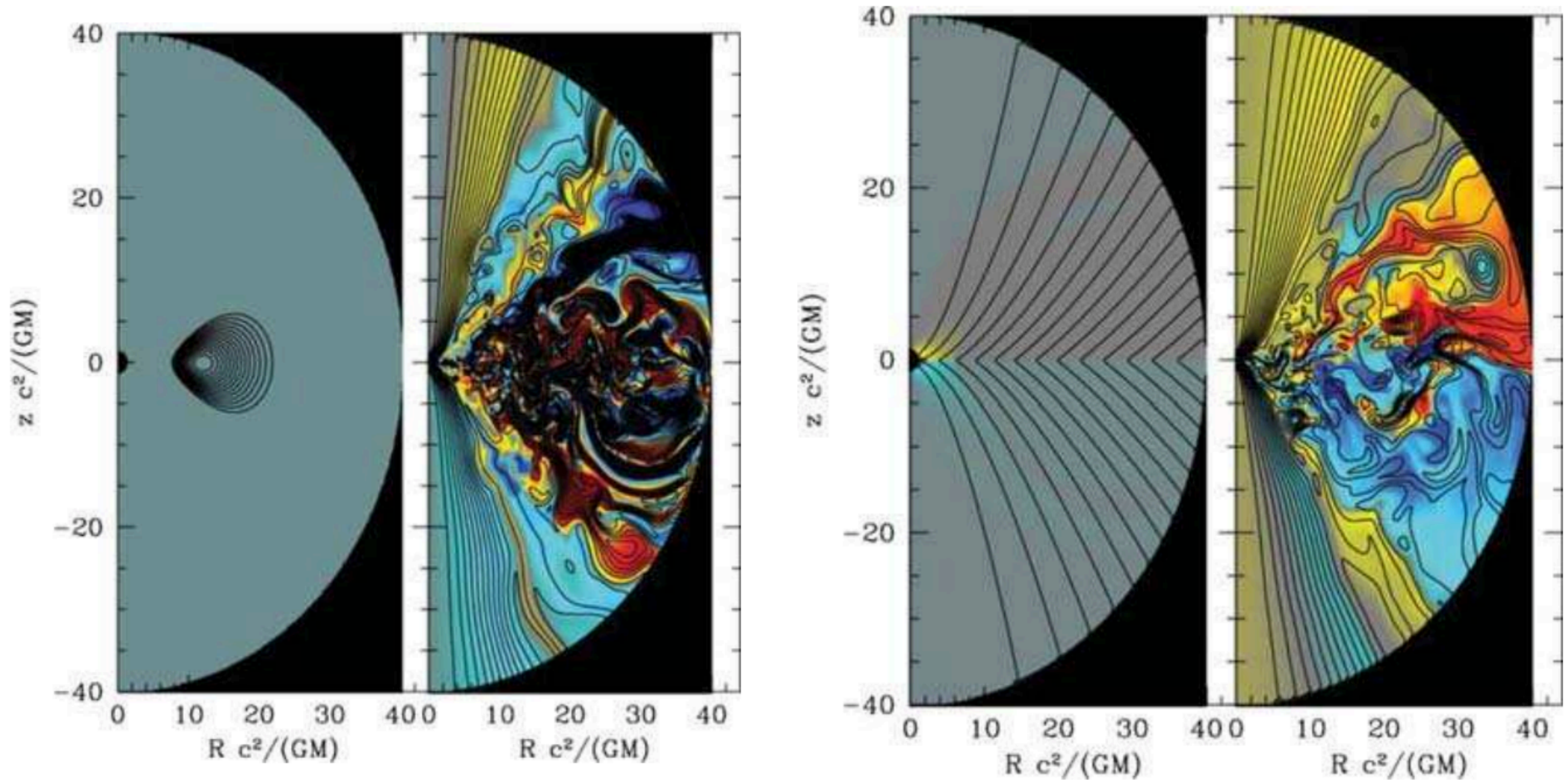
(time unit: GM/c^3)



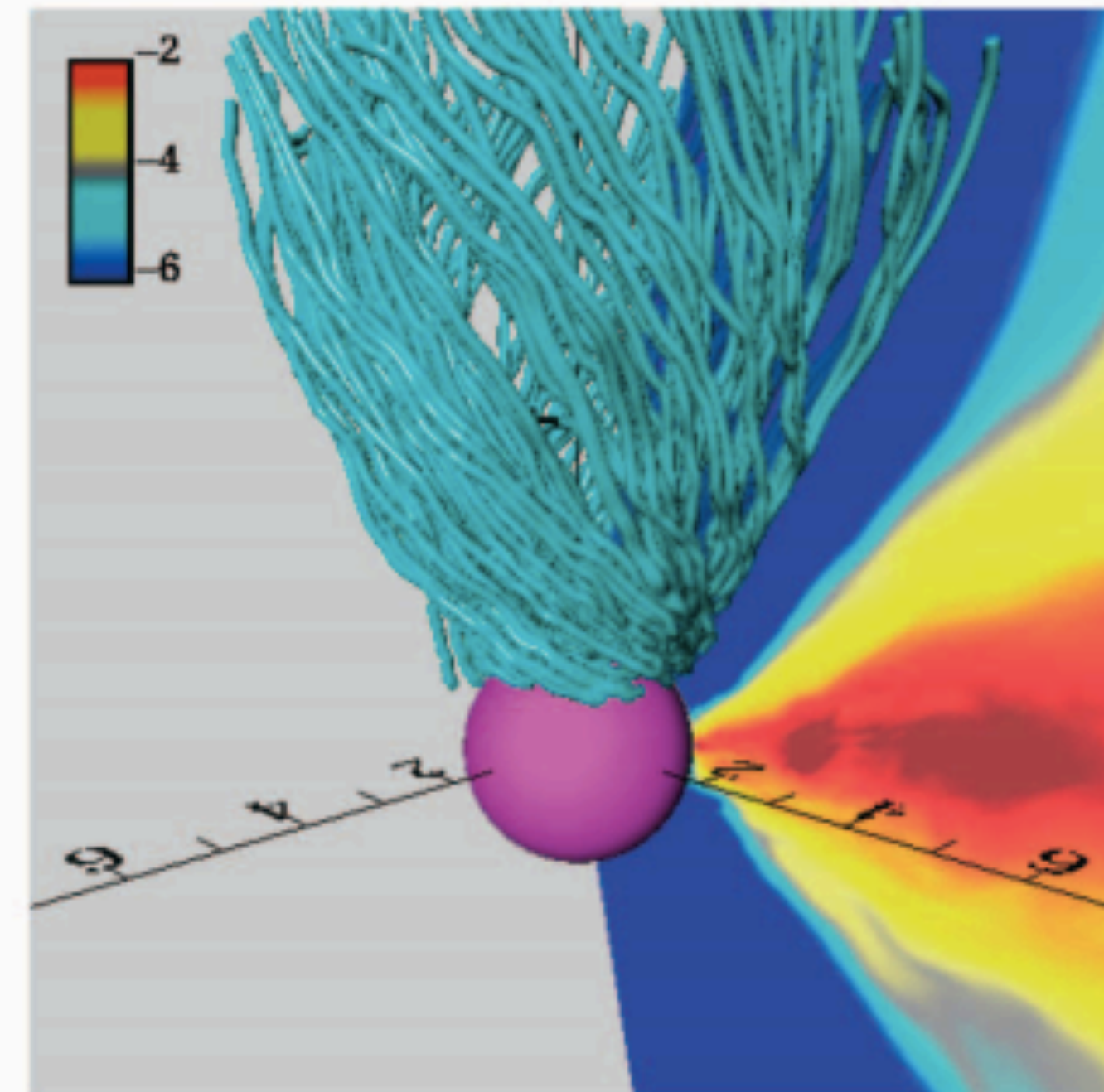
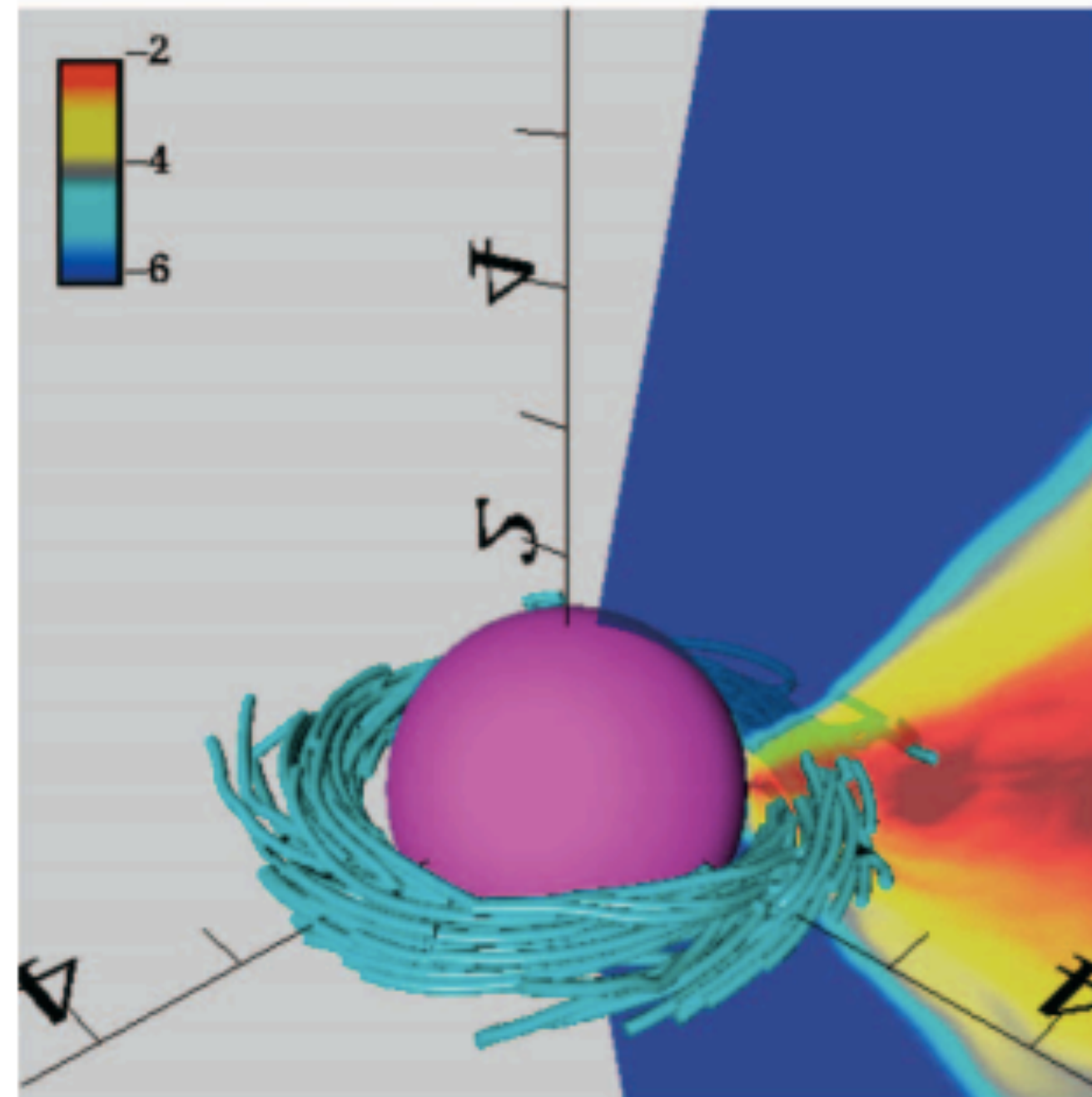
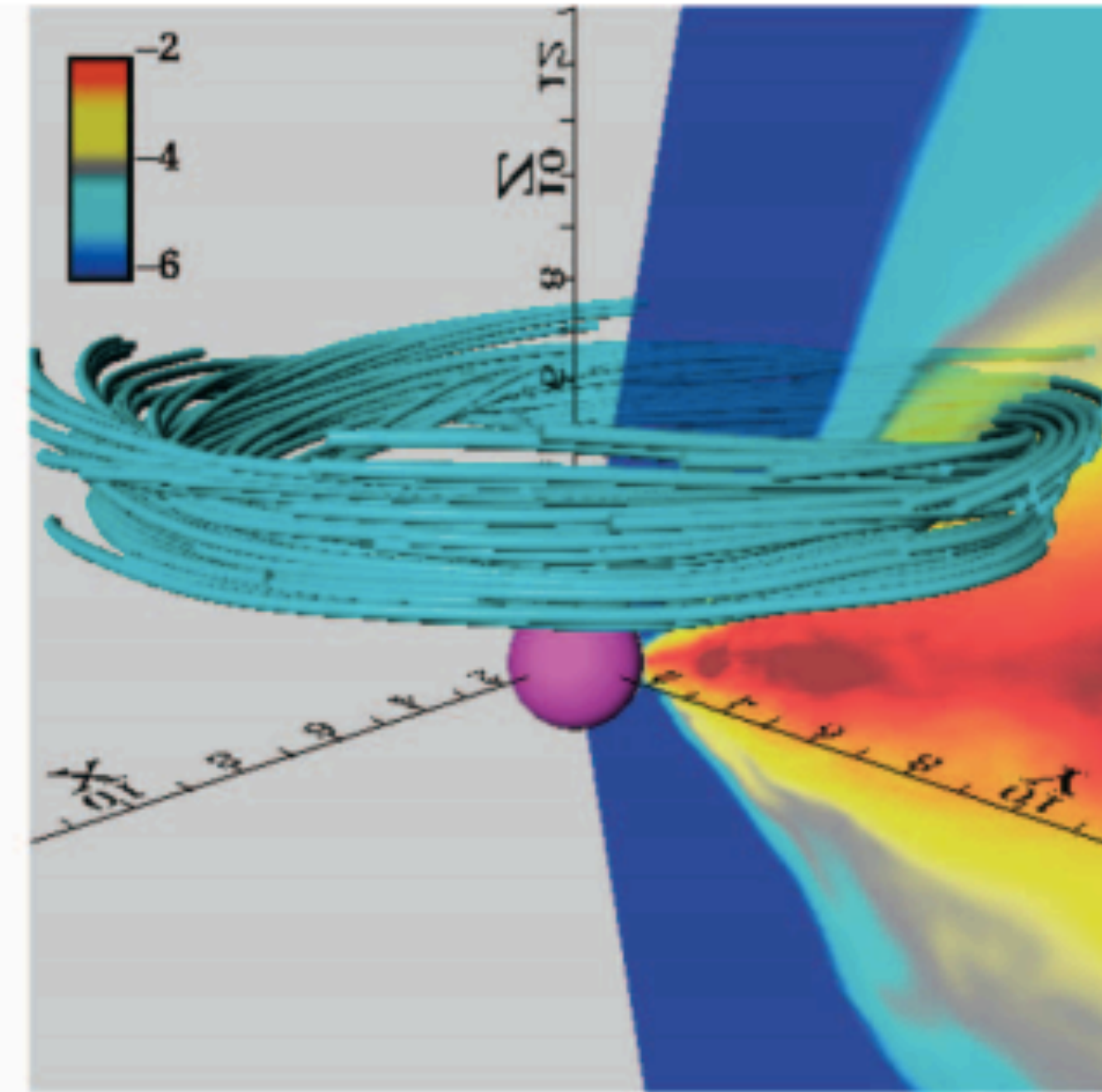
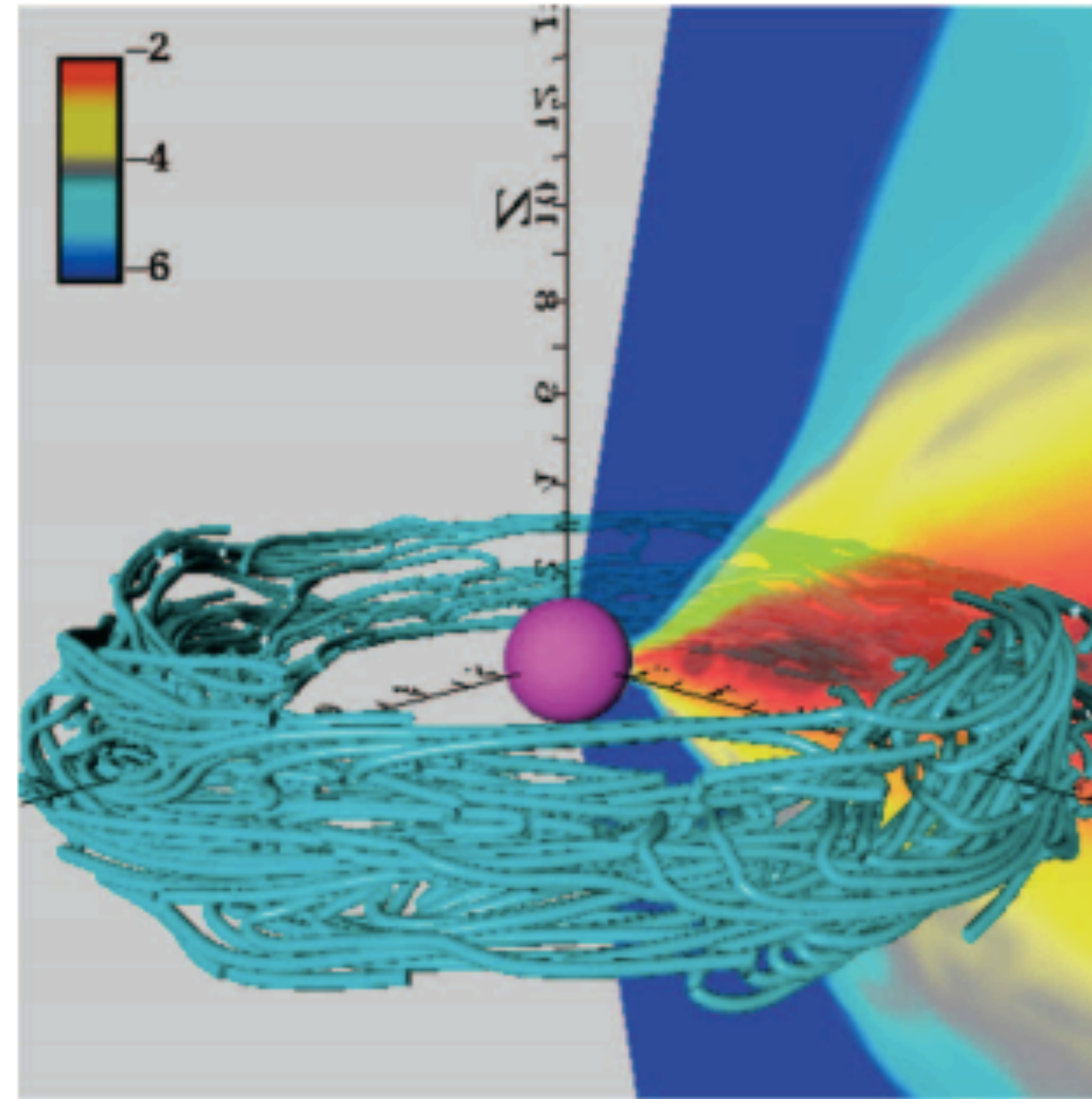
(scale unit: GM/c^2)

- approximation: just **ignore radiation!**
- **black hole mass** and **accretion rate** (or, alternatively, density unit) can be specified AFTER the simulation
- actively developed since ~ 2000
- starting from **one-fluid** simulation

initial magnetic field does matter

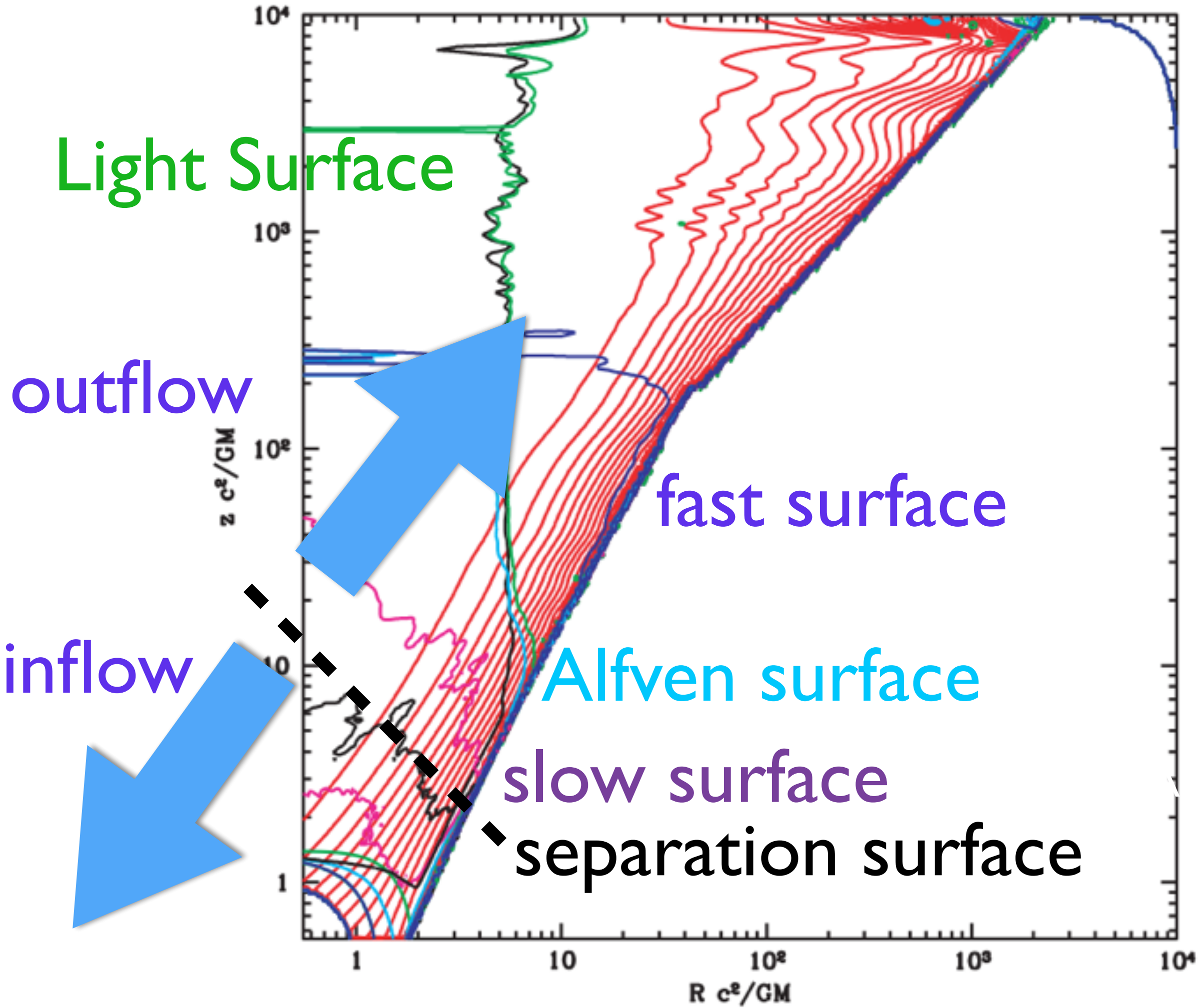
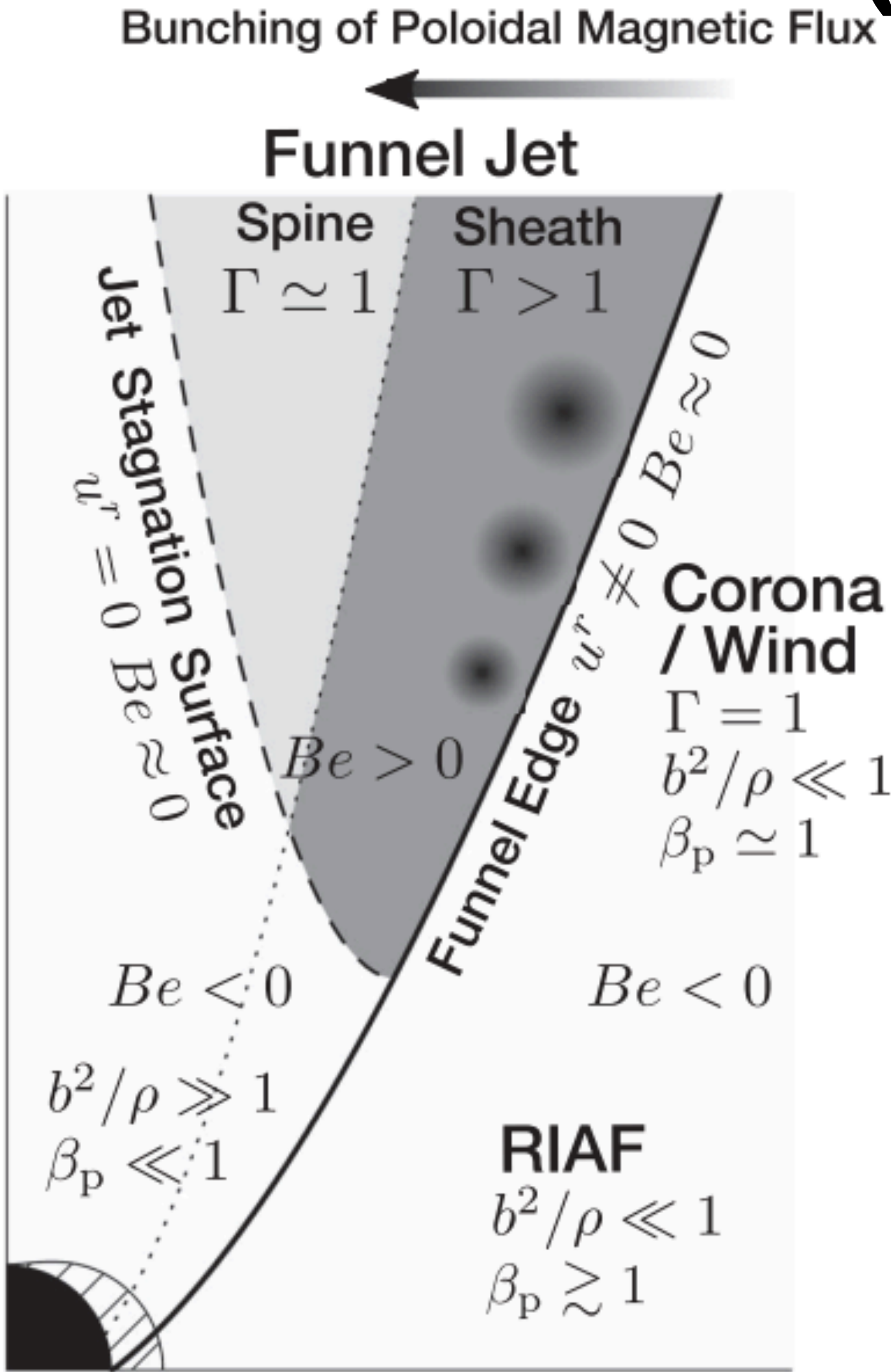


Hirose & Krolik
2003, 2004,
2005a, 2005b



$$\beta_p \equiv p_{\text{gas}}/p_{\text{mag}}$$

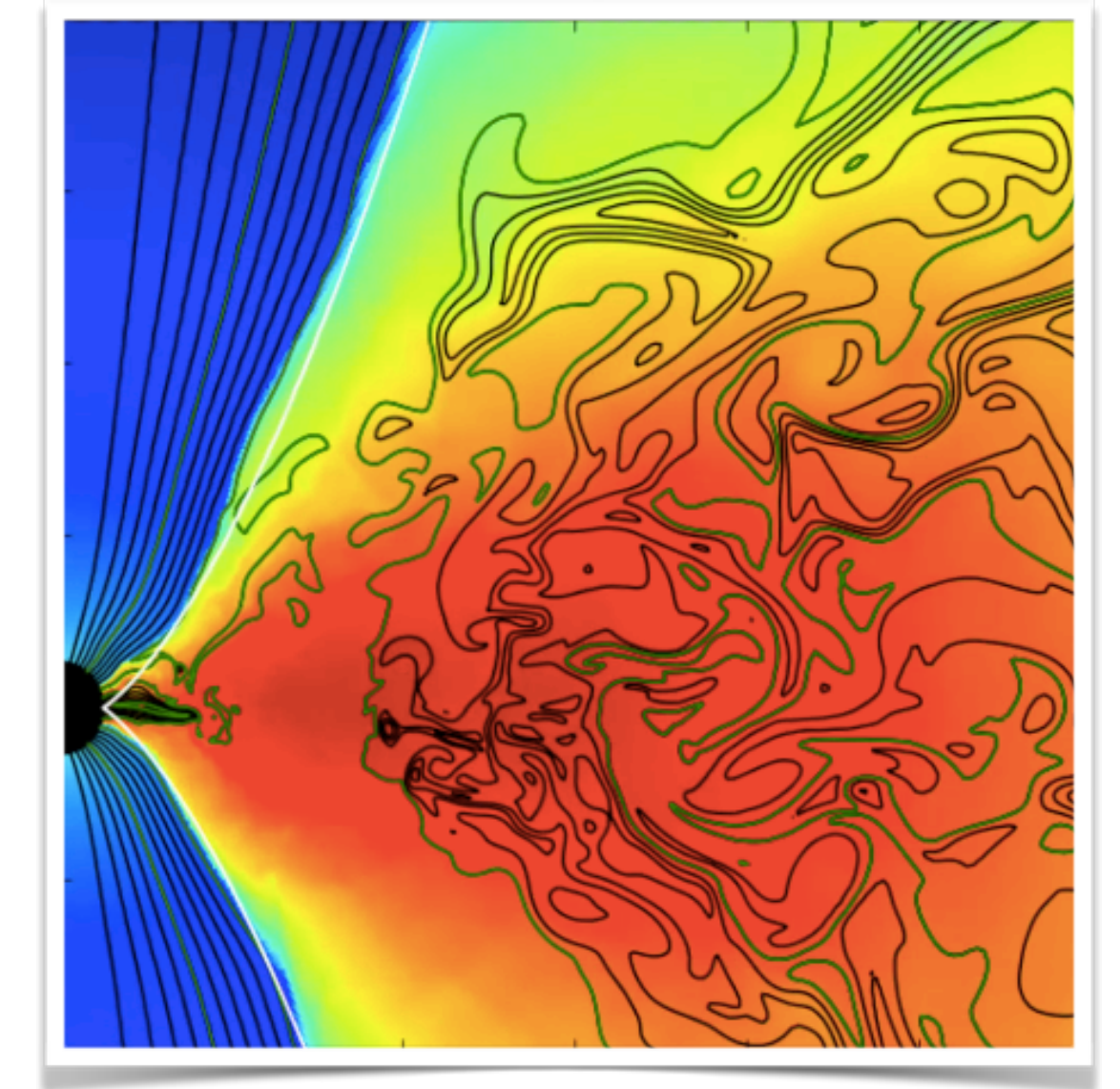
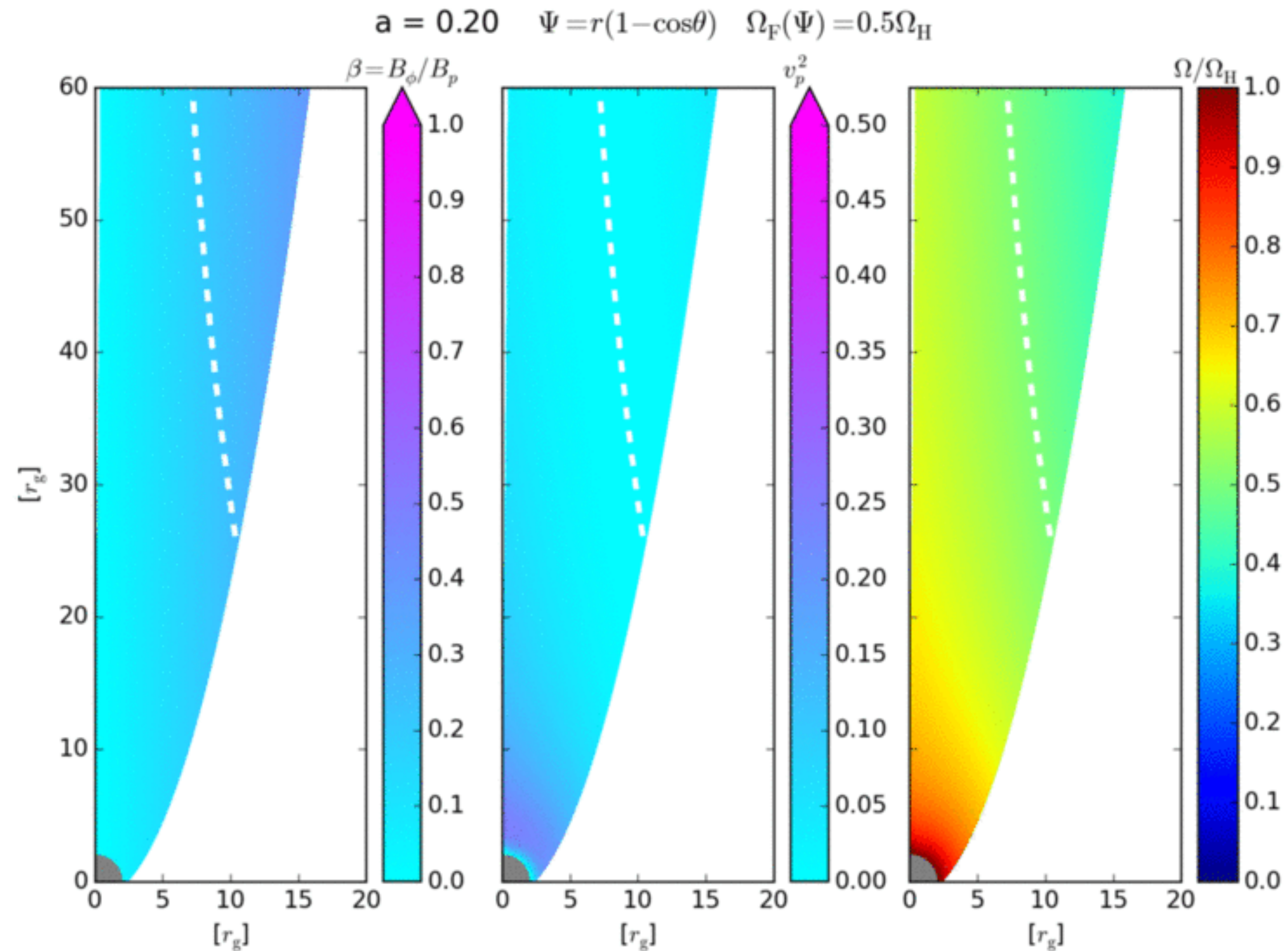
inflow and outflow share the same (large-scale) field line!



Nakamura+18 (see also Pu+ 15,20 for analytical approaches)

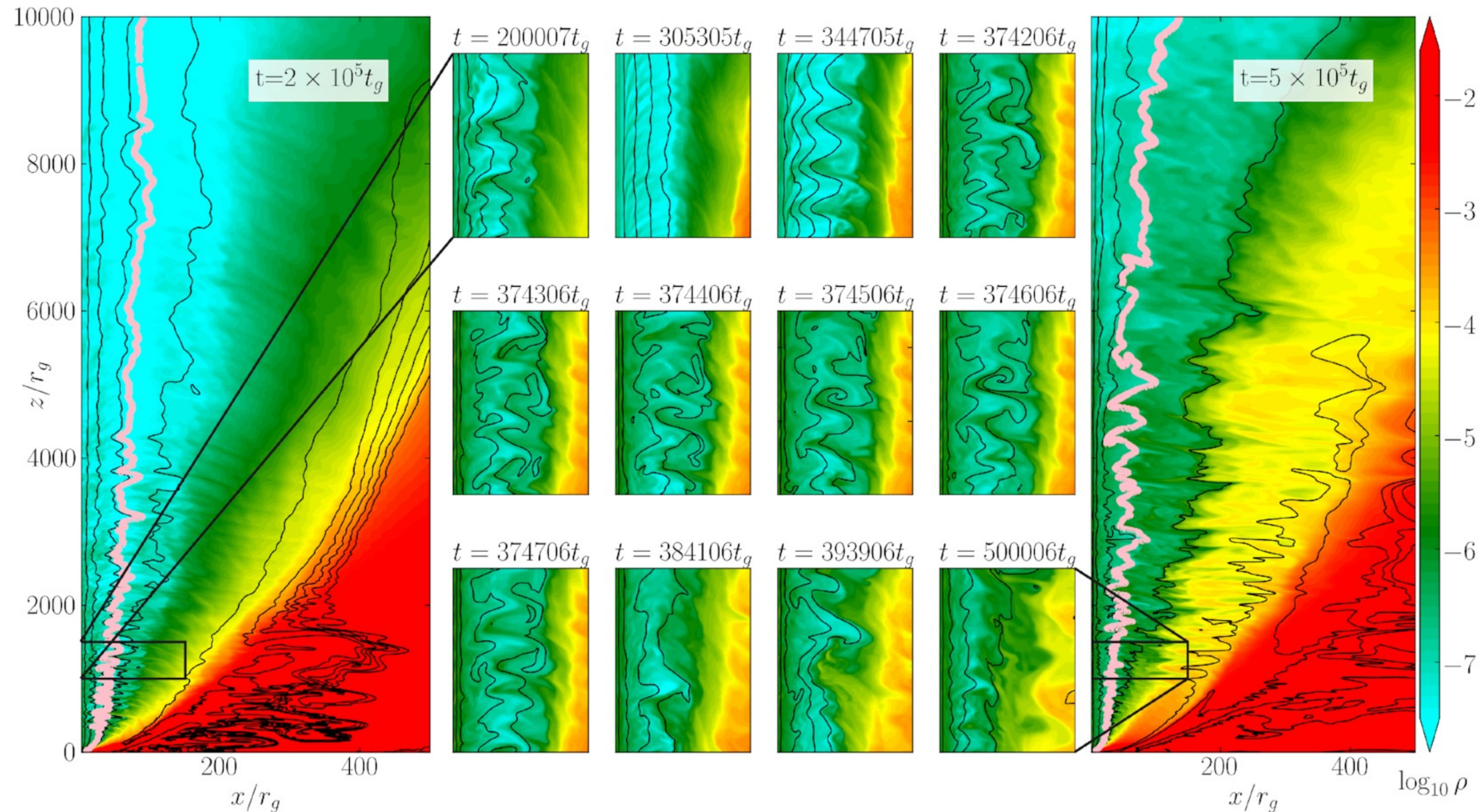
time-averaged GRMHD simulation result
 McKinney06

stagnation as function of BH spin



semi-analytical GRMHD jet model
by Pu & Takahashi 20

Mixing between the jet and the disc wind leads to mass loading of the jet



Chatterjee+ 19, by using GPU-accelerated GRMHD code H-AMR (Liska +18)

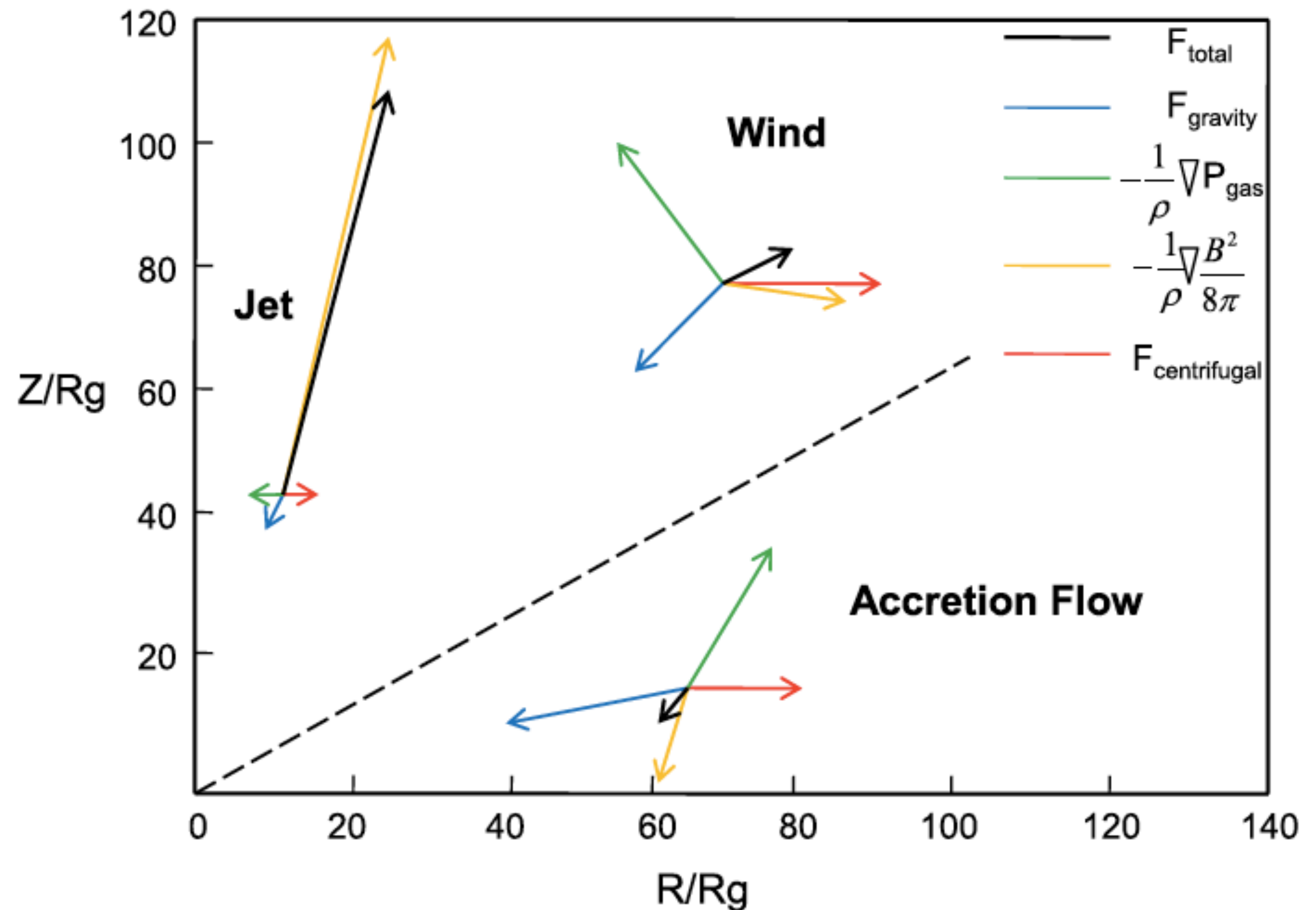
wind properties

wind from hot accretion:

$$\dot{M}_{\text{wind}} \propto \dot{M}_{\text{BH}} \times r^s$$
$$s \approx 1$$

Cheng-Yu's talk

Holger's talk

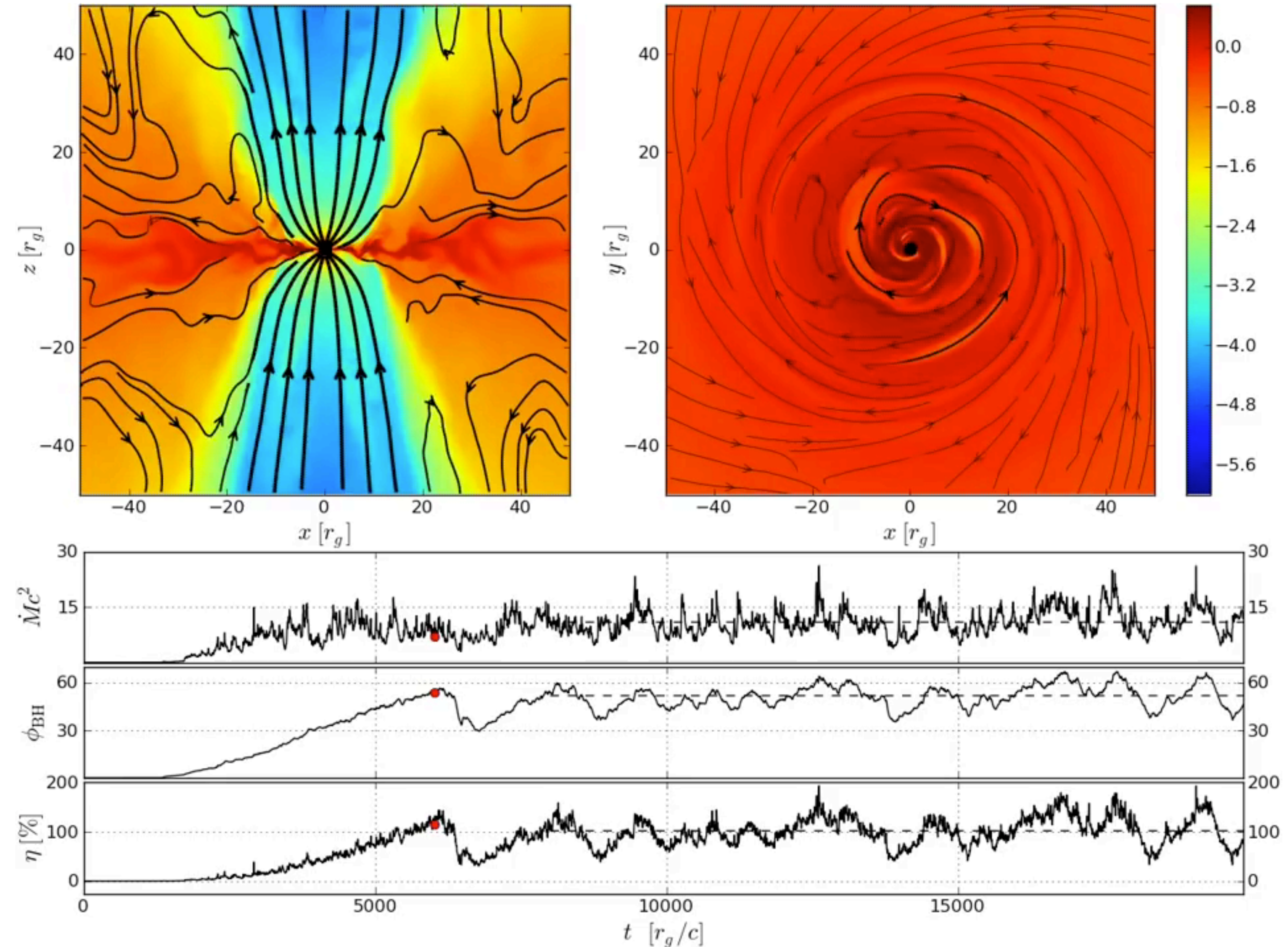


Yuan+15: 3D GRMHD simulation, $a=0$

$P_{\text{jet}} > P_{\text{acc}}$ for a fast-spinning black hole?

$$p^{BZ} \approx \Phi^2 a_*^2$$

$$\Phi \propto BM^2$$



more magnetic flux on black hole

upper limit

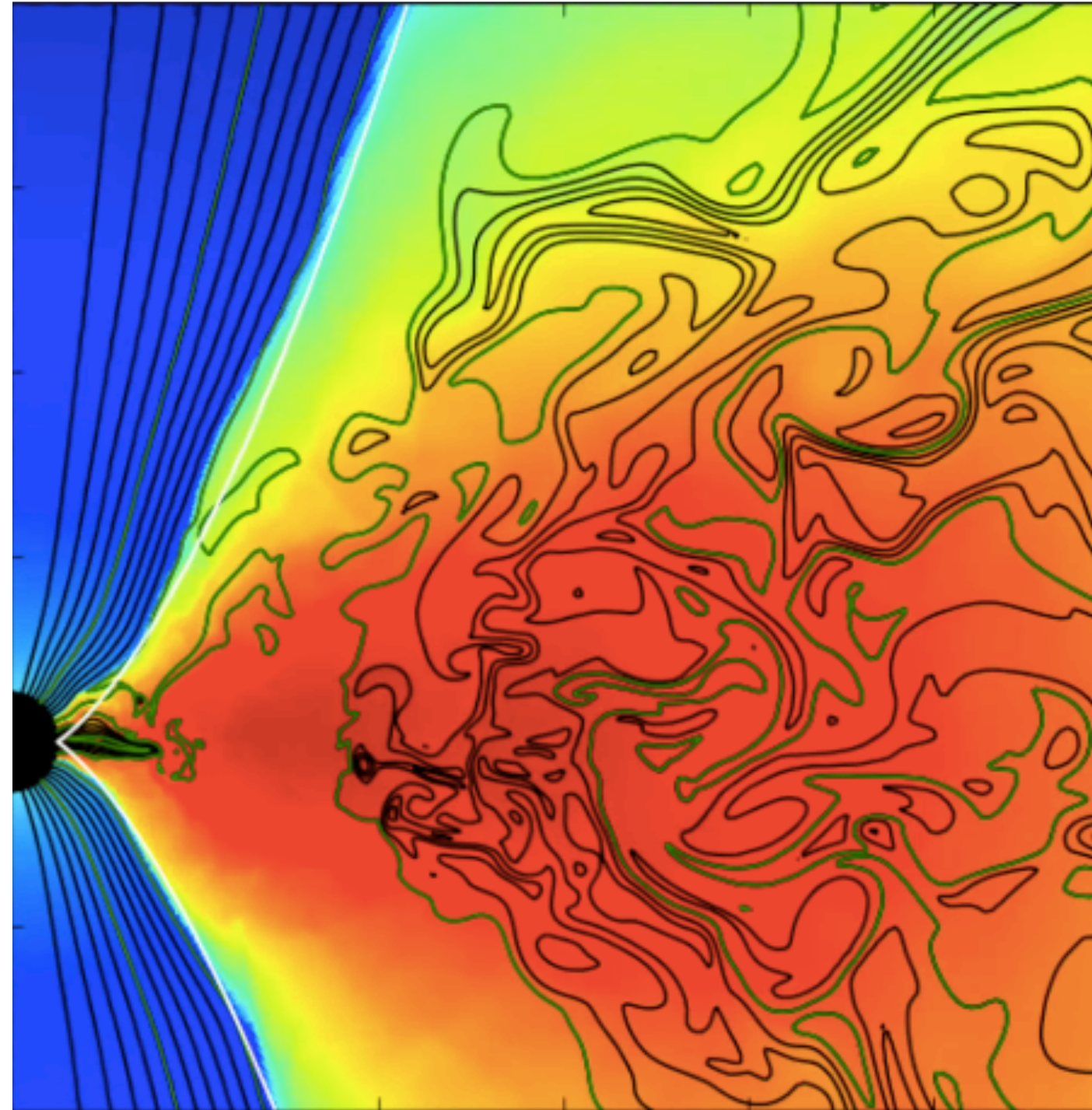
$$\phi \equiv \Phi_{\text{BH}} (\dot{M} R_g^2 c)^{-1/2}$$

$$\phi \sim 1$$

$$\phi \sim 50$$

SANE

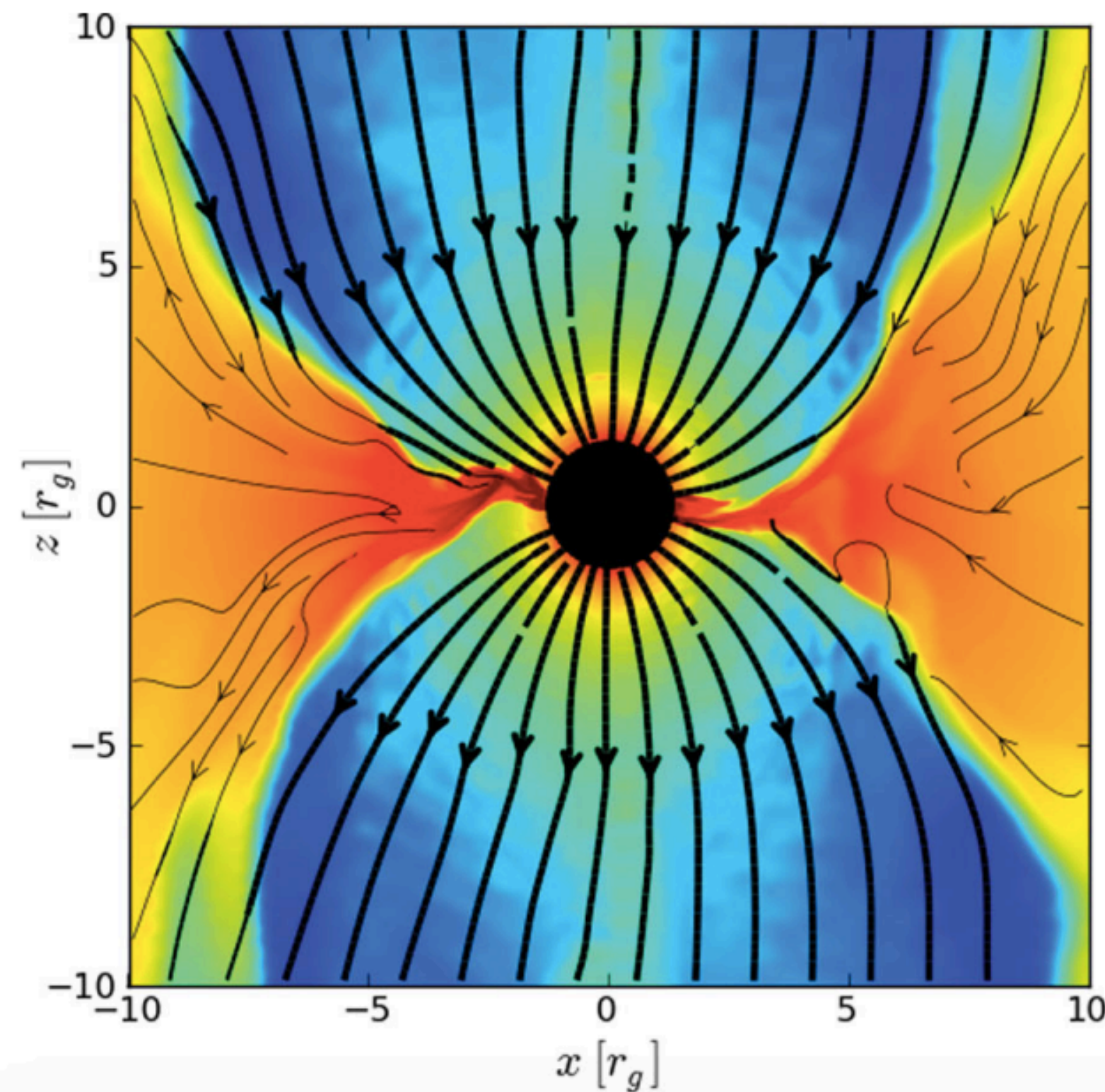
(Standard And Normal Evolution)



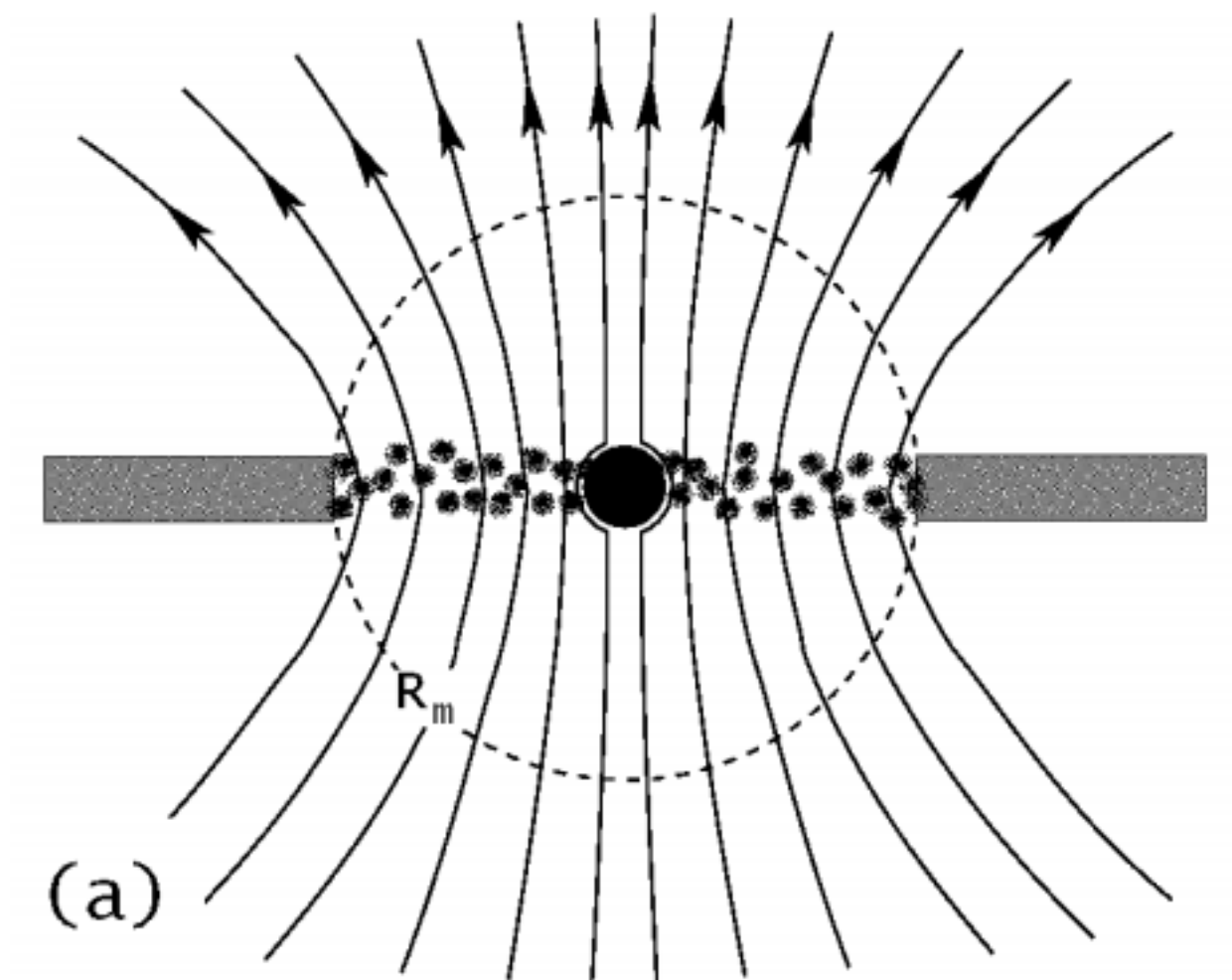
e.g. Narayan+12

MAD

(Magnetically Arrested Disk)



Narayan+03, Tchekhovskoy+11; McKinney+12



Narayan+03

linking simulations to **EHT observations** with known unknowns

**parameterize the
thermodynamics/electron
heating:**

$$T_i/T_e = R_{\text{high}} \frac{\beta_p^2}{1 + \beta_p^2} + \frac{1}{1 + \beta_p^2}$$

$$\beta_p \equiv p_{\text{gas}}/p_{\text{mag}}$$

Mościbrodzka et al (2016)

EHT paper V

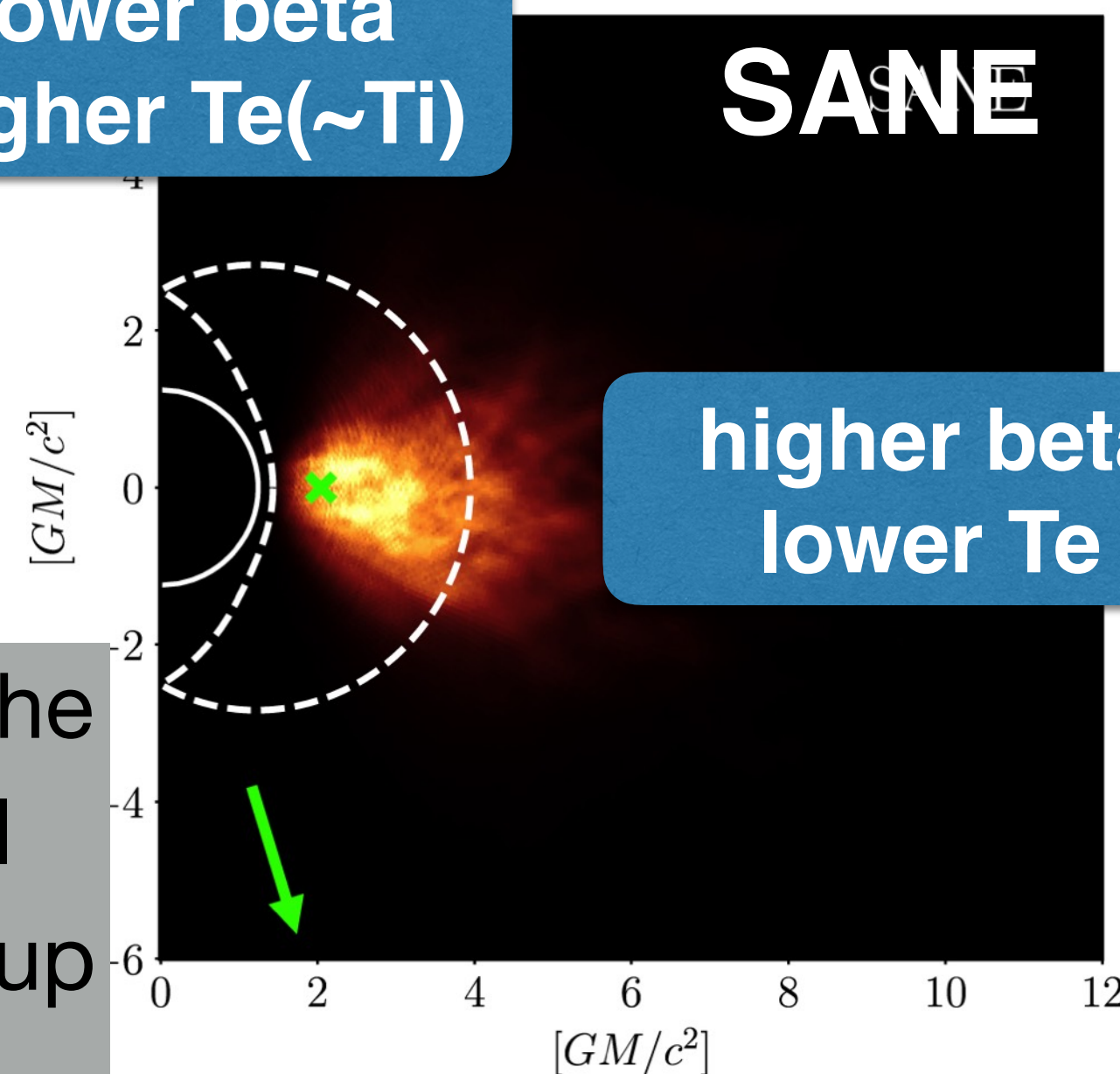
$R_{\text{high}} = 1, 10, 20, 40, 80, 160$

lower the T_e near the equatorial region

Binned location of the
point of origin for all
photons that make up
an image

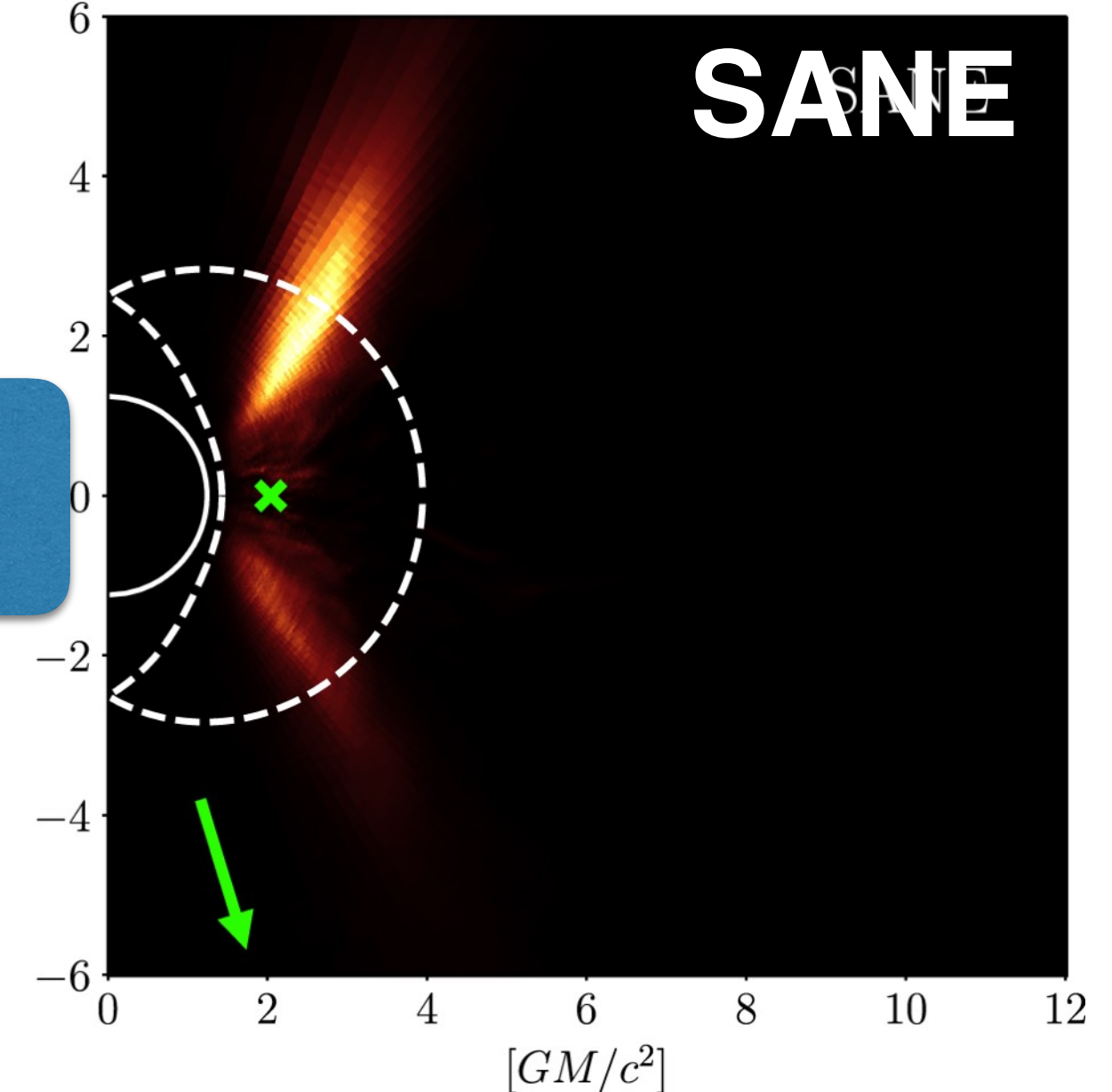
lower beta
higher $T_e(\sim T_i)$

SANE



higher beta
lower T_e

SANE



ps. non-thermal electrons is also important but ignored

beyond one-fluid approximation

two fluid
(ions + thermal electrons)

based on single-T flow via post-processing steps

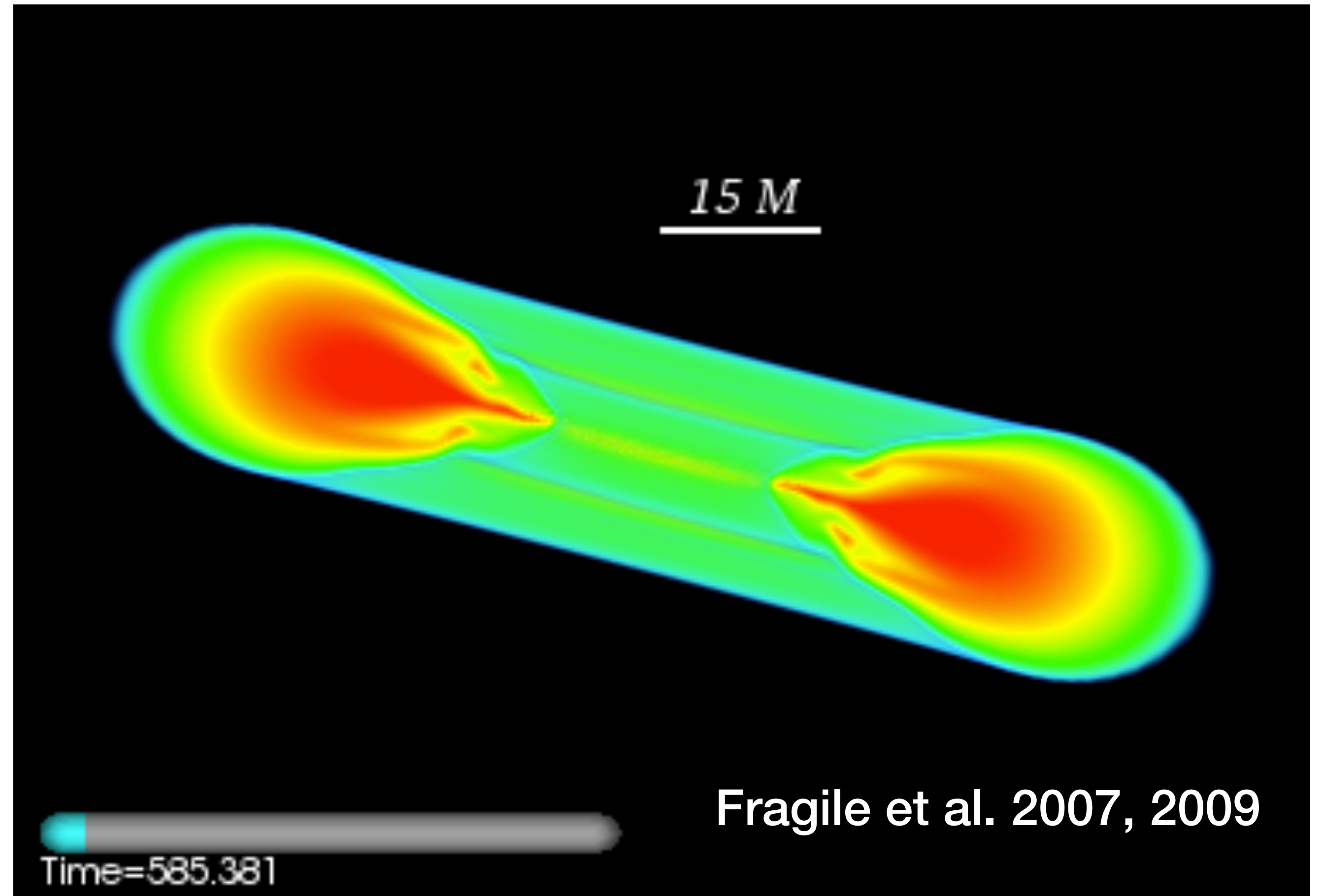
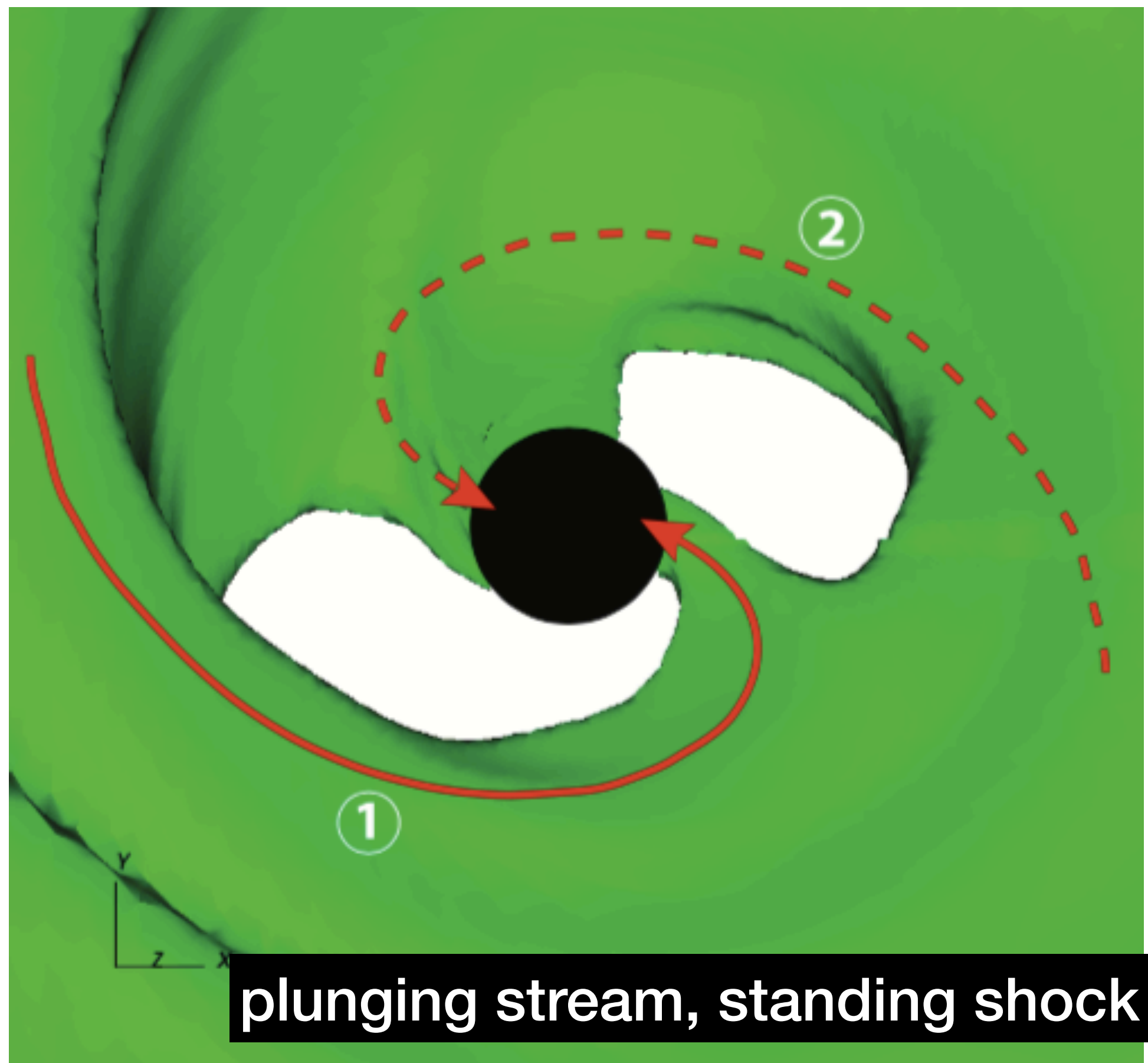
(Ressler et al. 2015, 2017)
(Ryan et al. 2017 GRRMHD:ebhlight)

independent two fluid
Sadowski et al. 2017 GRrMHD:KORAL

three fluid
**(ions + thermal electrons +
non thermal electrons)**

independent three fluid
Chael et al. 2017; GRrMHD:KORAL

Tilted disk



(see also Chatterjee+ 20)

Final Remarks

- what's interesting about BH accretion (on horizon-scale)?
 - (1) accretion type as function of accretion rate (related to plasma physics, energy equation)
 - (2) relativistic jet, winds (disk-jet coupling)
 - (1)+(2): physical origins of AGN feedback (if exist)
 - black hole spin, magnetic field matters: **simulation** brings surprises, **analytical model** brings insights; input from *microphysics* (*sub-grid physics*) needed cf. Karen's talk
 - other physics beyond horizon-scale: feedback, jet acceleration etc.
- with EHT (and LIGO/VIRGO/KAGRA), we are heading the **golden age of Black Hole Astrophysics** (in strong gravity regime!) cf. Yen-Chen's talk

★ Opportunities for all students in Taiwan!