Hidden Monopole Dark Matter via Axion Portal and its Implications for Direct Search and Beam-Dump Experiments

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Hidden monopole dark matter

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  - **It is an inevitable topological object if the universe experiences a phase transition in the hidden sector.**
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Can we detect the hidden monopole DM?

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Can we detect the hidden monopole DM?

No, at least in the minimum setup. One has to introduce certain couplings with the standard model (SM) sector.

Hidden monopole DM-SM interactions

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  - **Vector portal (strictly constrained by many exps. and obs.)**

    (c.f. Jaeckel & Ringwald, 2010)

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  - Higgs portal (expected scattering cross-section is very small)
    (c.f. Beak, Ko & Park, 2013)
  - Vector portal (strictly constrained by many exps. and obs.)
    (c.f. Jaeckel & Ringwald, 2010)
  - Axion portal ⟵ Our main interest
    (c.f. W. Fischler & J. Preskill '83)

't Hooft-Polyakov monopole

- It is known that a magnetic monopole can arise when a non-abelian gauge symmetry is spontaneously broken via the Higgs mechanism.

't Hooft, Polyakov '74

$$\mathrm{SU}(2)_{\mathrm{H}} + \boldsymbol{\phi} = (\phi_1, \phi_2, \phi_3)$$

$$\mathcal{L}_{\mathrm{H}} = -\frac{1}{4}\boldsymbol{F}_{\mathrm{H}}^{\mu\nu} \cdot \boldsymbol{F}_{\mathrm{H}\mu\nu} + \frac{1}{2}\mathcal{D}^{\mu}\boldsymbol{\phi} \cdot \mathcal{D}_{\mu}\boldsymbol{\phi} - \mathcal{V}(\phi)$$

$$\boldsymbol{F}_{\mathrm{H}}^{\mu\nu} = \partial^{\mu}\boldsymbol{A}_{\mathrm{H}}^{\nu} - \partial^{\nu}\boldsymbol{A}_{\mathrm{H}}^{\mu} + e_{\mathrm{H}}\boldsymbol{A}_{\mathrm{H}}^{\mu} \times \boldsymbol{A}_{\mathrm{H}}^{\nu}$$

$$\mathcal{D}^{\mu}\boldsymbol{\phi} = \partial^{\mu}\boldsymbol{\phi} + e_{\mathrm{H}}\boldsymbol{A}_{\mathrm{H}}^{\mu} \times \boldsymbol{\phi} \qquad \mathcal{V}(\phi) = \frac{1}{4}\lambda_{\phi}\left(\phi^2 - v_{\mathrm{H}}^2\right)^2$$

$\times$: products in the
$\cdot$ group space

hidden gauge coupling

vev of the scalar field

't Hooft-Polyakov monopole

- **Expand the Lagrangian density around the vacuum state**

$$\phi \to \phi + (0, 0, v_{\rm H}) \quad \longrightarrow \quad {\rm SU}(2)_{\rm H} \xrightarrow{\langle \phi \rangle} {\rm U}(1)_{\rm H}$$

- **Particle spectrum in the hidden sector** $\alpha_{\rm H} = e_{\rm H}^2/(4\pi)$
  - **Monopole is a soliton solution with finite energy configuration.**

Particle	Mass	Hidden electric charge	Hidden magnetic charge
$\gamma_{\rm H}$	0	0	0
φ	$m_\varphi = \sqrt{2\lambda_\phi}\, v_{\rm H}$	0	0
$W_{\rm H}^{\pm}$	$m_{W'} = \sqrt{4\pi\alpha_{\rm H}}\, v_{\rm H}$	$Q_{\rm E} = \pm e_{\rm H}$	0
${\rm M}(\overline{\rm M})$	$m_{\rm M} = \sqrt{4\pi/\alpha_{\rm H}}\, v_{\rm H}$	$Q_{\rm E} = \pm e_{\rm H}\theta_{\rm H}/(2\pi)$	$Q_{\rm M} = \pm 4\pi/e_{\rm H}$

The Witten effect

Witten '79

- **The theta term of hidden U(1) gauge symmetry**

$$\mathcal{L}_\theta = \theta_{\rm H} \frac{e_{\rm H}^2}{32\pi^2} F_{\rm H}^{\mu\nu} \widetilde{F}_{{\rm H}\mu\nu} = -\theta_{\rm H} \frac{e_{\rm H}^2}{8\pi^2} \boldsymbol{E}_{\rm H} \cdot \boldsymbol{B}_{\rm H}$$

  - **This term usually has no effect since it is a total derivative.**

The Witten effect

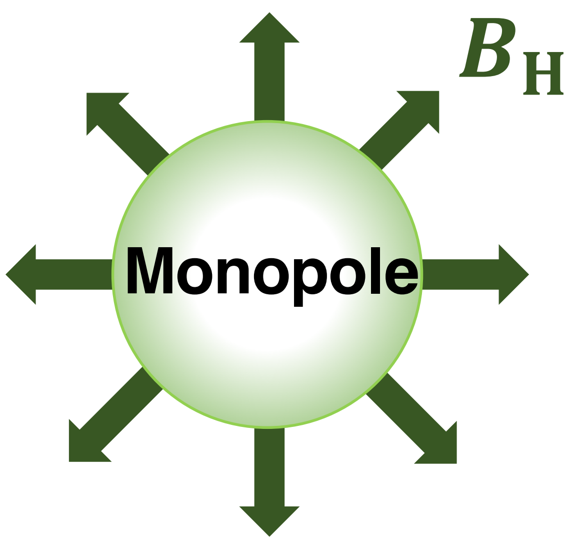
Witten '79

- **Hidden Maxwell's equation**

$F_{\rm H}^{j0} = E_{\rm H}^{j} \quad F_{\rm H}^{jk} = -\epsilon_{jkl} B_{\rm H}^{l}$

$$\partial_\mu F_{\rm H}^{\mu\nu} = \frac{e_{\rm H}^2}{8\pi^2} \partial_\mu \left(\theta_{\rm H} \widetilde{F}_{\rm H}^{\mu\nu} \right) \longrightarrow \nabla \cdot \boldsymbol{E}_{\rm H} = \frac{e_{\rm H}^2}{8\pi^2} \nabla \cdot \left(\theta_{\rm H} \boldsymbol{B}_{\rm H} \right)$$

- **This term usually has no effect since it is a total derivative. However, it has physical effect in the monopole background.**



$$Q_{\rm M} = \pm \frac{4\pi}{e_{\rm H}}$$

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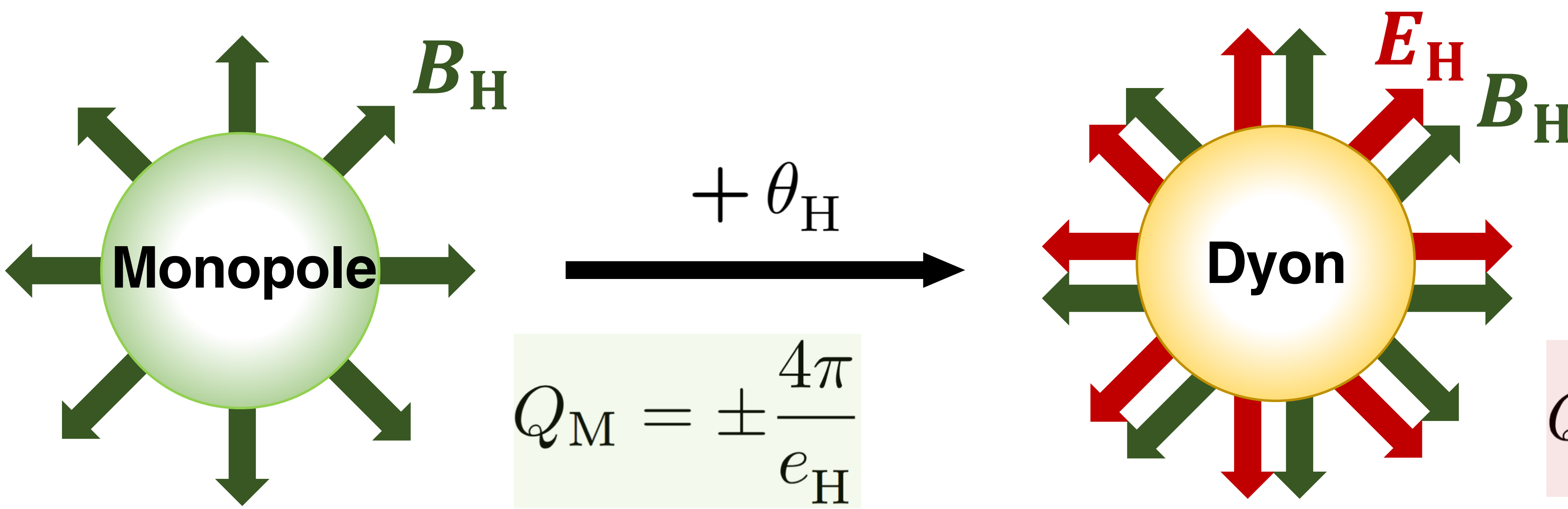


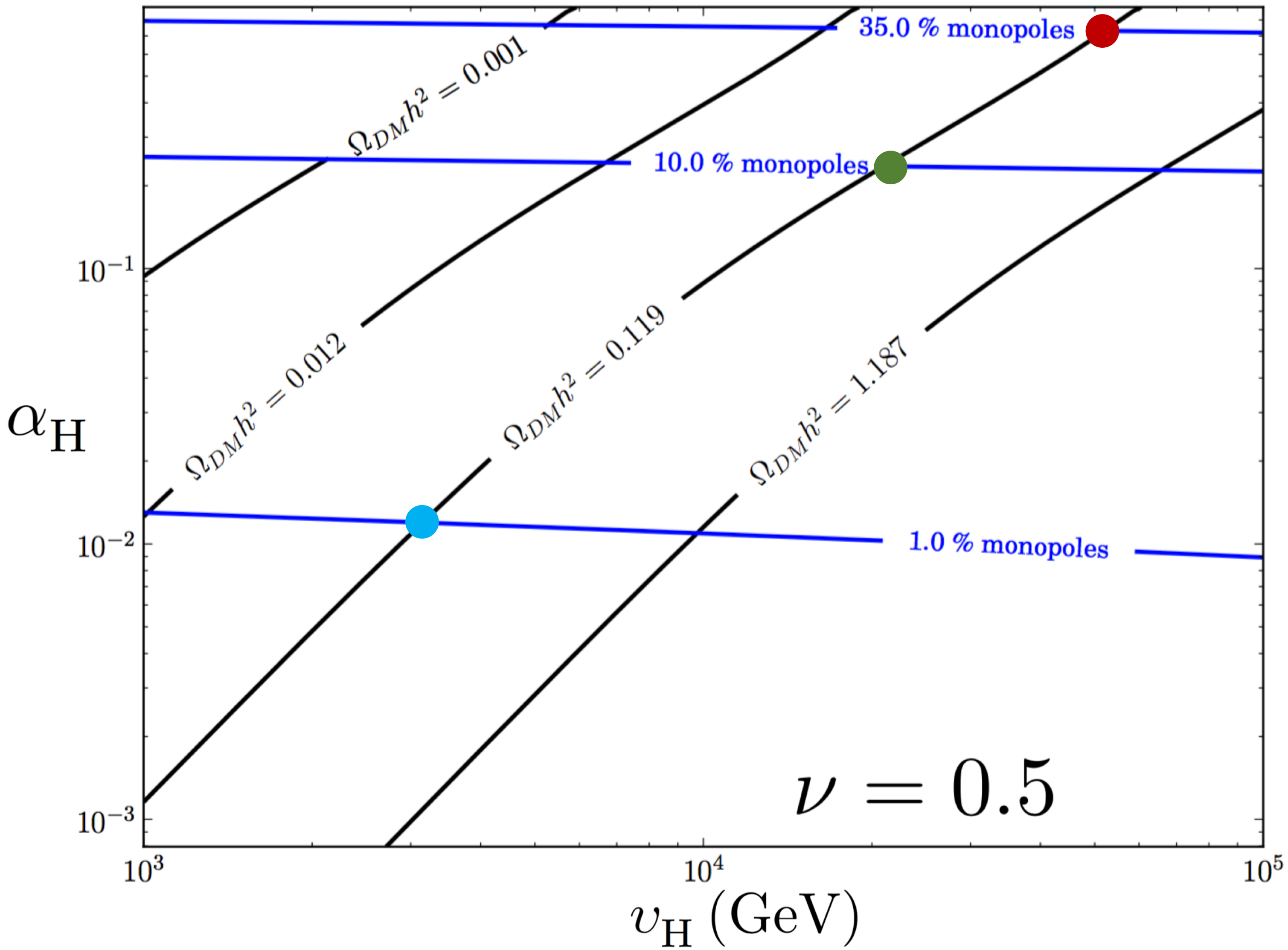
$$Q_{\mathrm{M}} = \pm\frac{4\pi}{e_{\mathrm{H}}}$$

$$Q_{\mathrm{E}} = \pm\frac{e_{\mathrm{H}}\theta_{\mathrm{H}}}{2\pi}$$

Benchmark point

■ Combined relic abundance of DM

Khoze & Ro 2014



$$m_{\rm M} = \sqrt{4\pi/\alpha_{\rm H}}\, v_{\rm H}$$

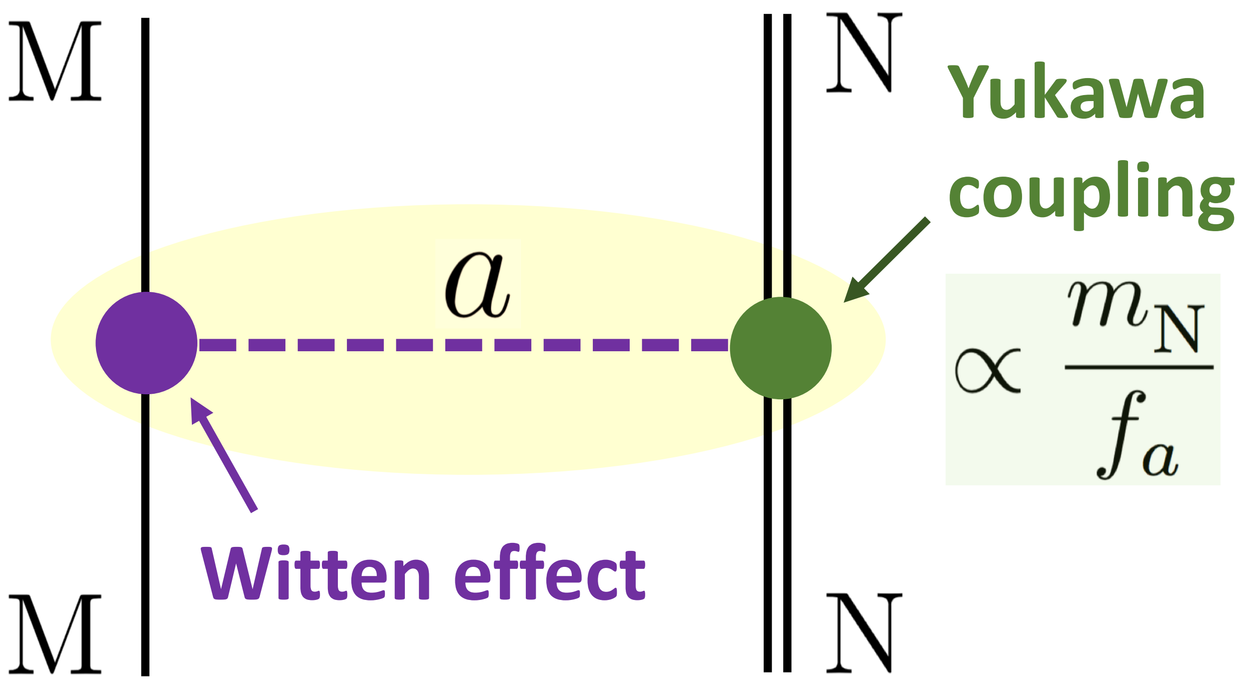
- ● ~ 2.2*10^5 GeV
- ● ~ 1.5*10^5 GeV
- ● ~ 1.0*10^5 GeV

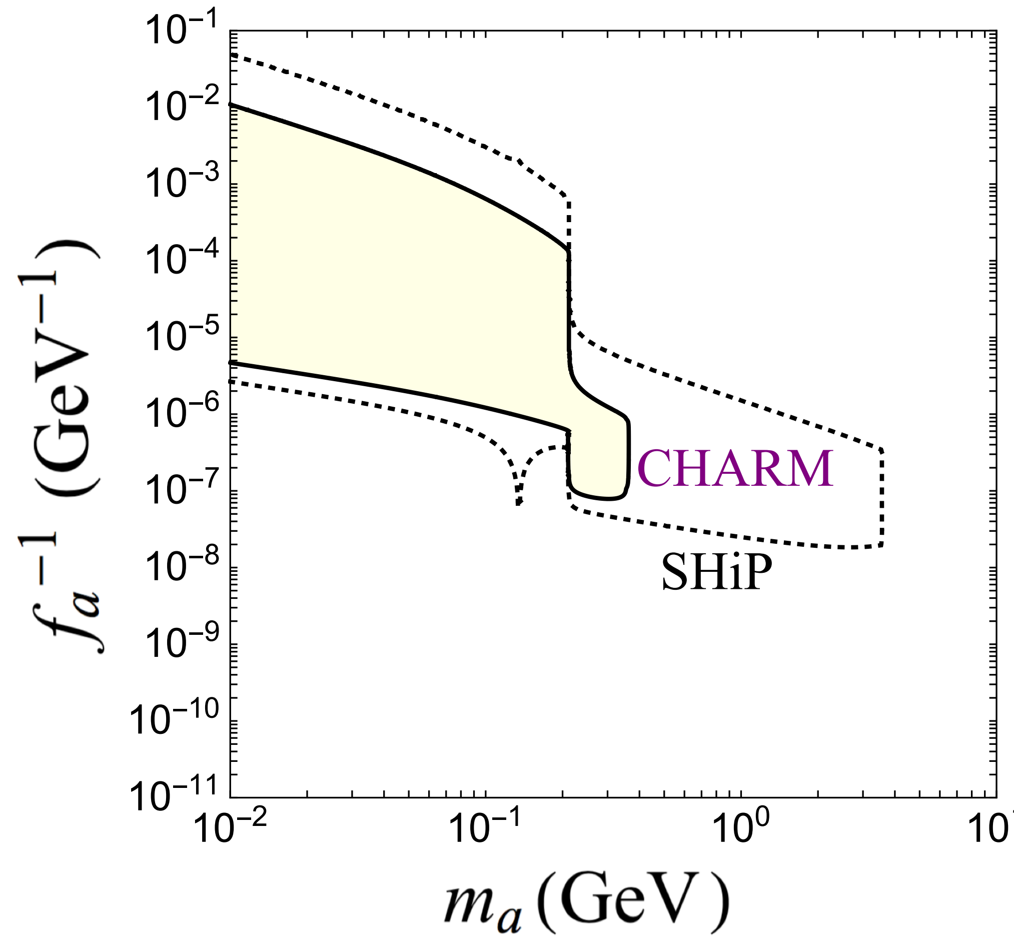
35% hidden monopole DM

$$\alpha_{\rm H} \simeq 0.73$$
$$m_{\rm M} \simeq 216\ {\rm TeV}$$

What we did

- **Axion portal coupling + Yukawa interaction**





Direct detection searches **Beam-dump experiments**

Axion portal coupling

- **Lagrangian density**

$$\mathcal{L} = -\frac{1}{4}F_{\rm H}^{\mu\nu}F_{{\rm H}\mu\nu} + \frac{1}{2}f_a^2\partial^\mu\theta\partial_\mu\theta - \frac{1}{2}m_a^2 f_a^2(\theta-\theta_0)^2 + \theta\frac{e_{\rm H}^2}{32\pi^2}F_{\rm H}^{\mu\nu}\widetilde{F}_{{\rm H}\mu\nu}$$

(c.f. W. Fischler & J. Preskill 83')

$$F_{\rm H}^{\mu\nu} = \partial^\mu A_{\rm H3}^\nu - \partial^\nu A_{\rm H3}^\mu$$

$$\theta \equiv a/f_a$$

- **Equation of motion of the axion field**

$$\frac{d^2\theta}{dr^2} + \frac{2}{r}\frac{d\theta}{dr} - \left(m_a^2 + \frac{r_0^2}{r^4}\right)\theta + m_a^2\theta_0 = 0$$

$$r_0 = \frac{e_{\rm H}}{8\pi^2 f_a}$$

- **Boundary conditions :** $\theta(r\to 0) = 0\ ,\quad \theta(r\to\infty) = \theta_0$

The total energy density of the axion-monopole system must be finite.

Axion portal coupling

- **Equation of motion of the axion field**

$$\frac{d^2\theta}{dr^2} + \frac{2}{r}\frac{d\theta}{dr} - \left(m_a^2 + \frac{r_0^2}{r^4}\right)\theta + m_a^2\theta_0 = 0 \qquad r_0 = \frac{e_{\mathrm{H}}}{8\pi^2 f_a}$$

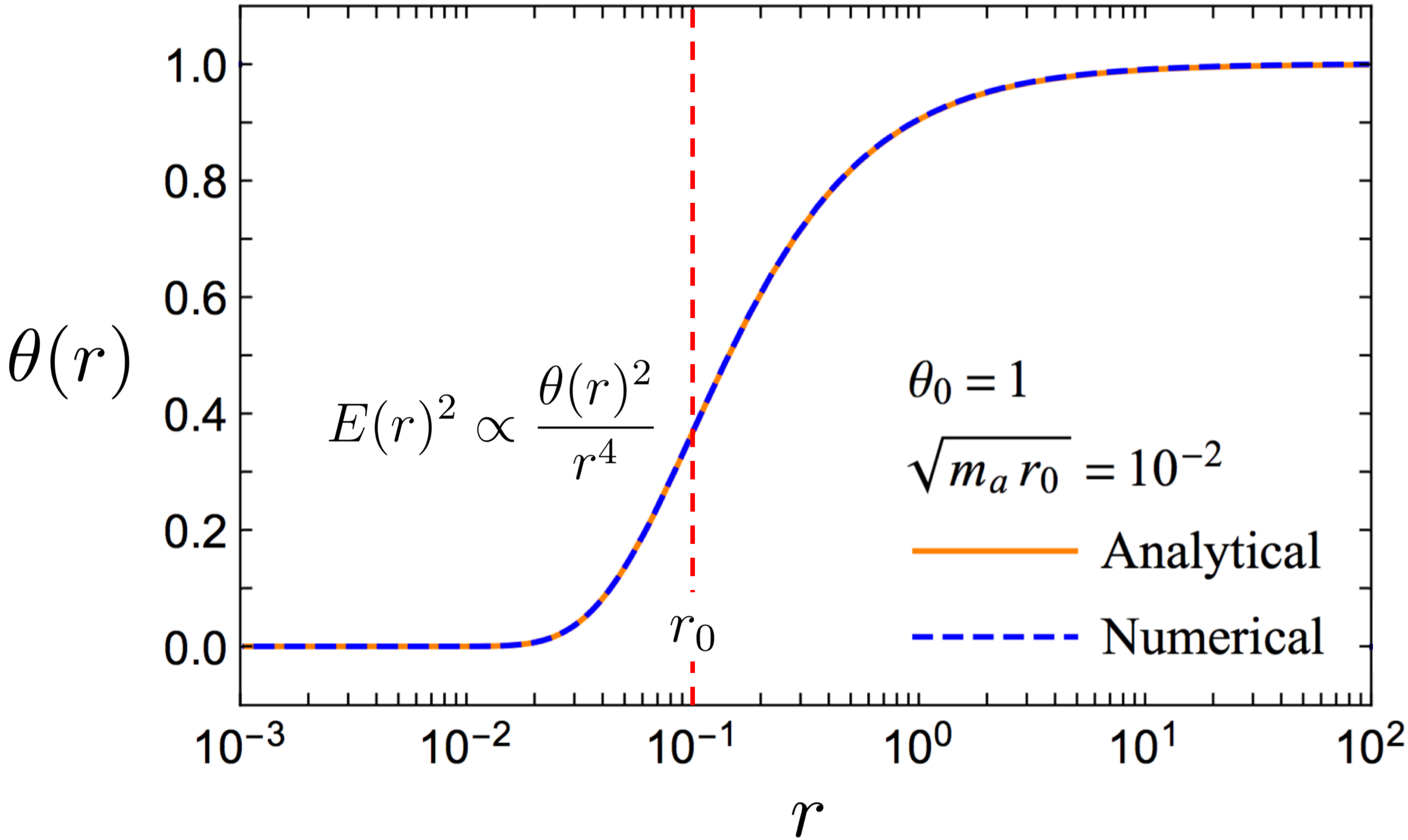
  - **Boundary conditions :** $\theta(r \to 0) = 0 \,, \quad \theta(r \to \infty) = \theta_0$

  - **This differential equation can be solved asymptotically.**

$$\theta(z) \simeq \begin{cases} \theta_+(z) \equiv \theta_0 \left(\dfrac{1+\sqrt{m_a r_0}}{1+2\sqrt{m_a r_0}}\right) e^{-z+\sqrt{m_a r_0}} & \text{for} \quad z > \sqrt{m_a r_0} \\ \theta_-(z) \equiv \theta_0 \left(1 - \dfrac{z}{1+2\sqrt{m_a r_0}} e^{-m_a r_0/z+\sqrt{m_a r_0}}\right) & \text{for} \quad z < \sqrt{m_a r_0} \end{cases}$$

$$\theta_+\left(\sqrt{m_a r_0}\right) = \theta_-\left(\sqrt{m_a r_0}\right)$$

Axion profile around the monopole



Hidden monopole-nucleon scattering

- **Axion-nucleon interaction (Yukawa coupling)**

$$H_{a-\mathrm{N}} = \frac{C_{\mathrm{N}} m_{\mathrm{N}}}{f_a} \int d^3x \left[a(x) \overline{\psi}_{\mathrm{N}}(x) i\gamma^5 \psi_{\mathrm{N}}(x) \right]$$

- **Amplitude of the hidden monopole-nucleon scattering**

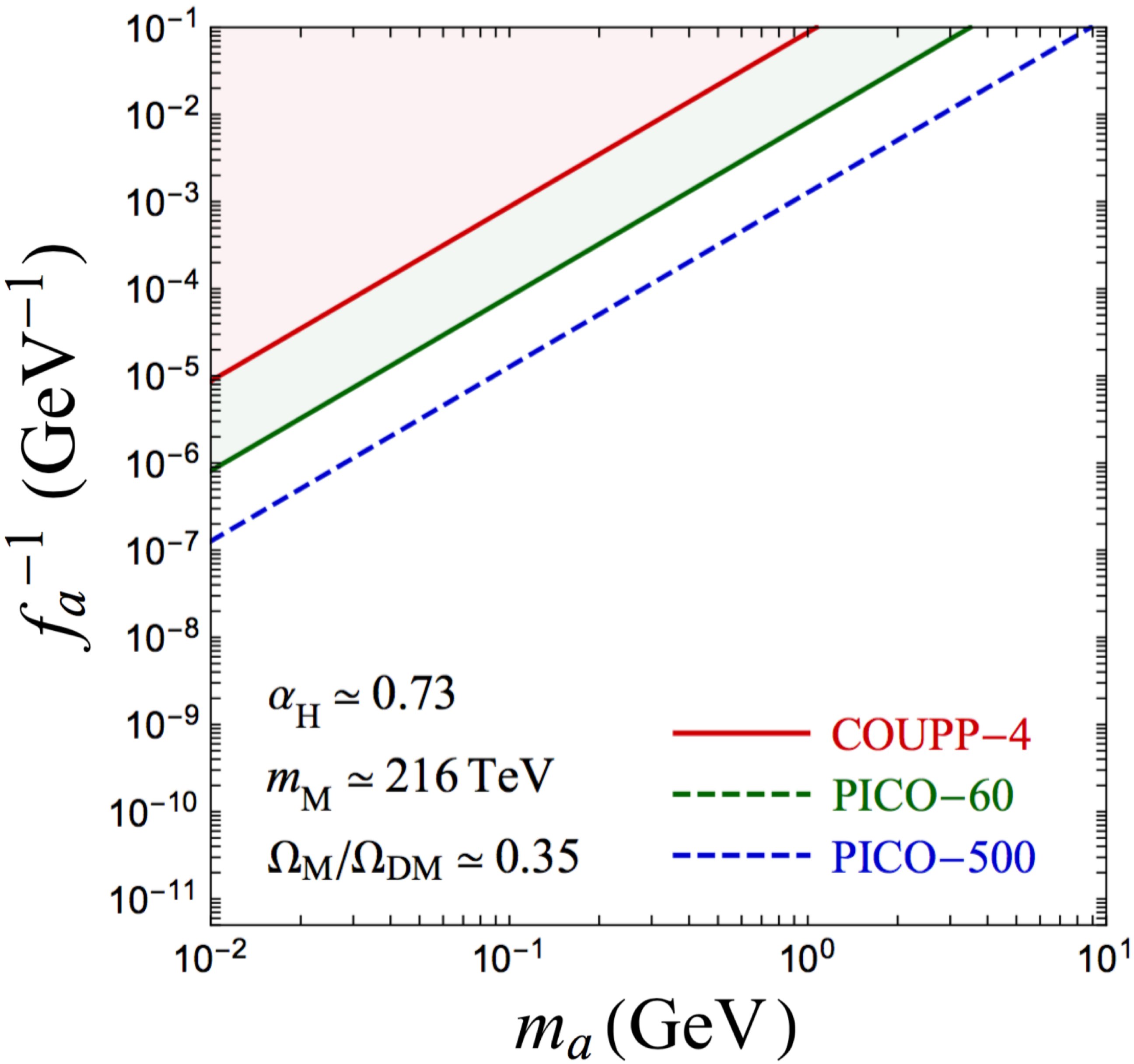
$$i\mathcal{M}_{\mathrm{M+N \to M+N}} = C_{\mathrm{N}} m_{\mathrm{N}} \, \overline{u}_{\mathrm{N}}(p') \gamma^5 u_{\mathrm{N}}(p) \int d^3x \, \boxed{\theta(\mathbf{x})} \, e^{-i\boldsymbol{q}\cdot\mathbf{x}}$$

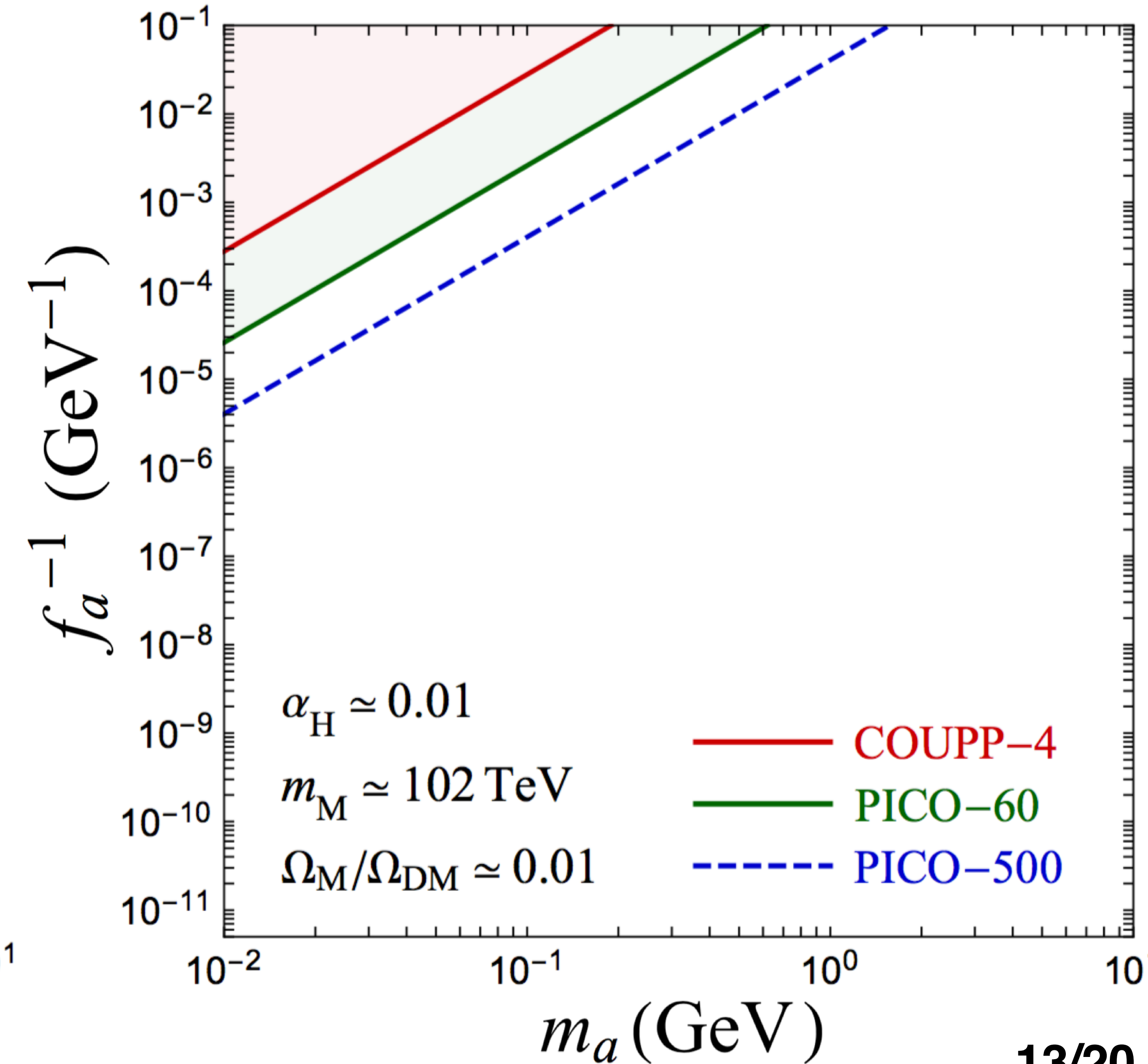
Axion profile

- **Spin-dependent cross-section**

$$\frac{d\sigma_{\mathrm{M+N \to M+N}}}{d\Omega} \simeq \frac{\alpha_{\mathrm{H}} \theta_0^2 C_{\mathrm{N}}^2}{16\pi^3} \frac{m_{\mathrm{N}}^2}{m_a^4 f_a^2} |\boldsymbol{q}|^2 \qquad \boldsymbol{q} = \boldsymbol{p}' - \boldsymbol{p}$$

Direct search exps. : m_a vs f_a^{-1}





Axion decay channels

- **Hidden photon decay channel**
  - **In our model, the axion can decay into the hidden photons**

$$\mathcal{L} = \frac{\alpha_{\rm H}}{8\pi}\frac{a}{f_{\rm H}} F_{\rm H}^{\mu\nu}\widetilde{F}_{{\rm H}\mu\nu} \longrightarrow \Gamma(a \to \gamma_{\rm H}\gamma_{\rm H}) = \frac{\alpha_{\rm H}^2 m_a^3}{256\pi^3 f_{\rm H}^2}$$

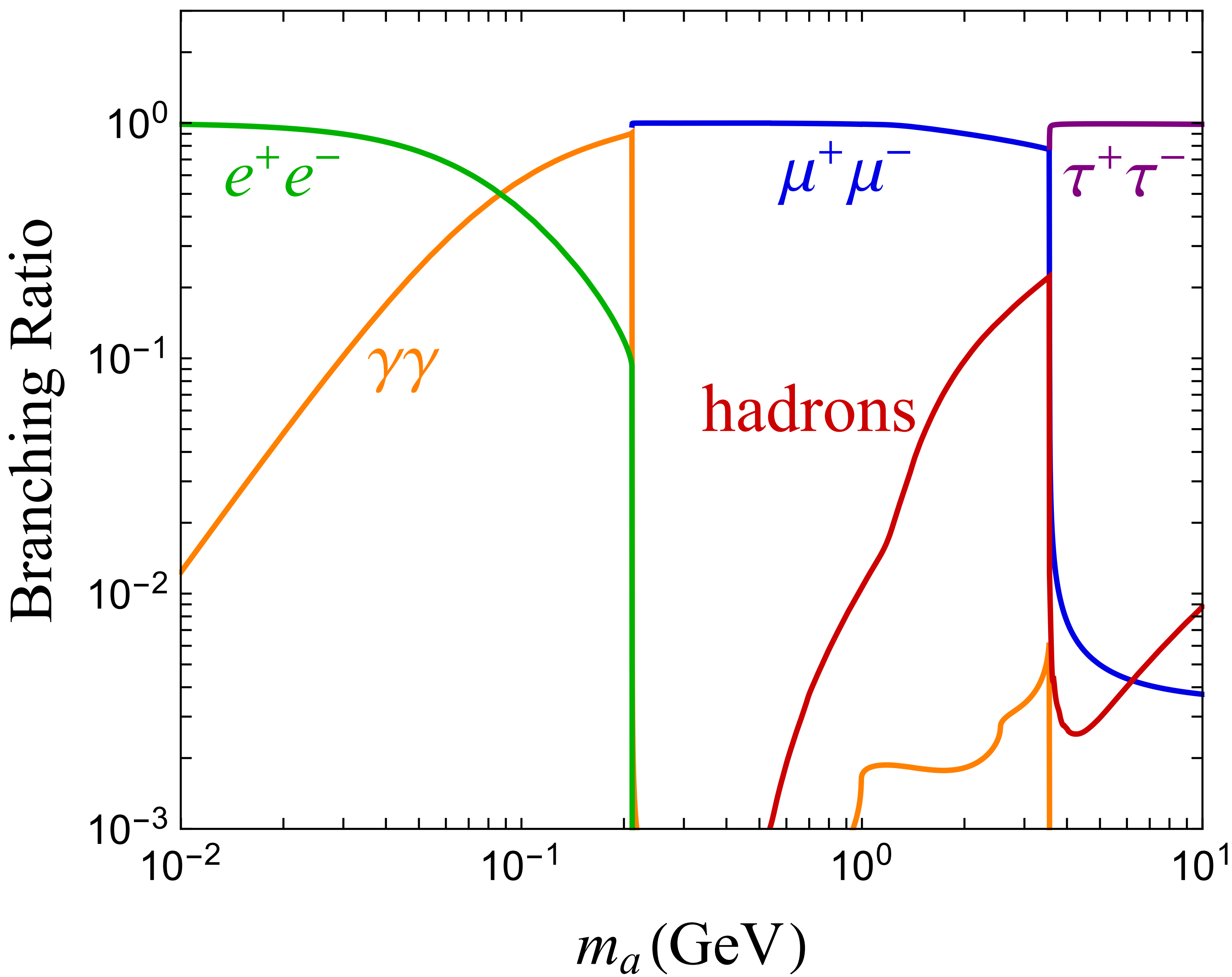
- **Fermion & photon decay channels**
  - **We assume Yukawa-like coupling for the axion**

$$\mathcal{L} = \sum_f \frac{m_f}{f_a} a\bar{f}i\gamma^5 f \longrightarrow$$

$$\Gamma(a \to f^+f^-) = \frac{m_a m_f^2}{8\pi f_a^2}\sqrt{1-\frac{4m_f^2}{m_a^2}}$$

$$\Gamma(a \to \gamma\gamma) \simeq \frac{\alpha^2 m_a^3}{256\pi^3 f_a^2}$$

Axion decay channels without γ_H

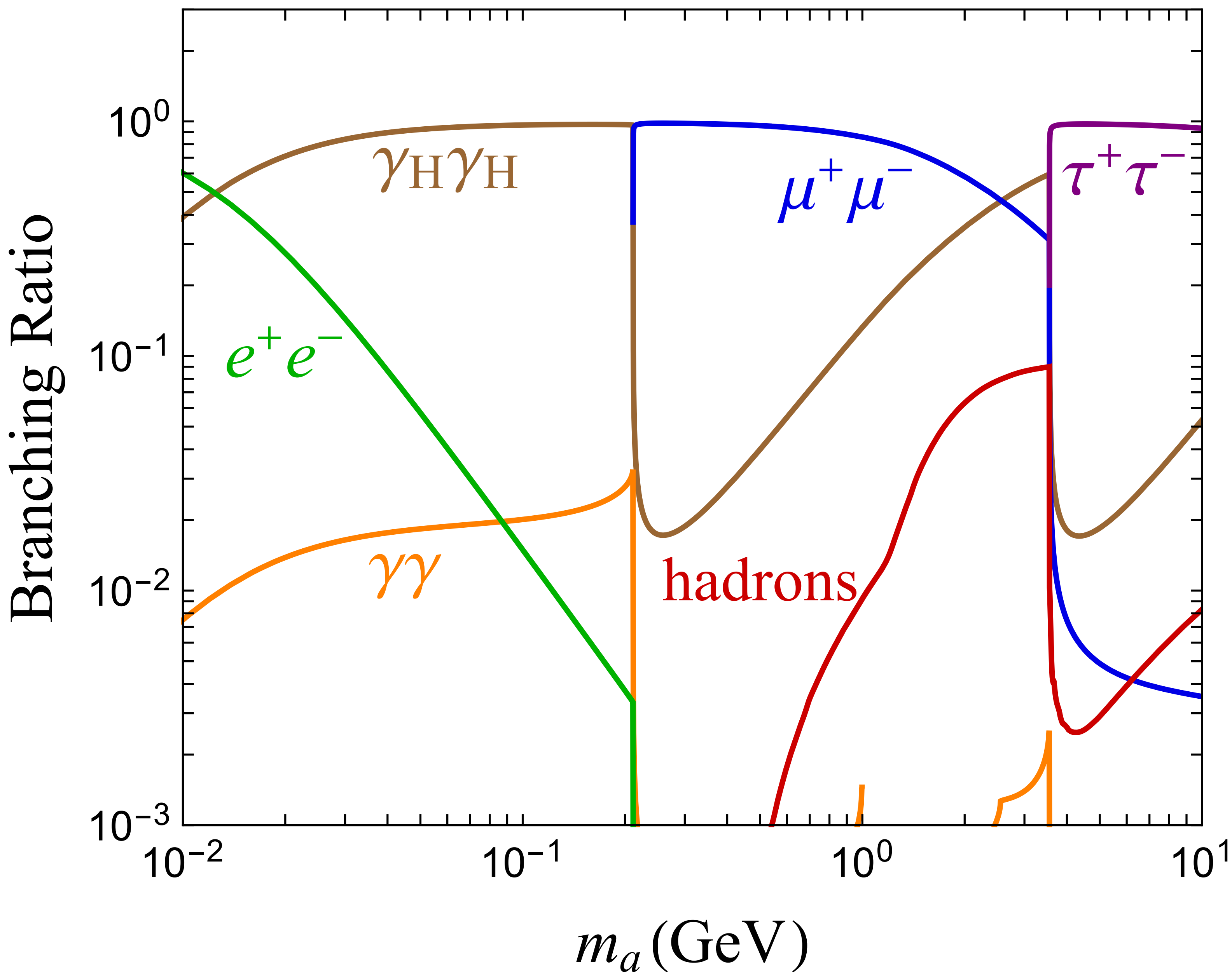


S.Y. Ho & F. Takahashi

M. Dolan et al. 2015

Axion decay channels with $\gamma_{\rm H}$

S.Y. Ho & F. Takahashi

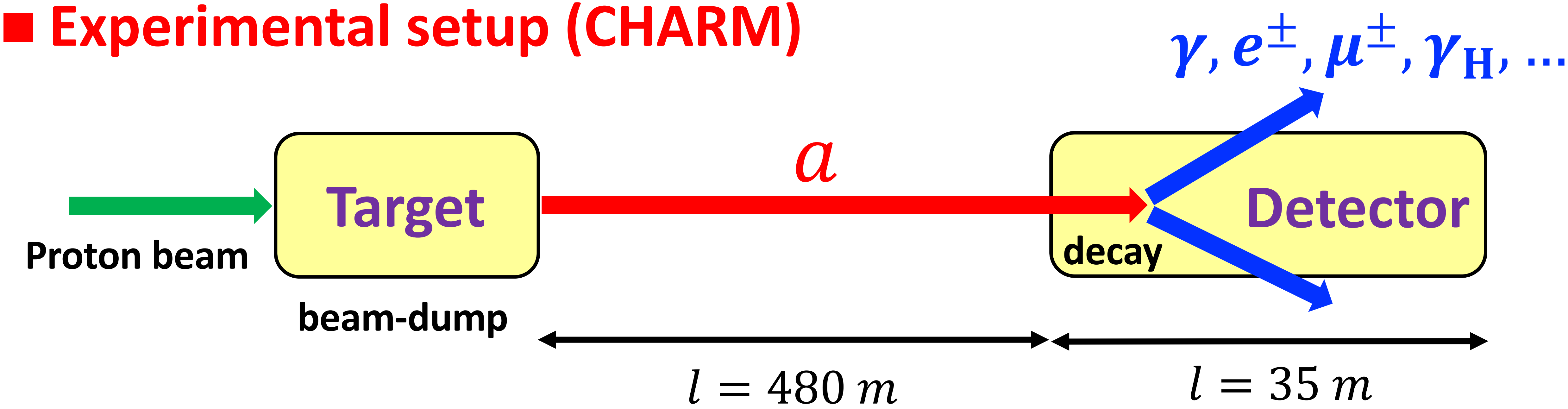


$$f_{\rm H} = f_a$$

$$\alpha_{\rm H} \simeq 0.73$$

Beam-dump experiments

■ Experimental setup (CHARM)

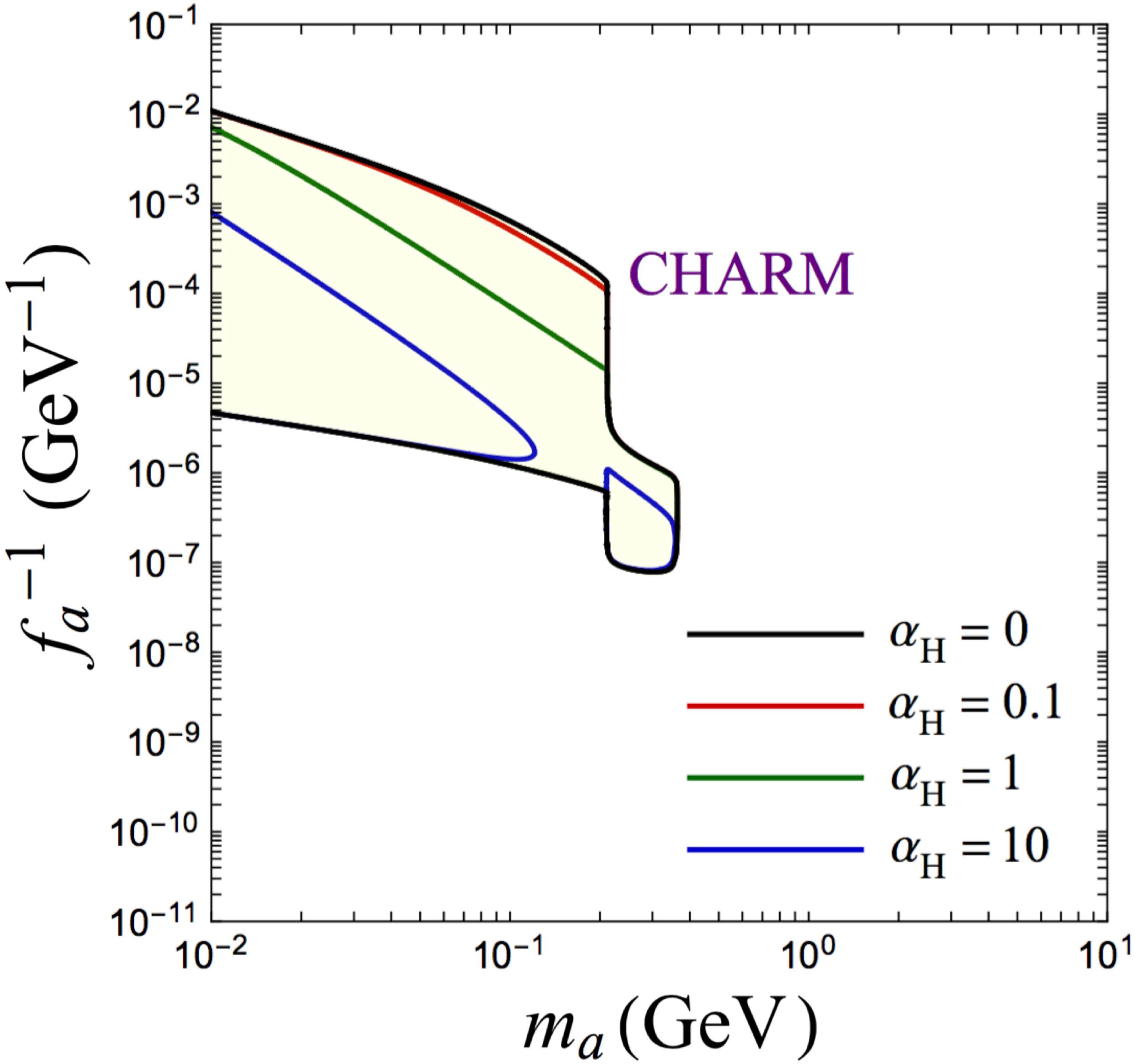


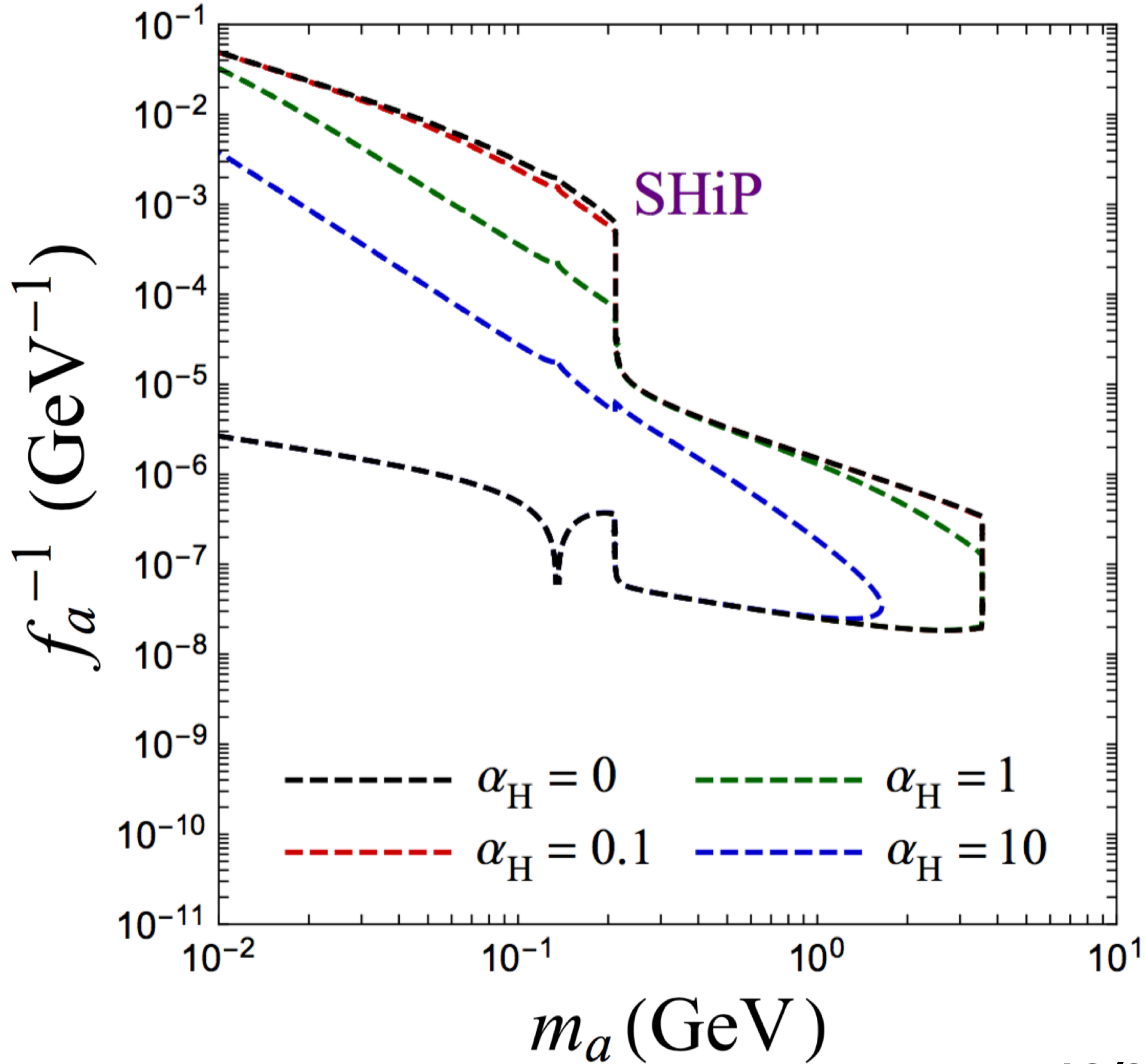
J.D. Clarke et al. 2014

$$N_{\rm det} \approx N_a \exp\left(-\frac{480\,{\rm m}}{\gamma_a \beta_a c\, \tau_a}\right)\left[1 - \exp\left(-\frac{35\,{\rm m}}{\gamma_a \beta_a c\, \tau_a}\right)\right] \sum_{X=e,\,\mu,\gamma} \mathcal{B}(a \to X\bar{X}) < 2.3$$

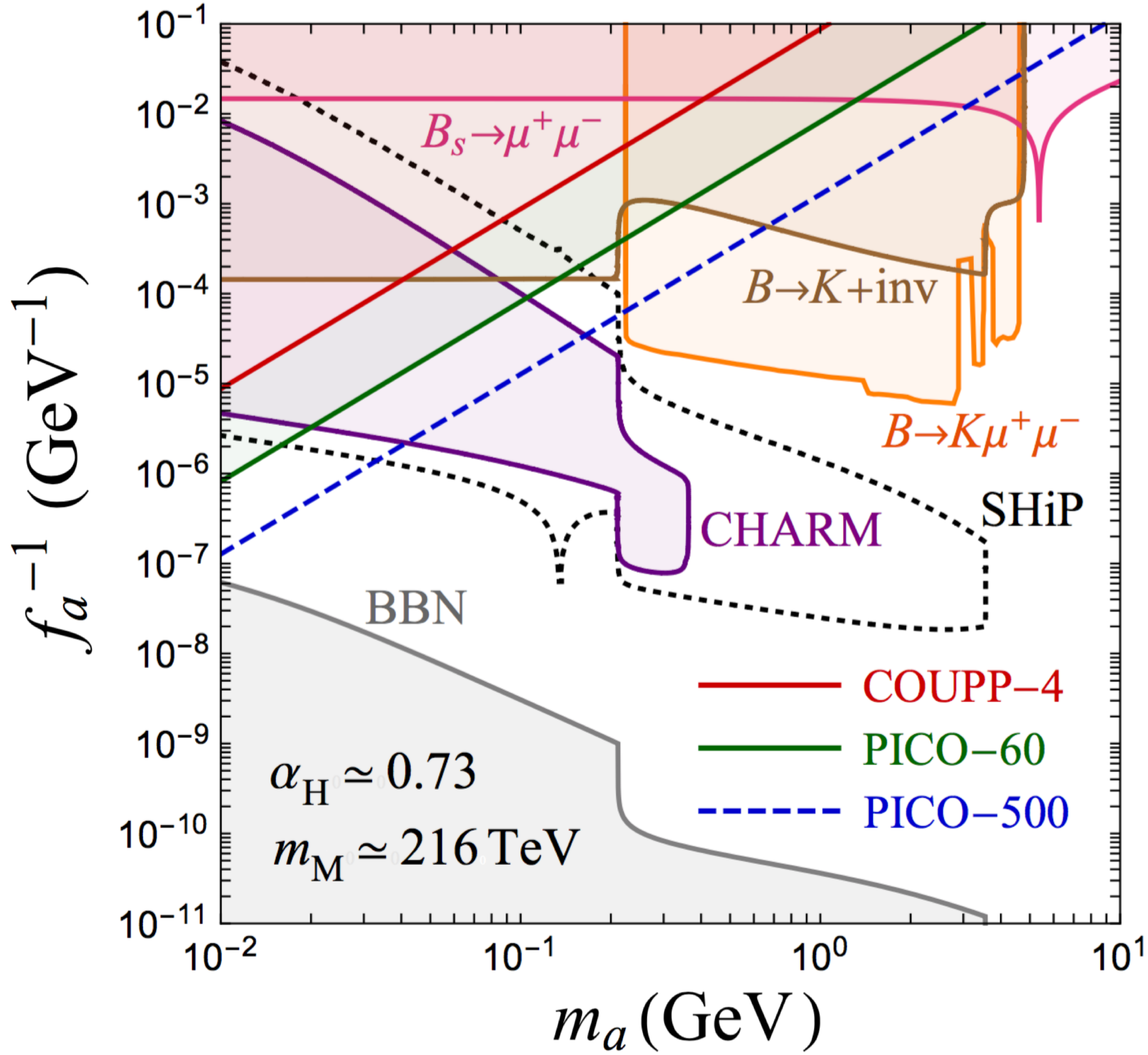
$$\gamma_a = (1-\beta_a^2)^{-1/2} \approx 10\,{\rm GeV}/m_a \qquad \tau_a = \frac{1}{\Gamma_a} = \frac{1}{\Gamma(a\to\gamma_{\rm H}\gamma_{\rm H}) + \Gamma(a \to {\rm vis})}$$

Beam-dump exps. : m_a vs f_a^{-1}





Combined result : m_a vs f_a^{-1}



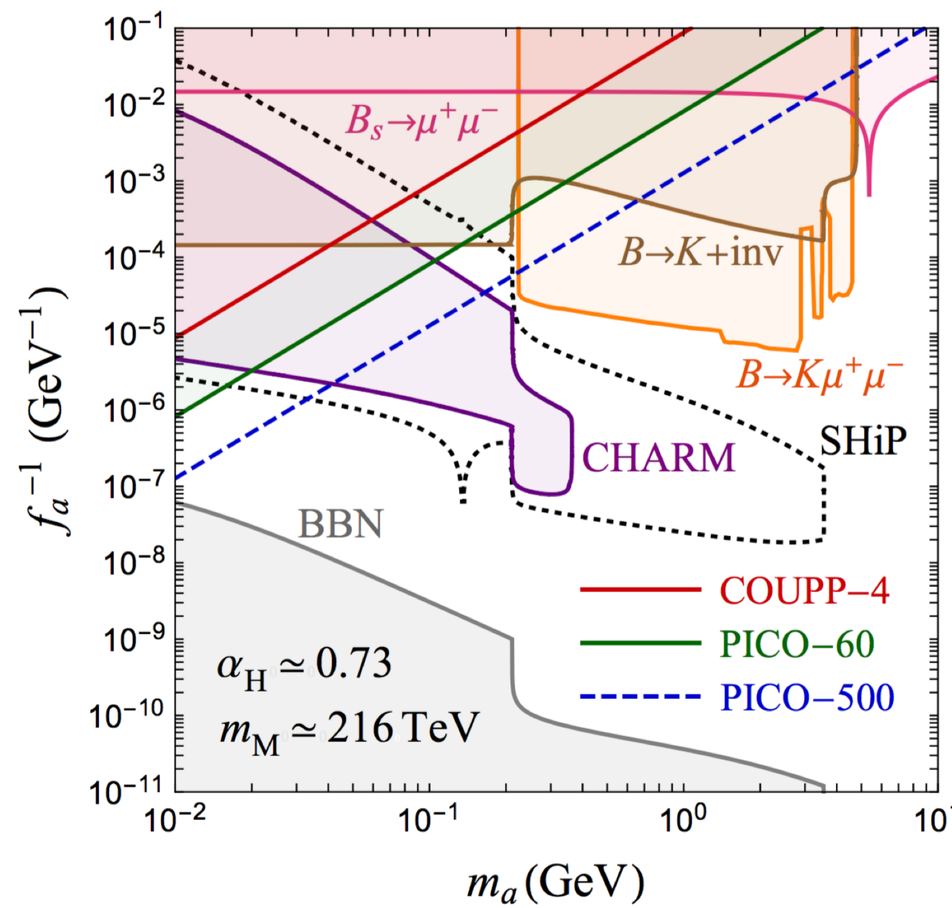
$$m_a = \mathcal{O}(10)\,\text{MeV}$$
$$f_a = \mathcal{O}(10^5)\,\text{GeV}$$

$$m_a = \mathcal{O}(100)\,\text{MeV}$$
$$f_a = \mathcal{O}(10^4)\,\text{GeV}$$

We find two parameter regions where both the hidden monopole DM and the axion are within the reach of the direct search and beam-dump experiments.

Summary

- We have studied the hidden monopole DM via the axion portal.
- We have computed the spin-dependent cross-section of the hidden monopole DM scattering off a nucleon and compare it to the direct search experiments.
- We have found two parameter regions where both the hidden monopole DM and the axion are within the reach of the direct search experiments & beam-dump experiments.



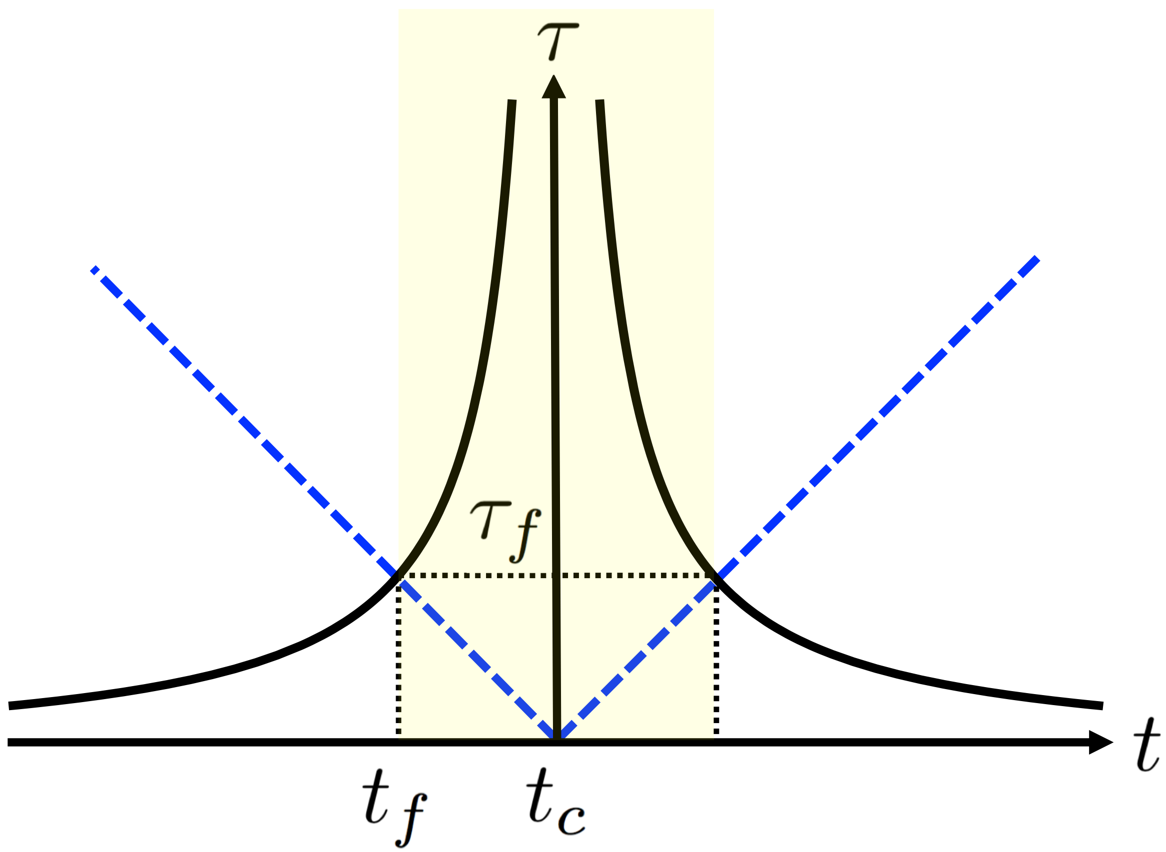
Back up

Kibble-Zurek mechanism

■ Second-order phase transition

$$\zeta = \zeta_0 |\epsilon|^{-\nu}, \quad \tau = \tau_0 |\epsilon|^{-\mu}, \quad \epsilon \equiv \frac{T - T_c}{T_c}$$

Correlation length **Relaxation time**



Frozen : $t_f - t_c = \tau_f$

$$|\epsilon_f| = \left[\tau_0 H(t_c)\right]^{1/(1+\mu)}$$

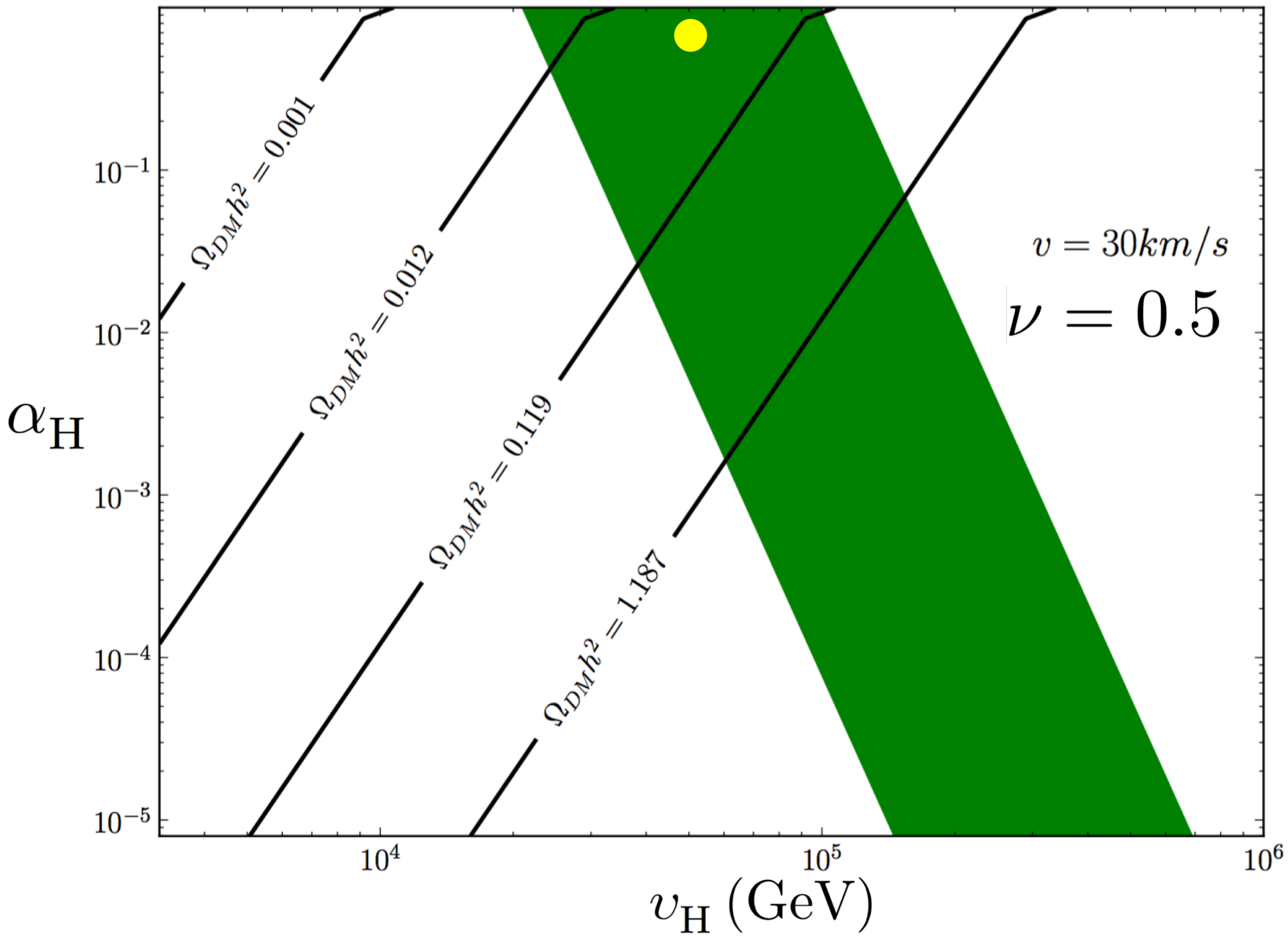
$$\zeta_f = \zeta_0 \left[\tau_0 H(t_c)\right]^{-\nu/(1+\mu)}$$

$$n_{\mathrm{M}} \simeq \zeta_f^{-3}$$

Benchmark point

■ Self-interacting DM : Hidden monopole

Khoze & Ro 2014



Green region

$$0.1\ \frac{\mathrm{cm}^2}{\mathrm{g}} < \frac{\sigma_{\mathrm{T}}}{m_{\mathrm{DM}}} < 10\ \frac{\mathrm{cm}^2}{\mathrm{g}}$$

$$v_{\mathrm{DM}} \simeq 30\ \frac{\mathrm{km}}{\mathrm{s}}$$

35% hidden monopole DM

$$\alpha_{\mathrm{H}} \simeq 0.73$$

$$m_{\mathrm{M}} \simeq 216\ \mathrm{TeV}$$