

*NCTS Annual Meeting 2019, Hsinchu, Taiwan*  
*Yen-Hsun Lin (林彥勳)*  
*Institute of Physics, Academia Sinica*

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# **Probing the isospin violation of self-interacting dark matter through old neutron stars**

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# Outline

▶ **Part I:**

Motivation for introducing dark matter (DM) self-interaction

▶ **Part II:**

- Neutron star (NS) capture of isospin violation DM
- Black hole (BH) formation in the NS

▶ **Part III:**

NS sensitivities on DM-baryon cross section and isospin violation

▶ **Summary**



X-ray: NASA/CXC/SAO

Optical: NASA/STScI

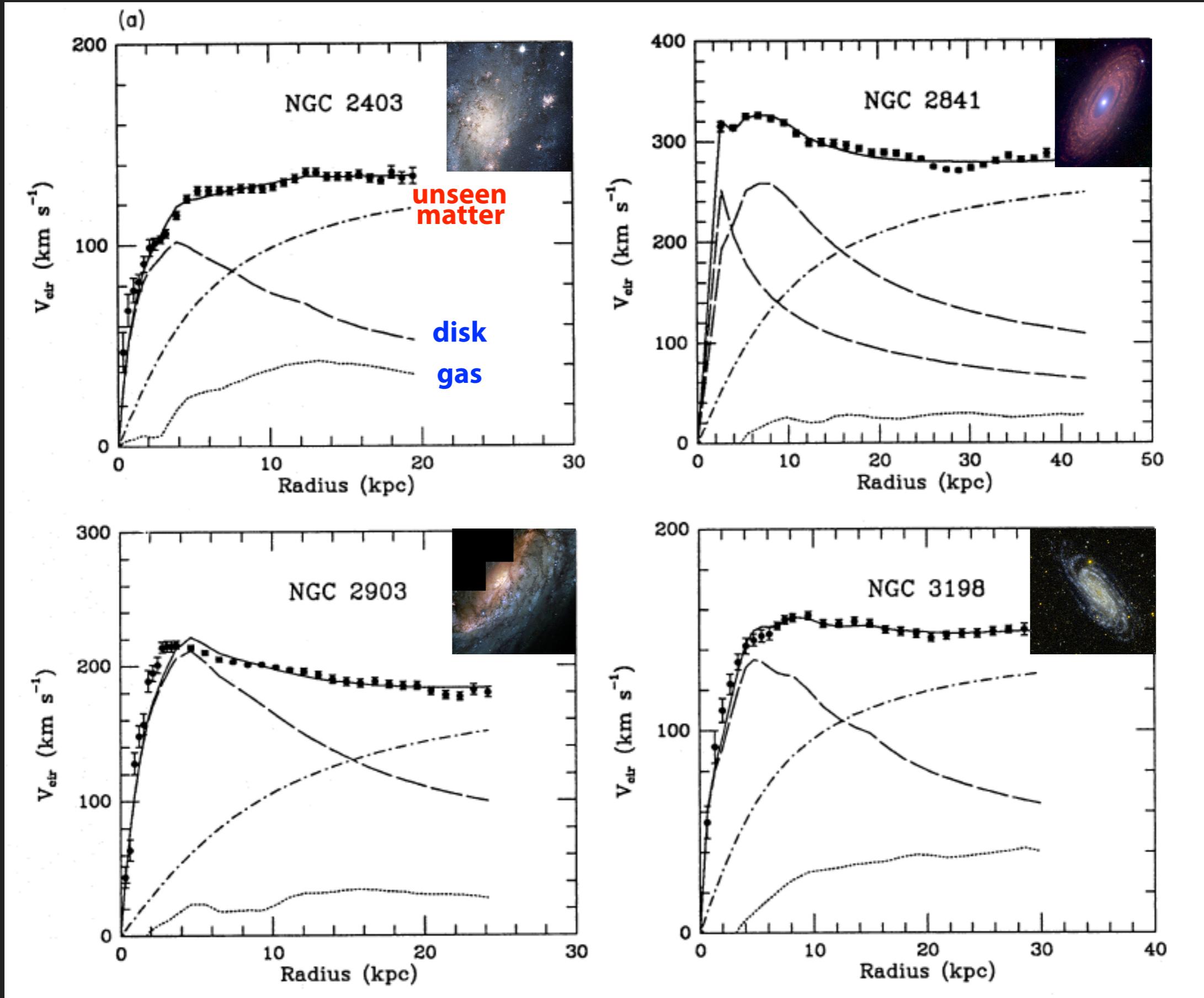
Infrared: NASA-JPL-Caltech

**Crab Nebula**

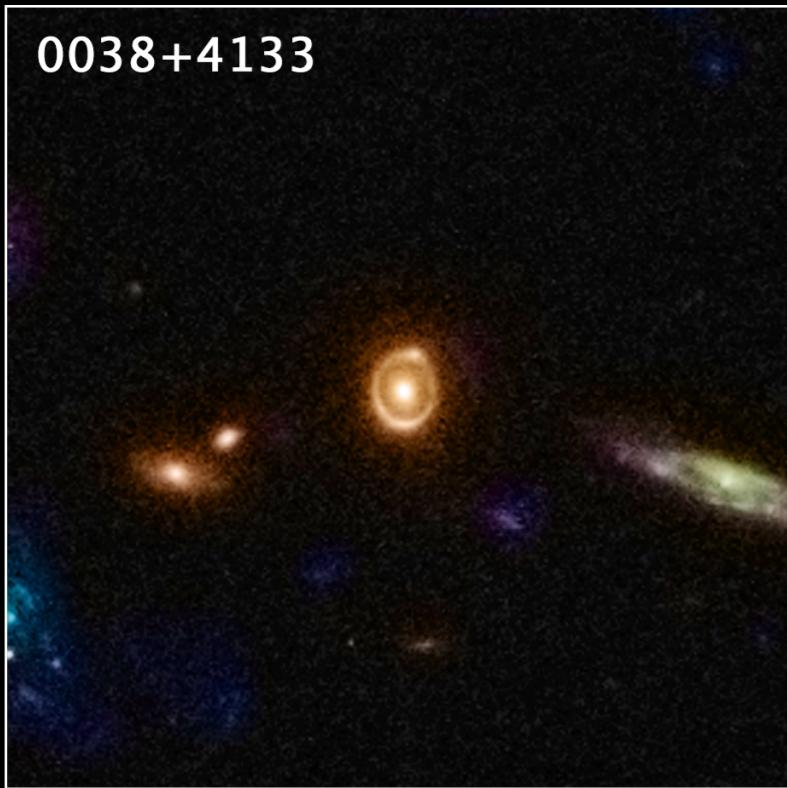
## Part I

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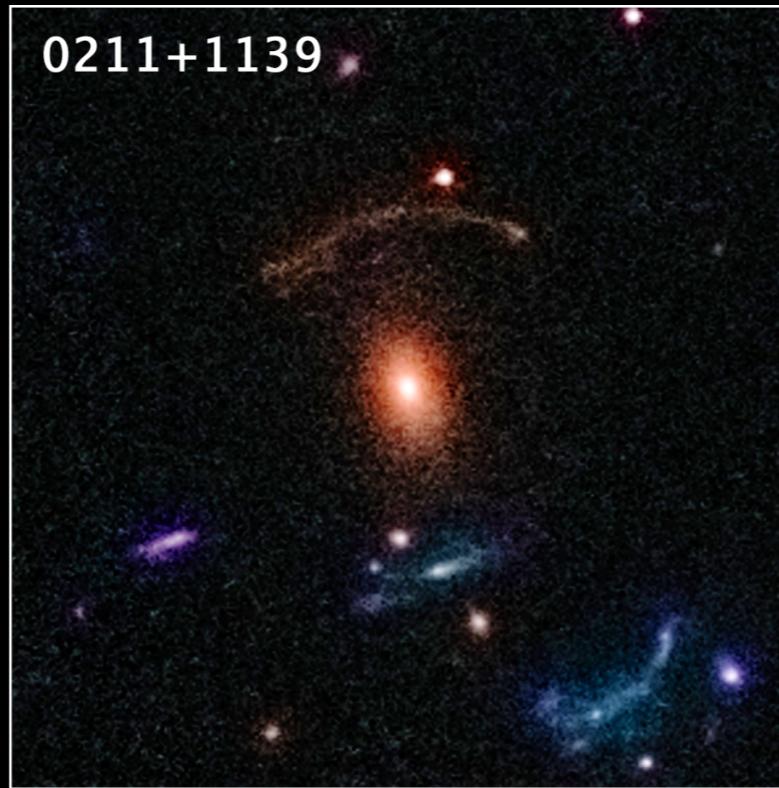
# DM in the Universe



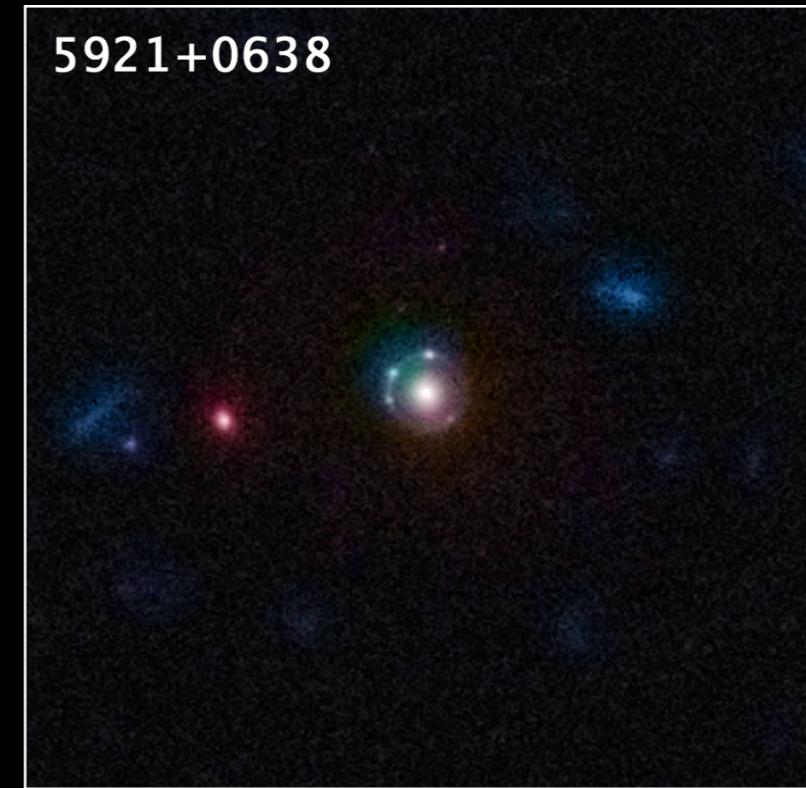
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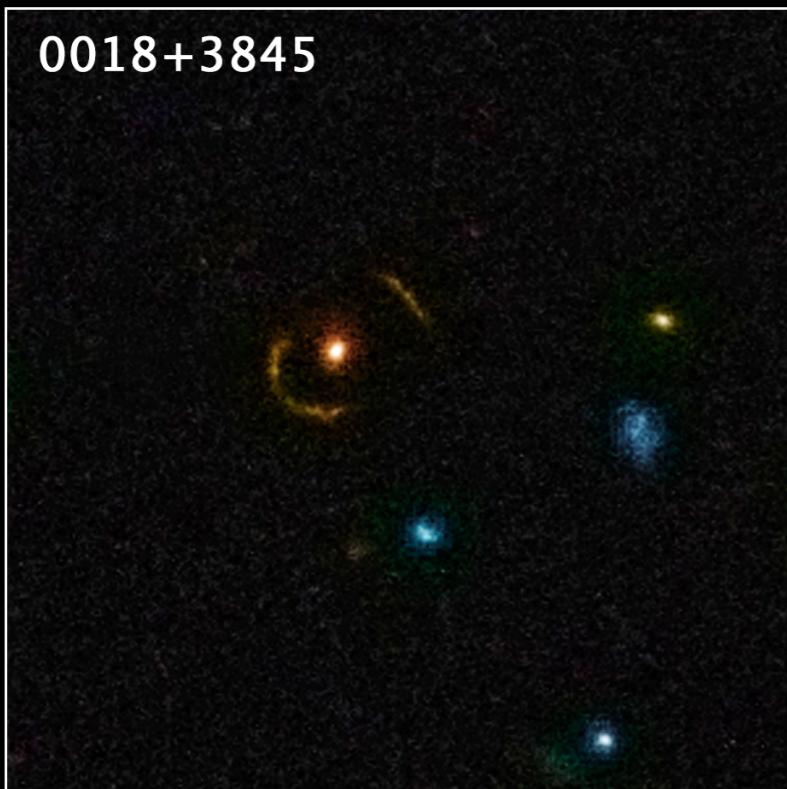
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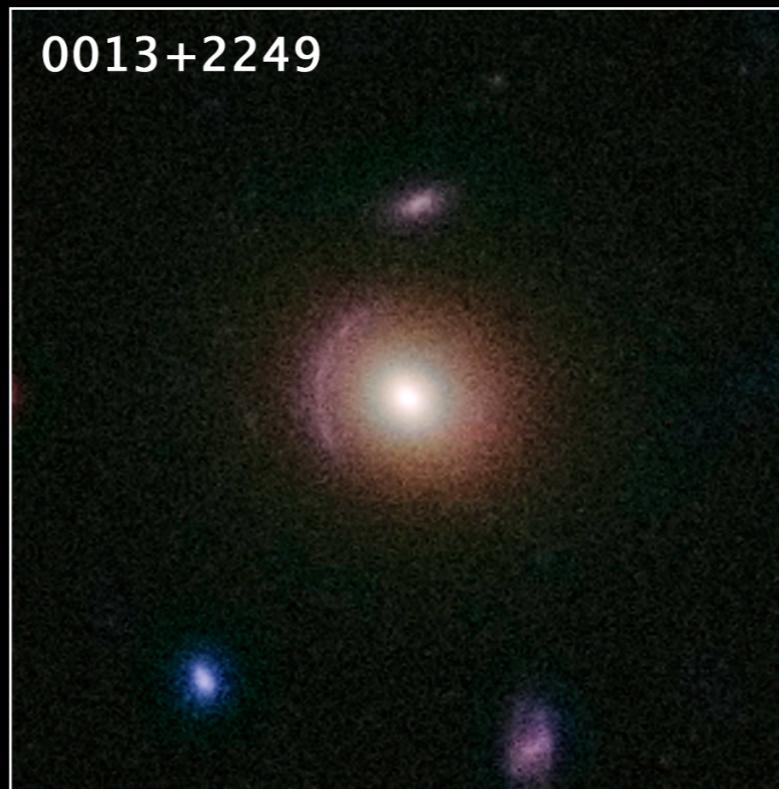
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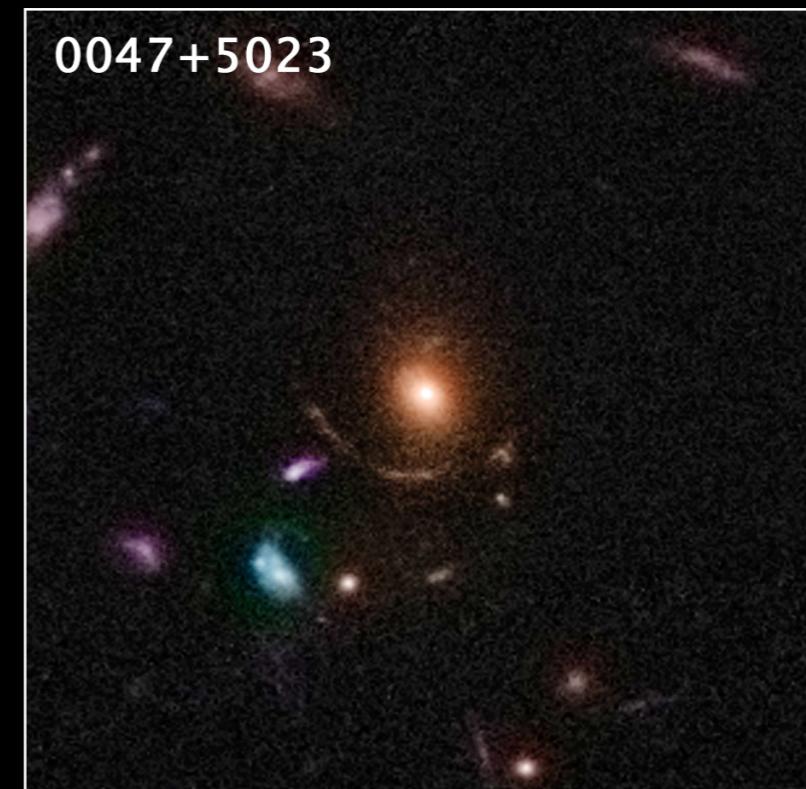
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0013+2249

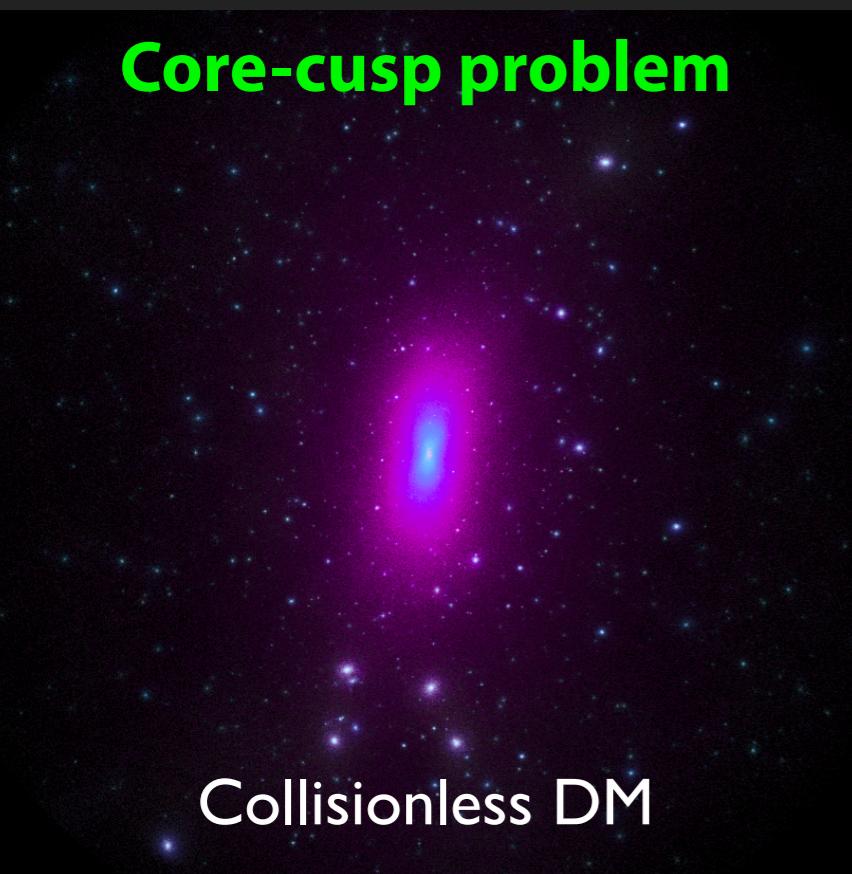


0047+5023

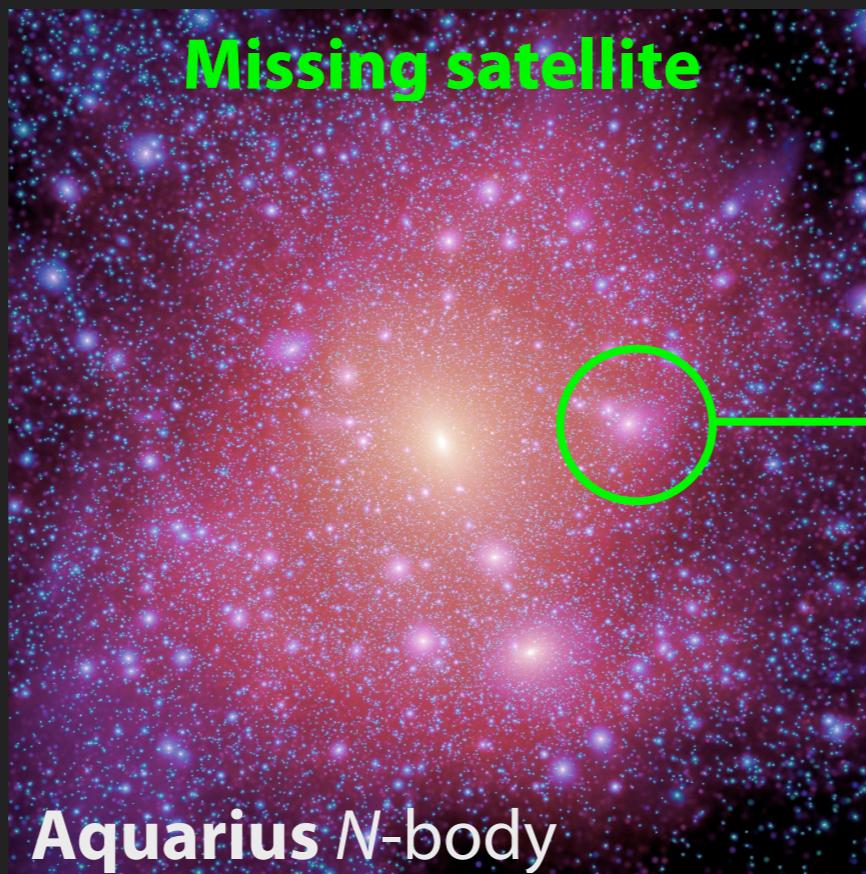


**Gravitational Lenses in the COSMOS Survey**  
*Hubble Space Telescope ■ ACS/WFC*

## Core-cusp problem



## Missing satellite

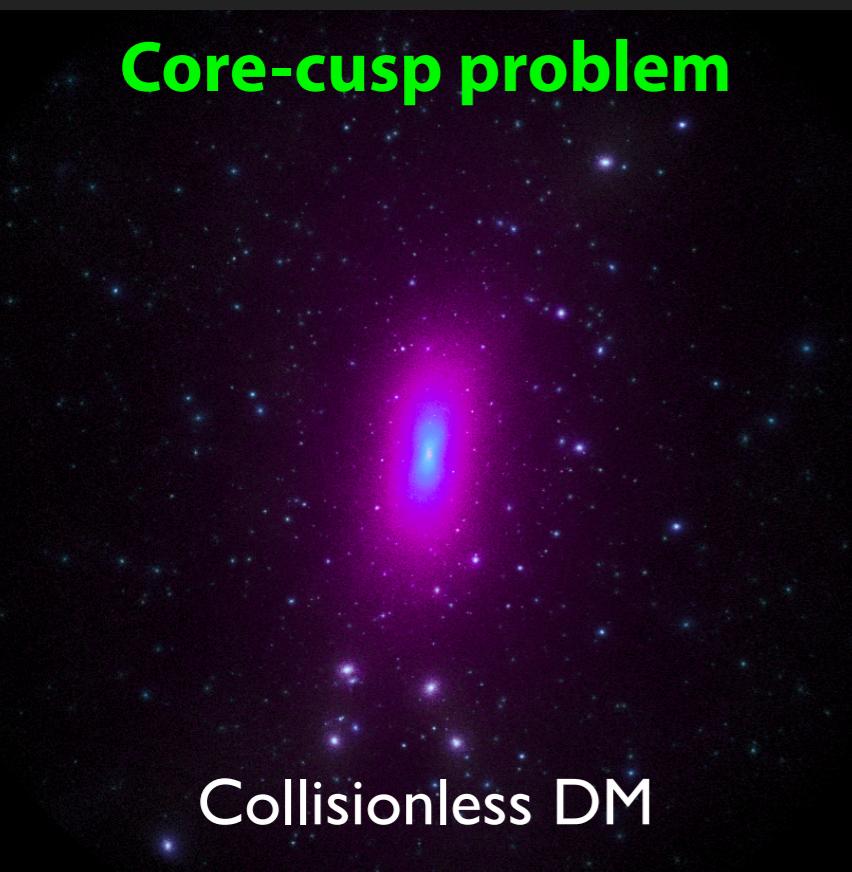


## Too-big-to-fail



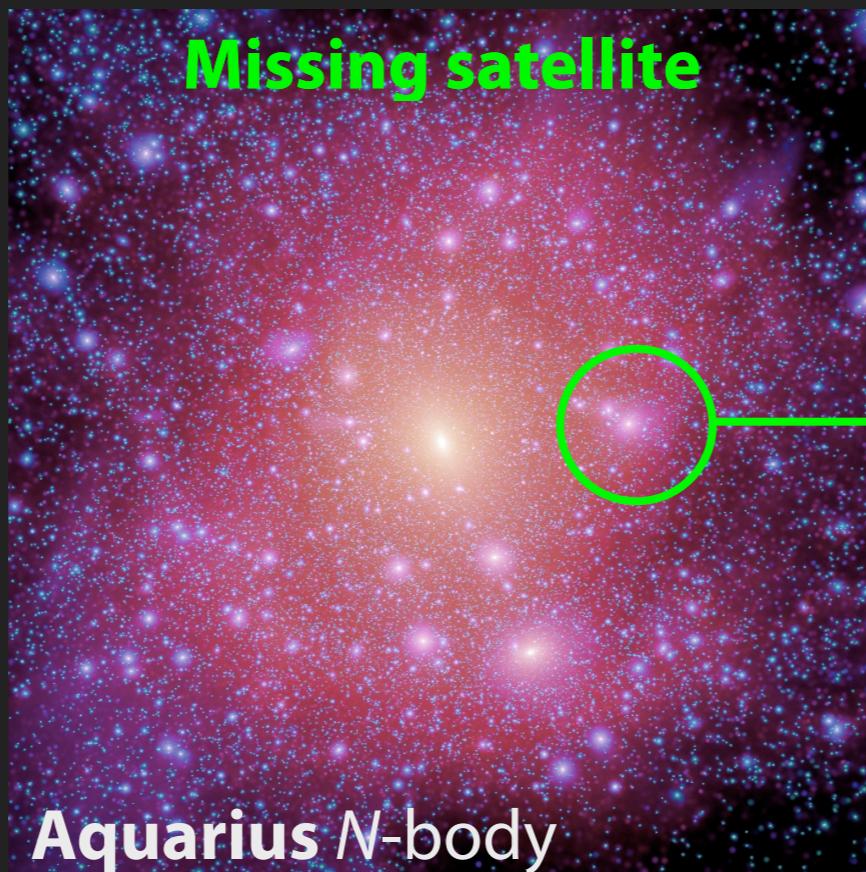
We didn't see any satellite as massive as predicted by the  $N$ -body sim.

## Core-cusp problem



Collisionless DM

## Missing satellite



Aquarius N-body

## Too-big-to-fail

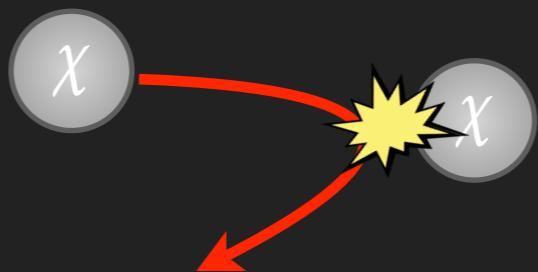


We didn't see any satellite as massive as predicted by the  $N$ -body sim.

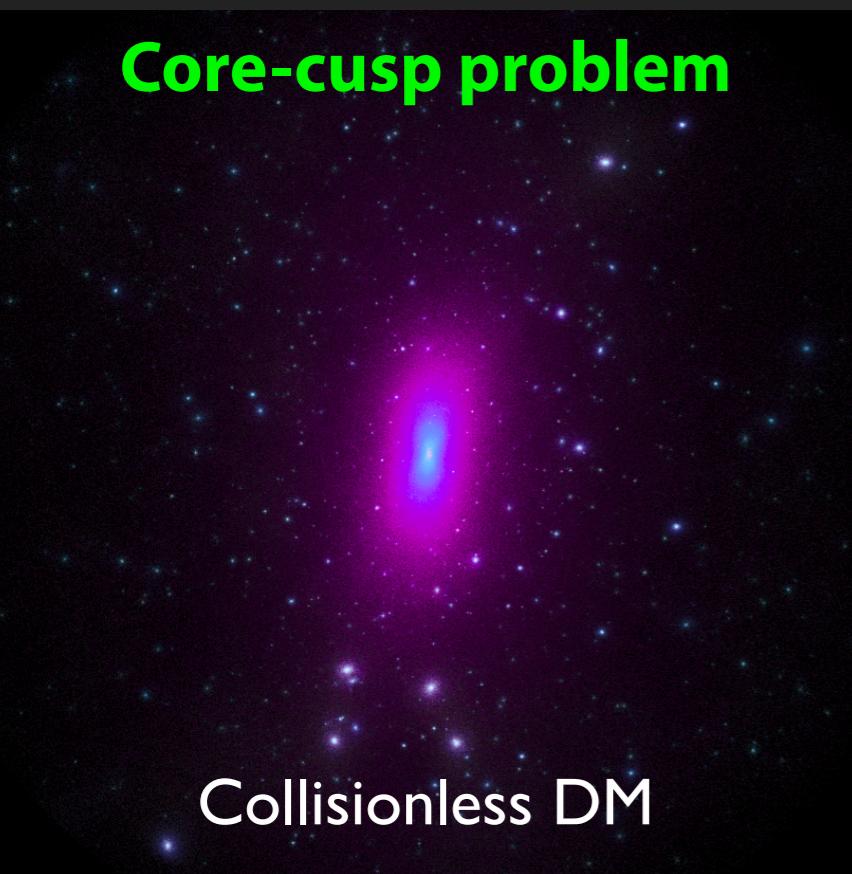
## To alleviate these small-scale problems:

DM self-interaction is introduced

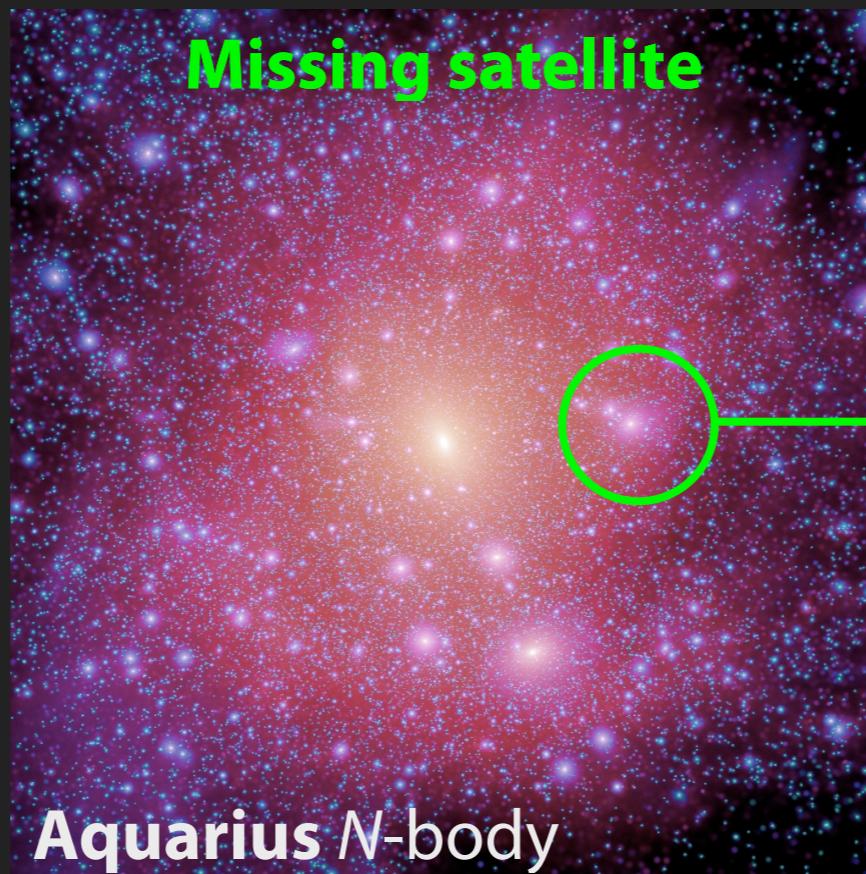
$$10^{-25} \frac{\text{cm}^2}{\text{GeV}} \leq \frac{\sigma_{\chi\chi}}{m_\chi} \leq 10^{-23} \frac{\text{cm}^2}{\text{GeV}}$$



## Core-cusp problem



## Missing satellite



## Too-big-to-fail

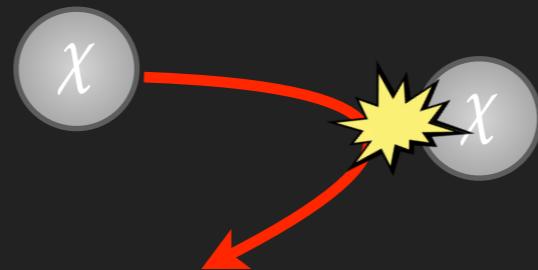


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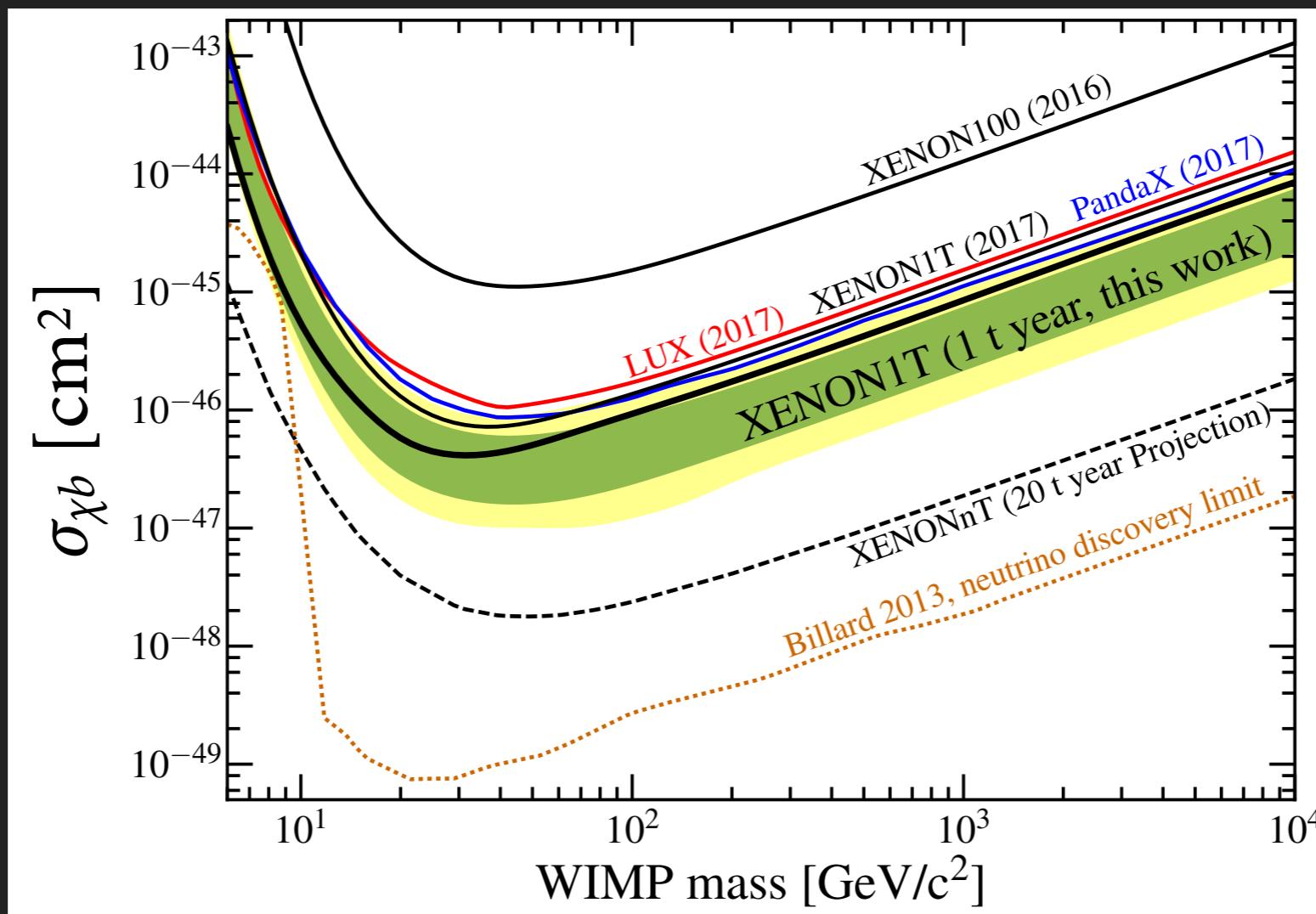
$$10^{-25} \frac{\text{cm}^2}{\text{GeV}} \leq \frac{\sigma_{\chi\chi}}{m_\chi} \leq 10^{-23} \frac{\text{cm}^2}{\text{GeV}}$$



Assuming attractive Yukawa int.

$$V(r) = \alpha_\chi \frac{e^{-m_\phi r}}{r}$$

# Constraints from DM direct searches



- S. A. Malik *et al.*, *Phys. Dark Univ.* **9-10**, 51 (2015)  
O. Buchmueller *et al.*, *JHEP* 01, **037** (2015)  
J. Aalbers *et al.* [DARWIN], *JCAP* **11**, 017 (2016)  
D. S. Akerib *et al.* [LUX] *PRL* **118**, 021303 (2017)  
C. Amole *et al.* [PICO], *PRL* **118**, 251301 (2017)  
E. Aprile *et al.* [XENON] *PRL* **119**, 181301 (2017)

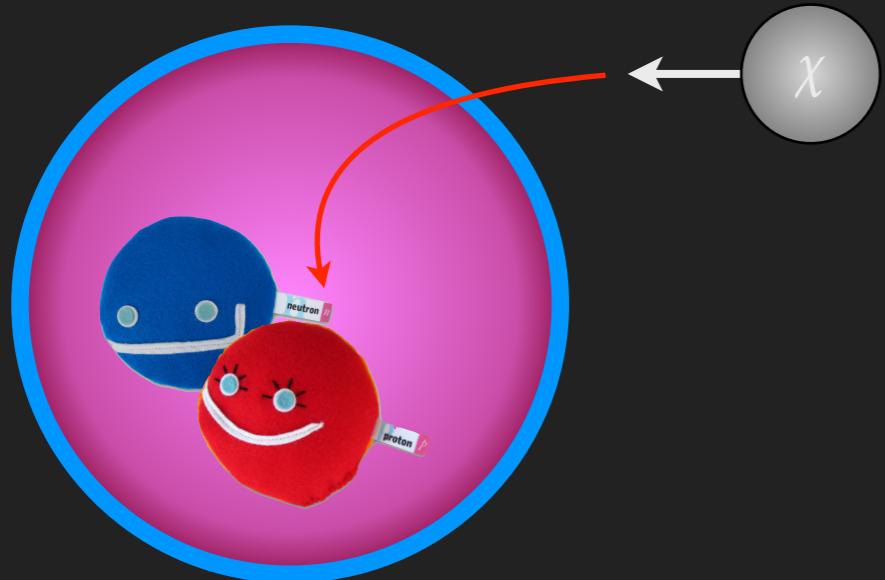


## Part II

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**DM captured by  
the neutron star**

# Capturing DM particles



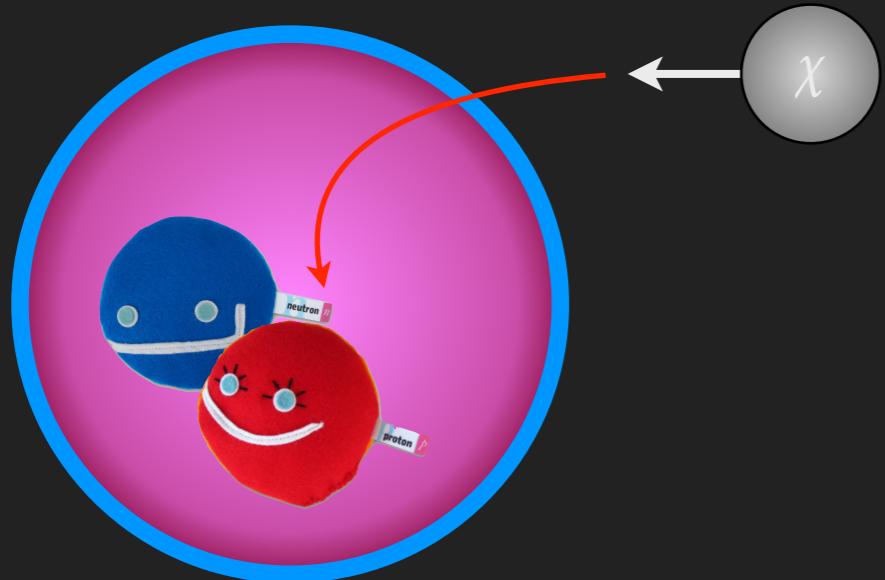
**NS capture rate  $C_c$ :**  
DM-baryon interaction  $\sigma_{\chi b}$   
 $b = n, p$  for neutron and proton

R. Garani *et al.*, JCAP **05**, 035 (2019)

$$C_c \propto \left( \frac{\rho_\chi}{m_\chi} \right) \int_0^\infty \frac{f(u)}{u} w(r) du \int_0^{v_{\text{esc}}(r)} R^-(w \rightarrow v) dv$$

$$R^-(w \rightarrow v) = \int \zeta_b(r) \rho_u \frac{d\sigma_{\chi b}}{dv} |w - u| f_b(E_b, r) [1 - f_{b'}(E_b + q_0, r)] d^3 u$$

# Capturing DM particles



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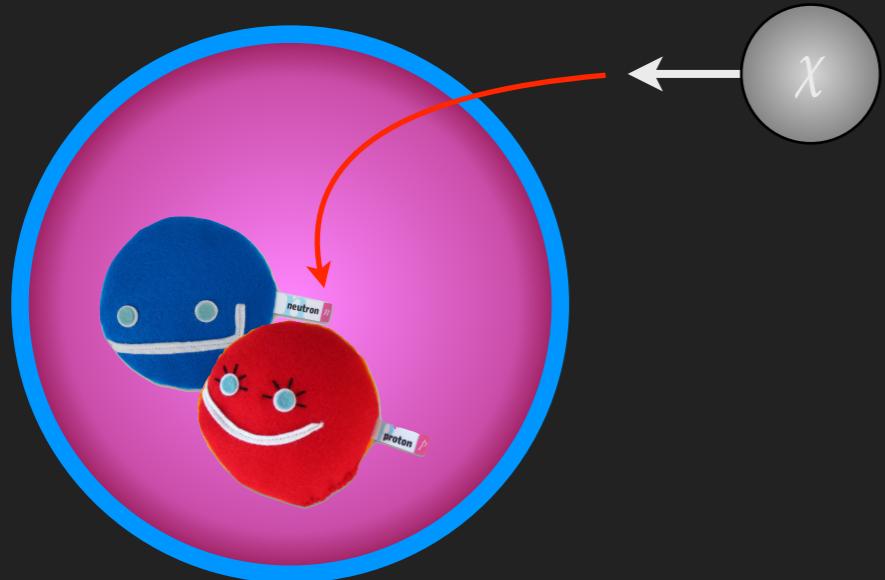
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differential scattering rate

$$R^-(w \rightarrow v) = \int \zeta_b(r) \rho_u \frac{d\sigma_{\chi b}}{dv} |w - u| f_b(E_b, r) [1 - f_{b'}(E_b + q_0, r)] d^3 u$$

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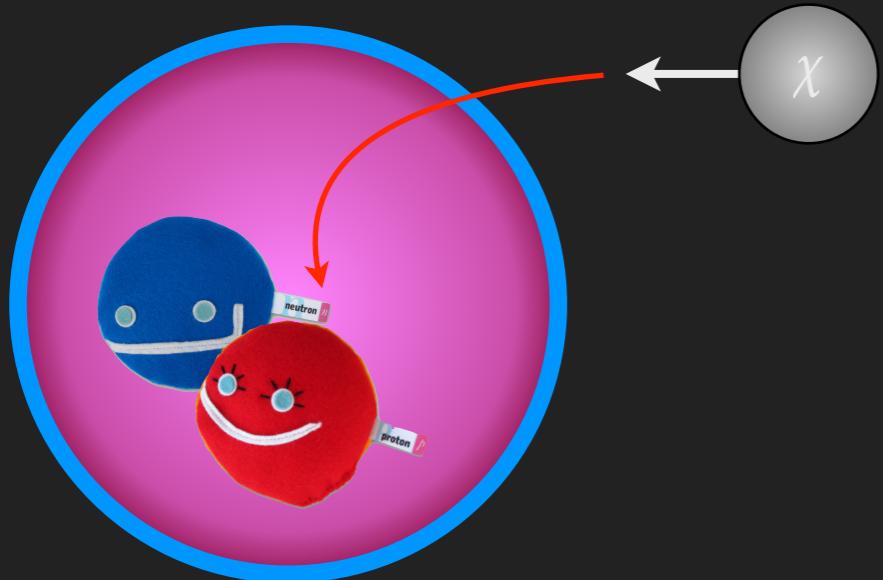
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differential scattering rate

$$R^-(w \rightarrow v) = \int \left[ \zeta_b(r) \rho_u \frac{d\sigma_{\chi b}}{dv} \right] |w - u| f_b(E_b, r) [1 - f_{b'}(E_b + q_0, r)] d^3 u$$

baryon density dist.

# Capturing DM particles



**NS capture rate  $C_c$ :**  
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R. Garani *et al.*, JCAP **05**, 035 (2019)

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DM-baryon  
cross section

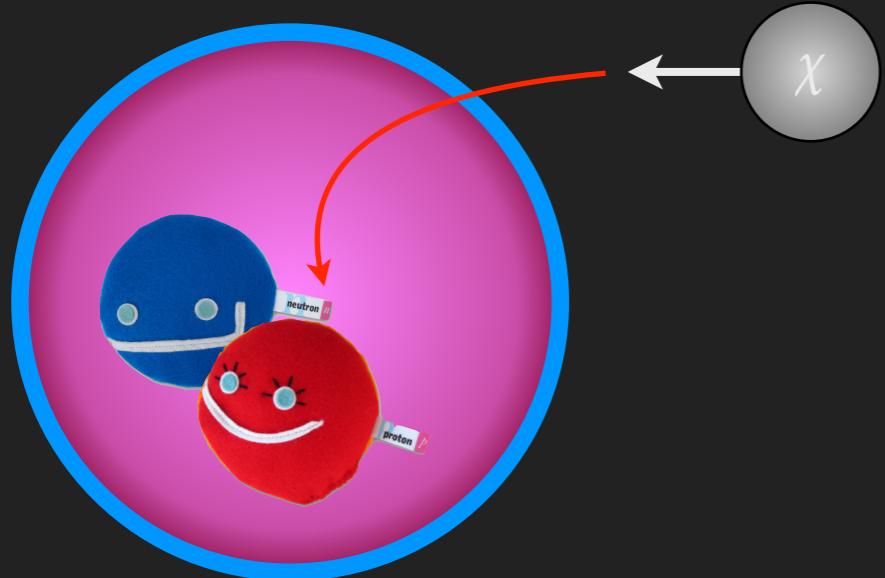
differential scattering rate

$$R^-(w \rightarrow v) = \int \zeta_b(r) \rho_u \frac{d\sigma_{\chi b}}{dv} |w - u| f_b(E_b, r) [1 - f_{b'}(E_b + q_0, r)] d^3 u$$

Annotations:

- A green box encloses  $\zeta_b(r) \rho_u$ . An orange box encloses  $\frac{d\sigma_{\chi b}}{dv}$ . A green arrow points from the green box to the text "baryon density dist.". An orange arrow points from the orange box to the text "DM-baryon cross section".

# Capturing DM particles



**NS capture rate  $C_c$ :**  
DM-baryon interaction  $\sigma_{\chi b}$   
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R. Garani *et al.*, JCAP **05**, 035 (2019)

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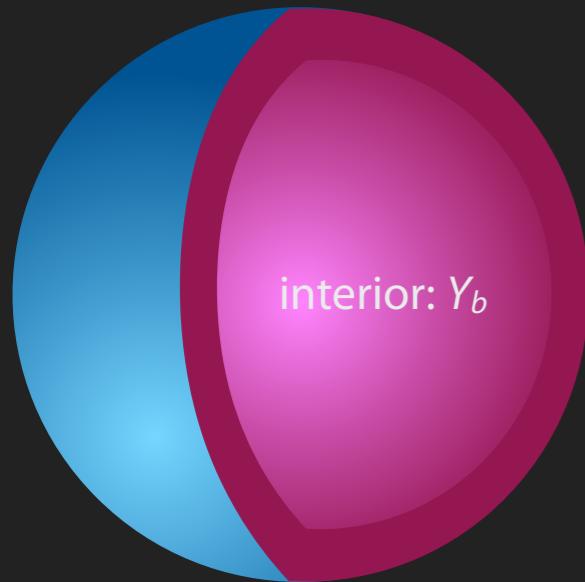
DM-baryon cross section

baryon density dist.

differential scattering rate

Fermi-Dirac dist. of baryons

# Baryons in the NS



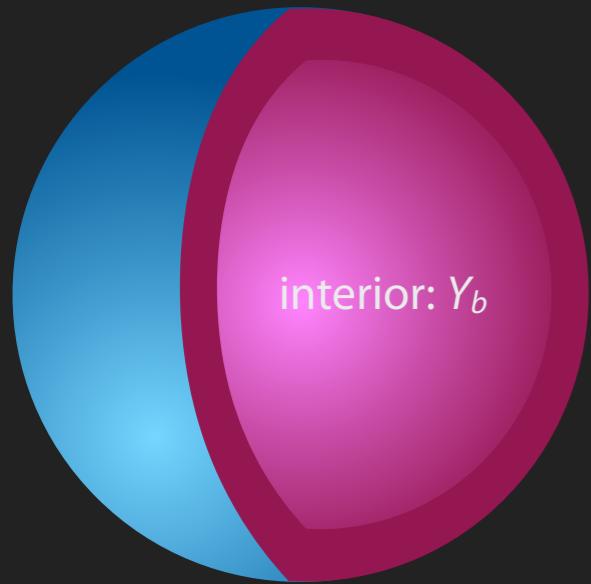
- Density distributions
  - Chemical potentials
- } not identical  
for  $n$  and  $p$

A. Y. Potekhin *et al.*, AA **560**, A48 (2013)

S. Goriely *et al.*, PRC **88**, 024303 (2013)

R. Garani *et al.*, JCAP **05**, 035 (2019)

# Baryons in the NS

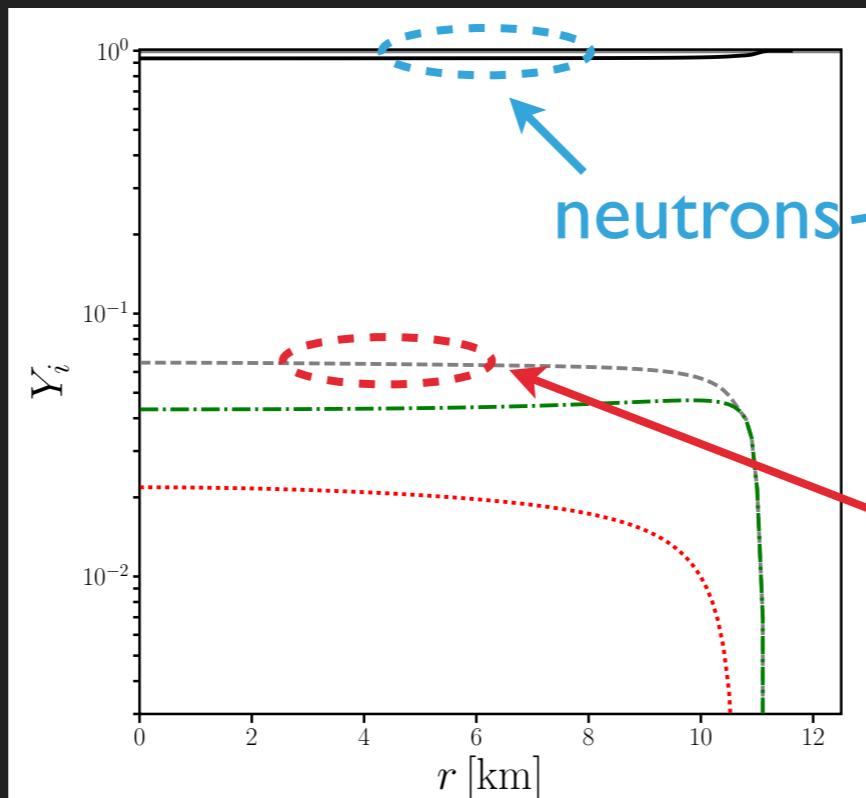


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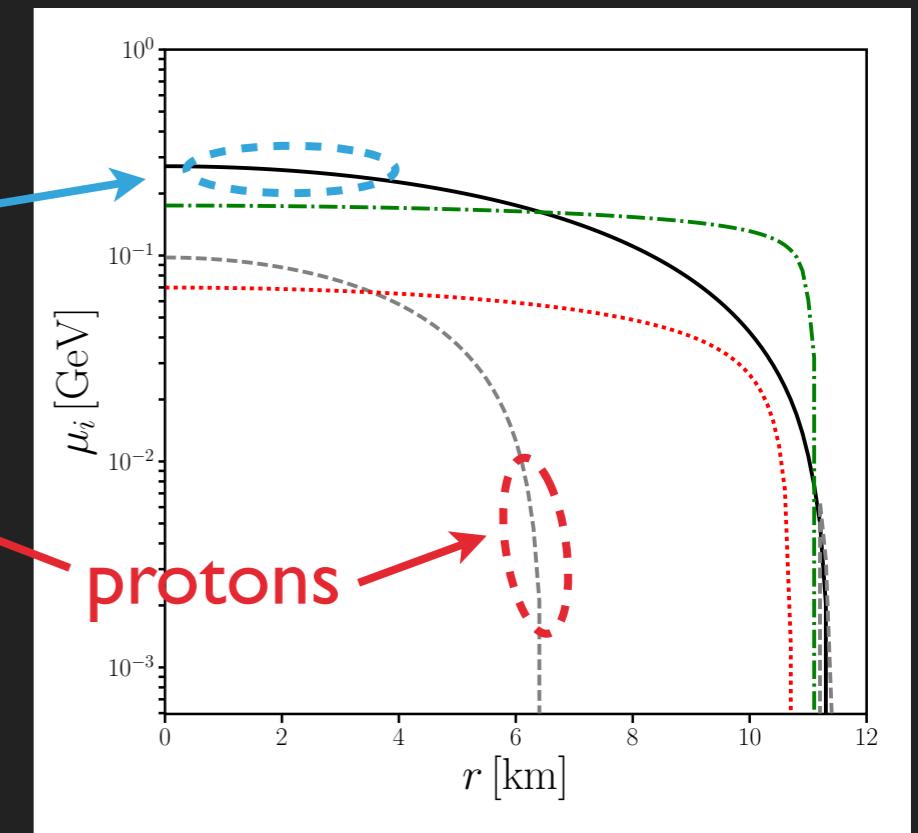
- Density distributions
- Chemical potentials

not identical  
for  $n$  and  $p$

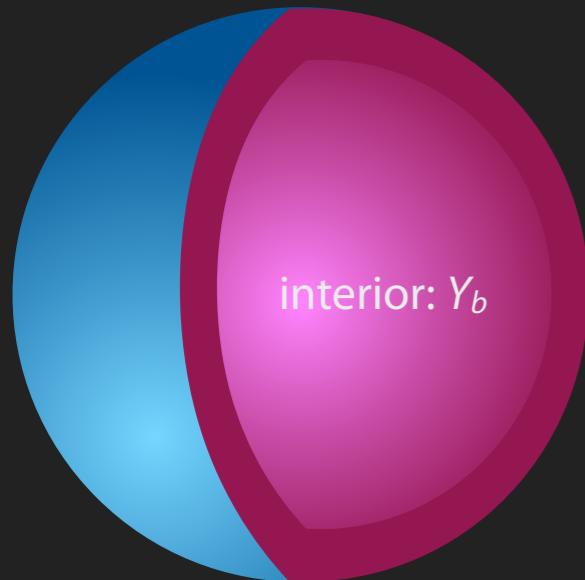
baryonic yields



chemical potentials

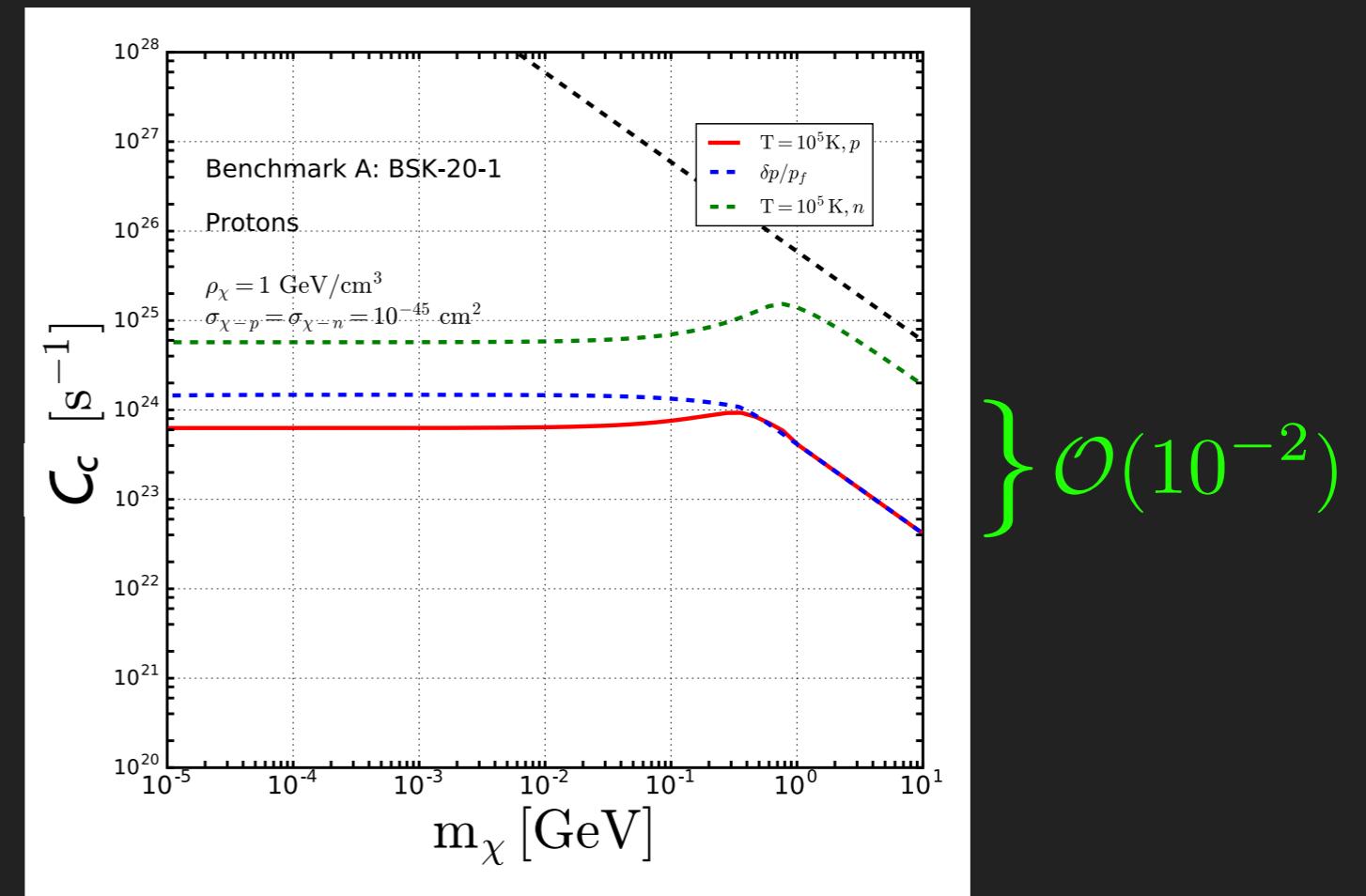


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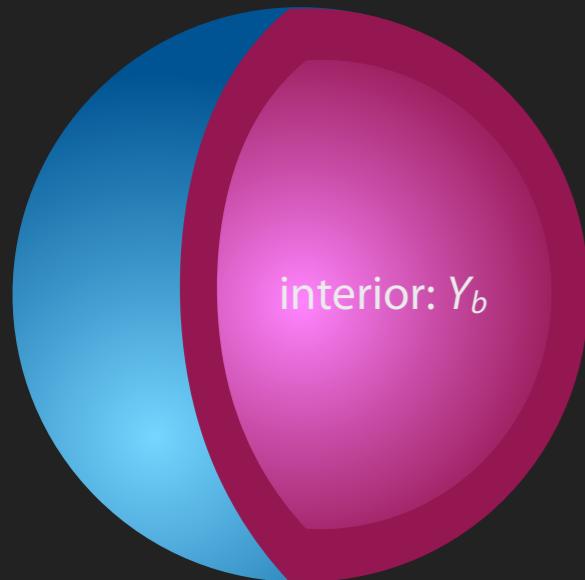
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Capture rate  $C_c$ :  $\sigma_{\chi n} = \sigma_{\chi p} = 10^{-45} \text{ cm}^2$



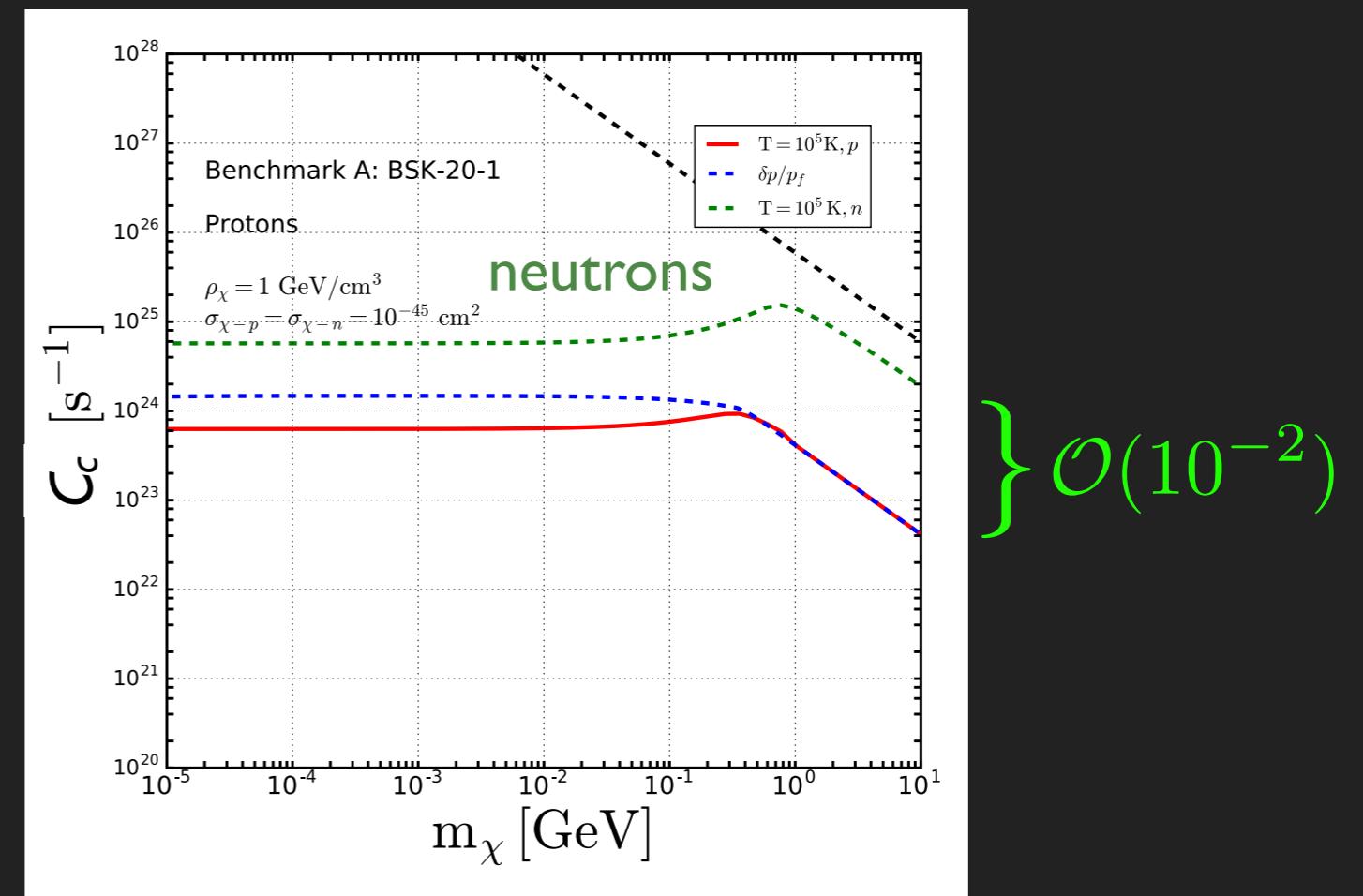
R. Garani *et al.*, JCAP **05**, 035 (2019)  
(private communication)

# Baryons in the NS



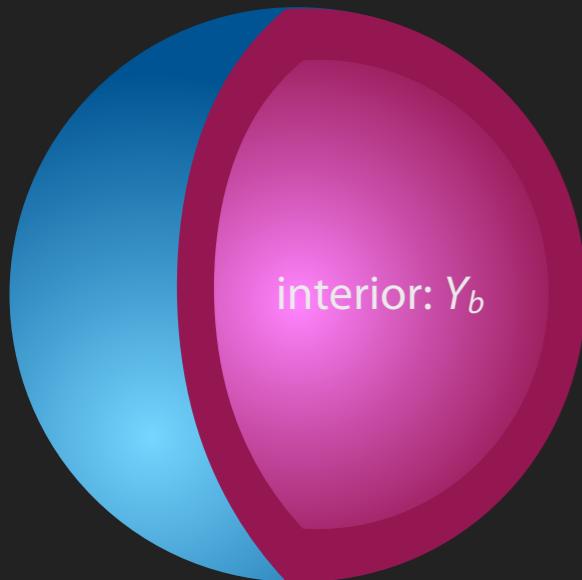
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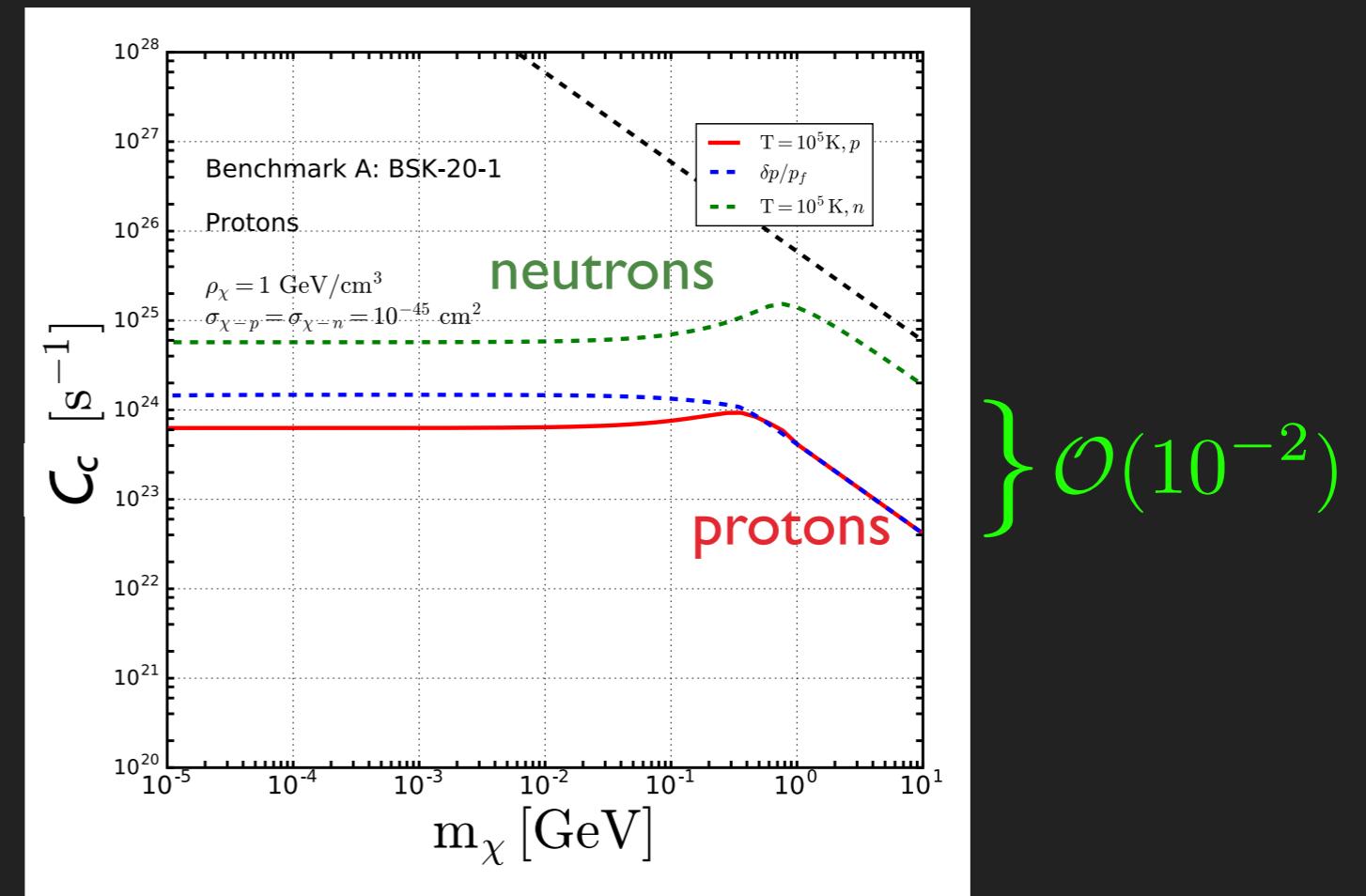
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# Baryons in the NS



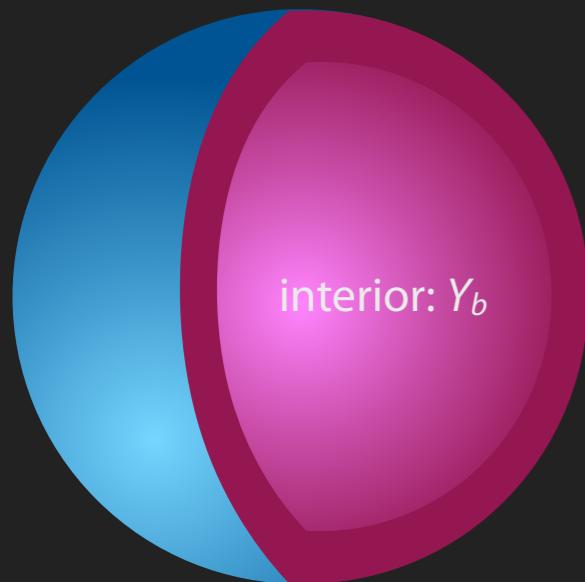
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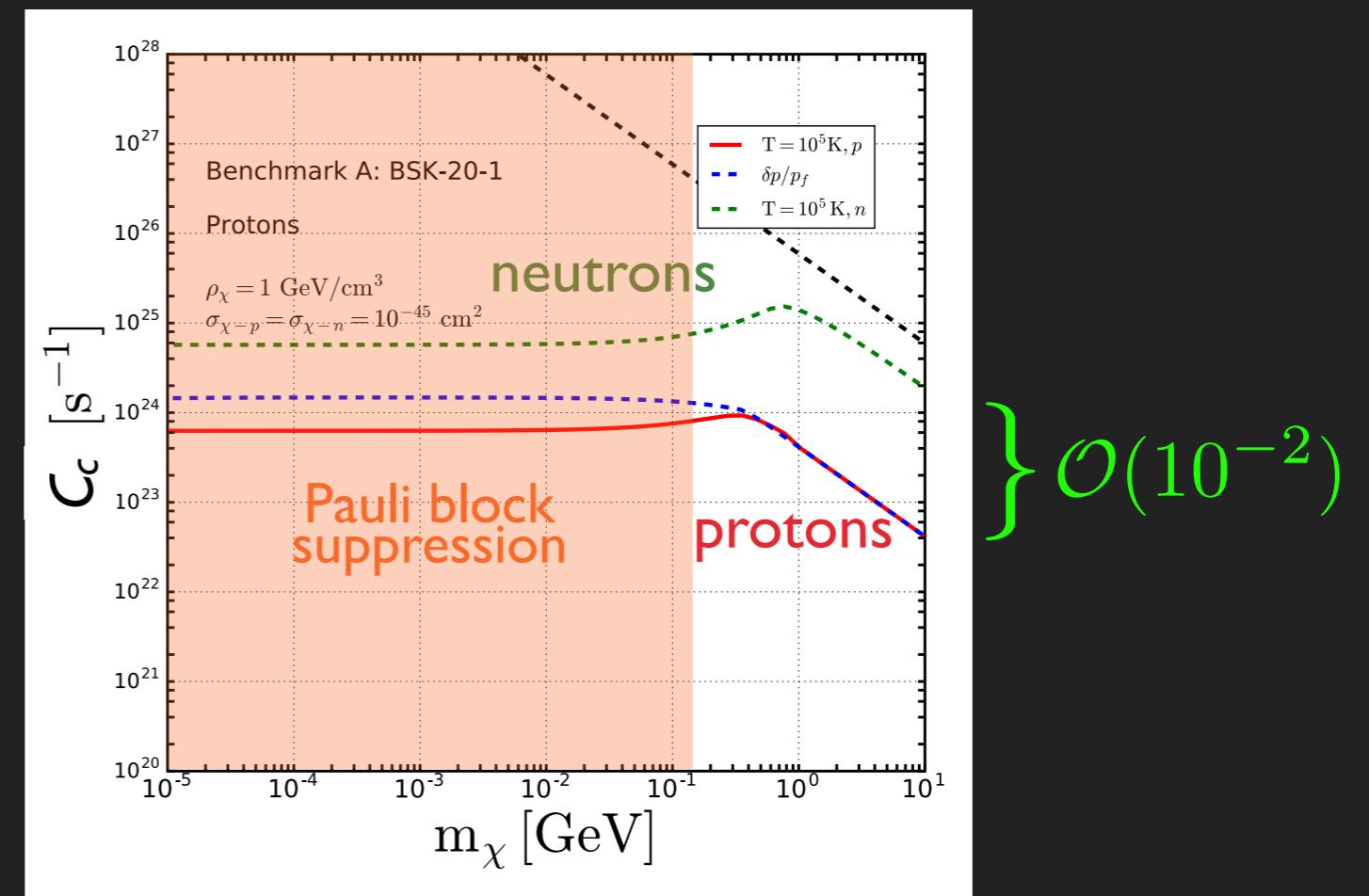
R. Garani *et al.*, JCAP **05**, 035 (2019)  
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# Baryons in the NS



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R. Garani *et al.*, JCAP **05**, 035 (2019)  
(private communication)

# DM-baryon interactions

neutron

G. Jungman *et al.*, *Phys. Rept.* **267**, 195 (1995)

$$\sigma_{\chi n} = \frac{4\mu_n^2}{\pi} f_n^2$$

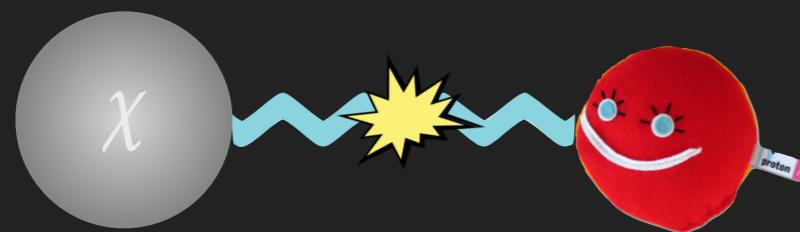
proton



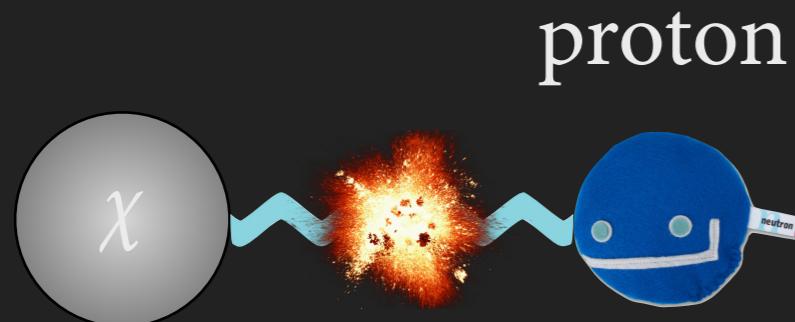
$$\sigma_{\chi p} = \frac{4\mu_p^2}{\pi} f_p^2$$

# DM-baryon interactions

neutron

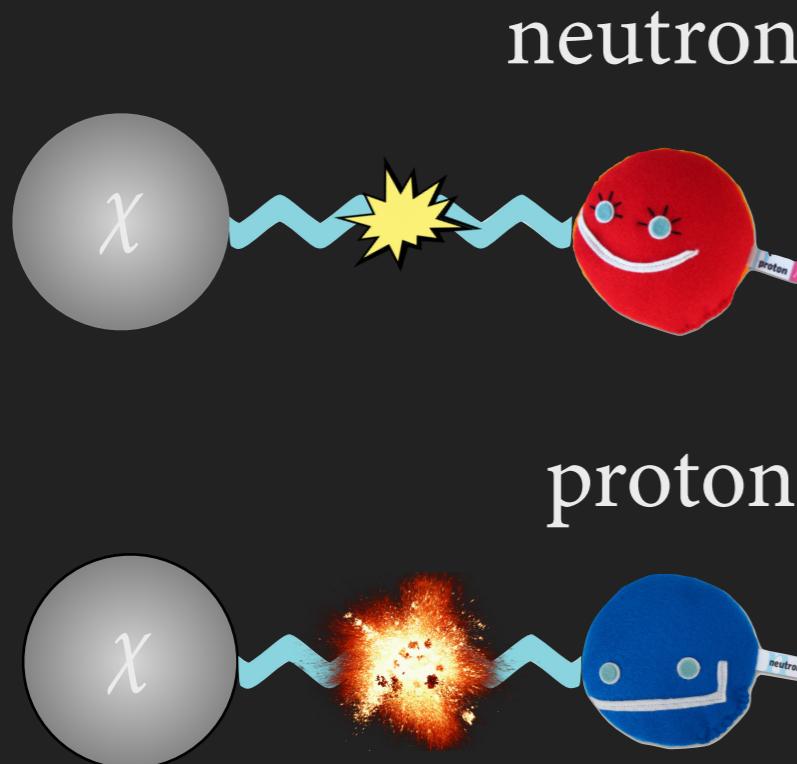
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~~|||~~

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# DM-baryon interactions



G. Jungman *et al.*, *Phys. Rept.* **267**, 195 (1995)

$$\left. \begin{aligned} \sigma_{\chi n} &= \frac{4\mu_n^2}{\pi} f_n^2 \\ \sigma_{\chi p} &= \frac{4\mu_p^2}{\pi} f_p^2 \end{aligned} \right\} \text{isospin violation}$$

# DM-baryon interactions

neutron



proton



$$\sigma_{\chi p} = \left( \frac{f_n}{f_p} \right)^{-2} \sigma_{\chi n}$$

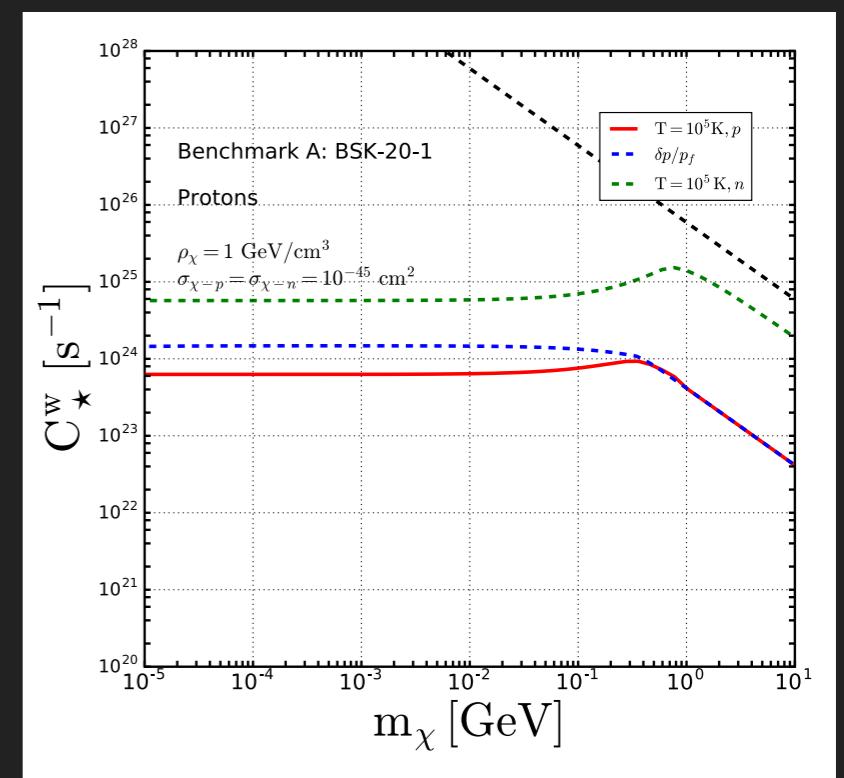
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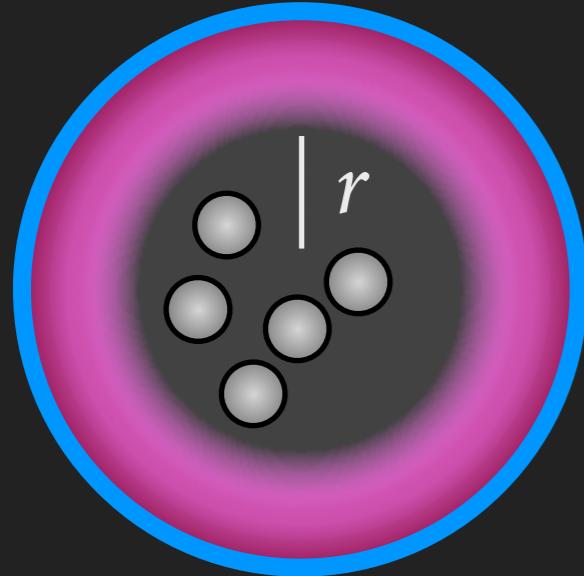
isospin violation



# DM in the NS

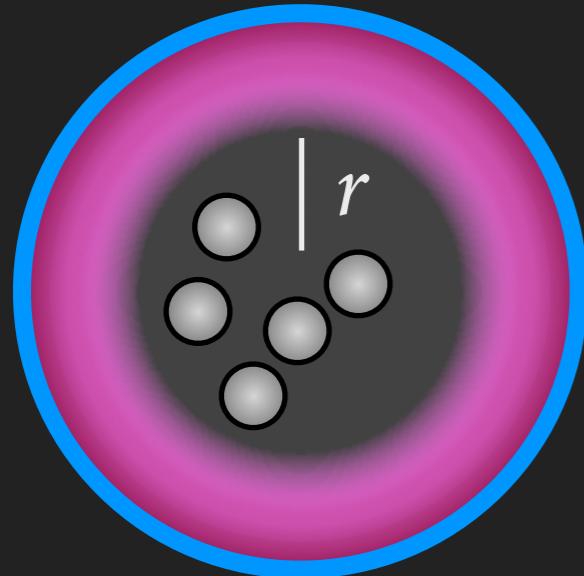
Virial theorem

$$\langle 2E_k \rangle = \frac{8}{3}\pi G \rho_b m_\chi r^2 + \frac{GN_\chi m_\chi^2}{r} + \sum_j^{N_\chi-1} \left( \frac{\alpha e^{-m_\phi r_j}}{r_j} + \alpha m_\phi e^{-m_\phi r_j} \right)$$



# DM in the NS

Virial theorem

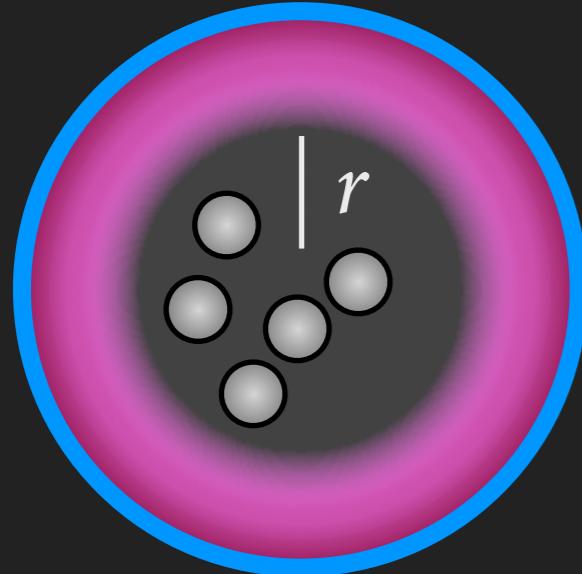


$$\langle 2E_k \rangle = \frac{8}{3}\pi G \rho_b m_\chi r^2 + \frac{GN_\chi m_\chi^2}{r} + \boxed{\sum_j^{N_\chi-1} \left( \frac{\alpha e^{-m_\phi r_j}}{r_j} + \alpha m_\phi e^{-m_\phi r_j} \right)}$$

Contribution from DM self-interaction  
modeling by Yukawa potential

# DM in the NS

Virial theorem



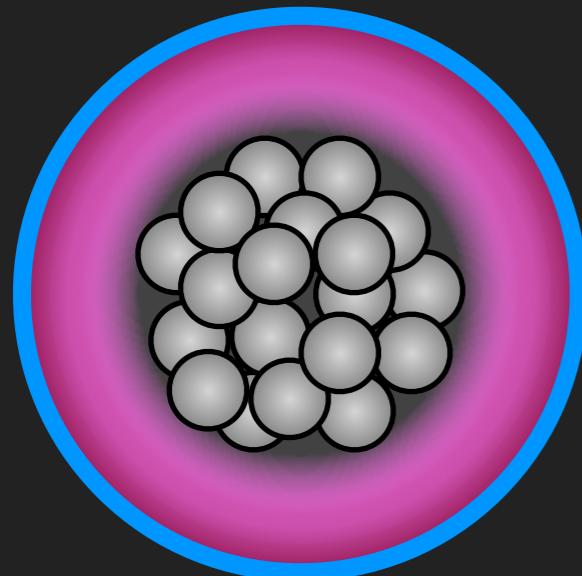
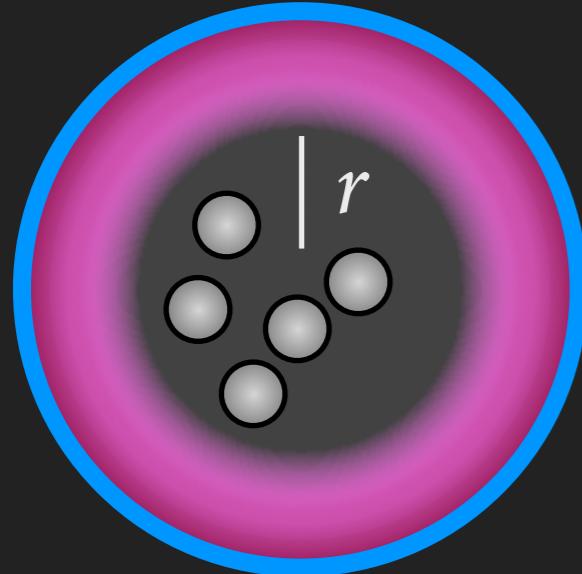
$$\langle 2E_k \rangle = \frac{8}{3}\pi G \rho_b m_\chi r^2 + \boxed{\frac{GN_\chi m_\chi^2}{r}} \quad \text{Increases as } N_\chi \text{ increasing}$$
$$+ \boxed{\sum_j^{N_\chi-1} \left( \frac{\alpha e^{-m_\phi r_j}}{r_j} + \alpha m_\phi e^{-m_\phi r_j} \right)}$$

Contribution from DM self-interaction  
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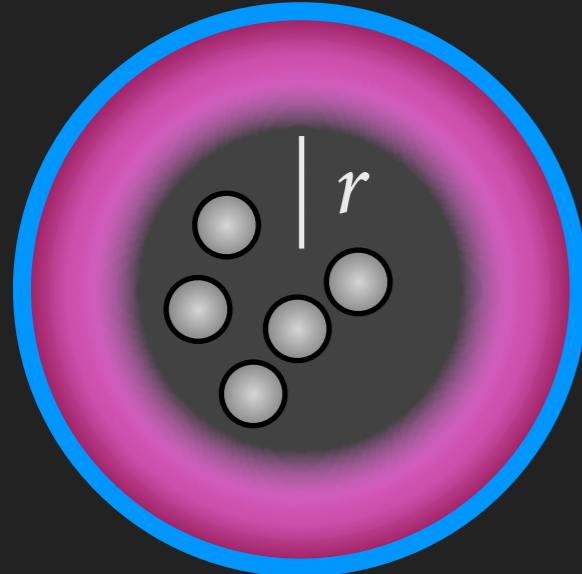
Contribution from DM self-interaction  
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# DM in the NS

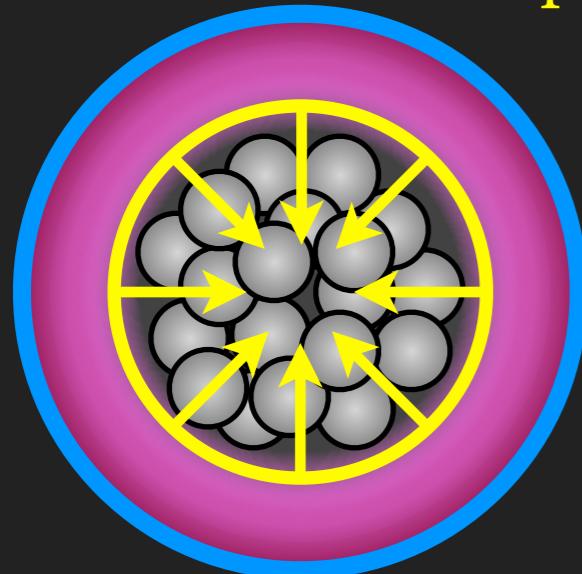
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gravitational  
collapse  $N_\chi > N_{\text{crit}}$



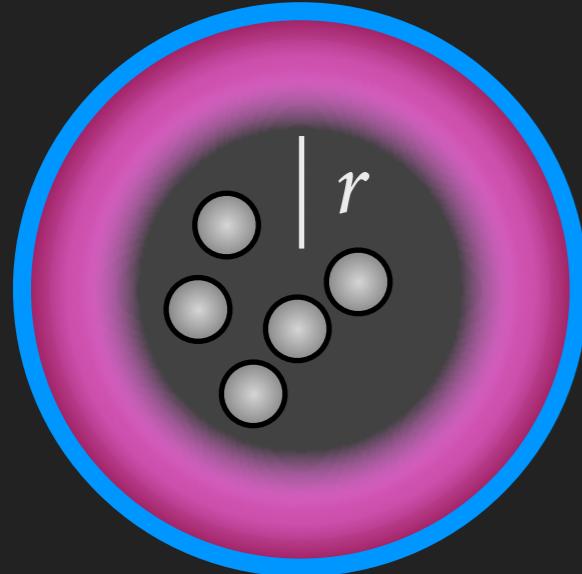
Contribution from DM self-interaction  
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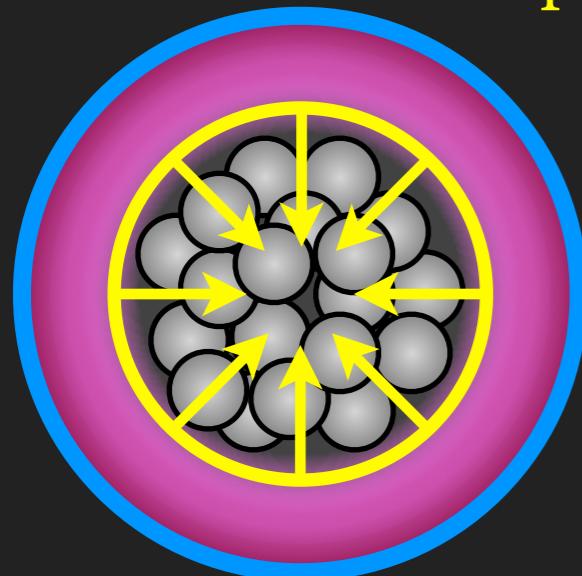
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gravitational  
collapse  $N_\chi > N_{\text{crit}}$



- { Black hole formation
- Halted by Fermi pressure

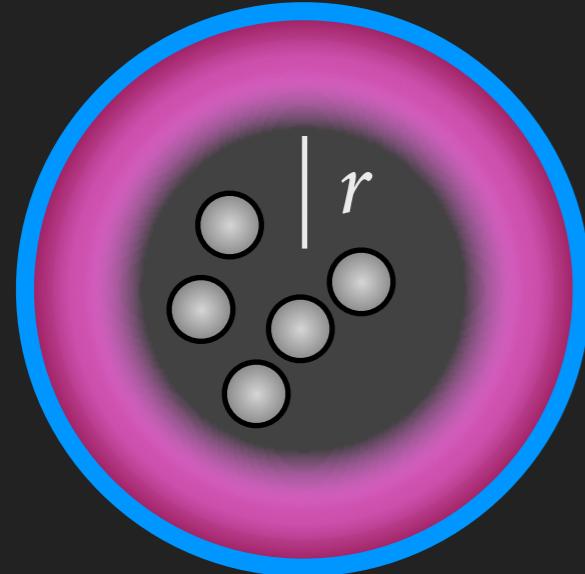
Contribution from DM self-interaction  
modeling by Yukawa potential

# DM in the NS

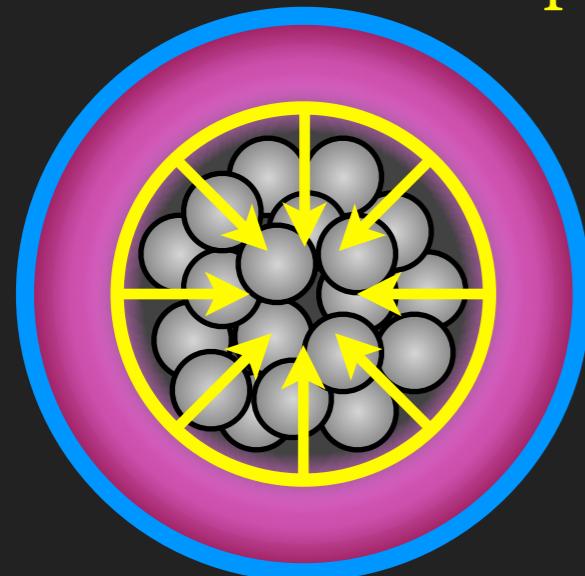
Virial theorem

$$\langle 2E_k \rangle = \frac{8}{3}\pi G \rho_b m_\chi r^2 + \boxed{\frac{GN_\chi m_\chi^2}{r}} \quad \text{Increases as } N_\chi \text{ increasing}$$

$$+ \boxed{\sum_j^{N_\chi-1} \left( \frac{\alpha e^{-m_\phi r_j}}{r_j} + \alpha m_\phi e^{-m_\phi r_j} \right)}$$



gravitational  
collapse  $N_\chi > N_{\text{crit}}$

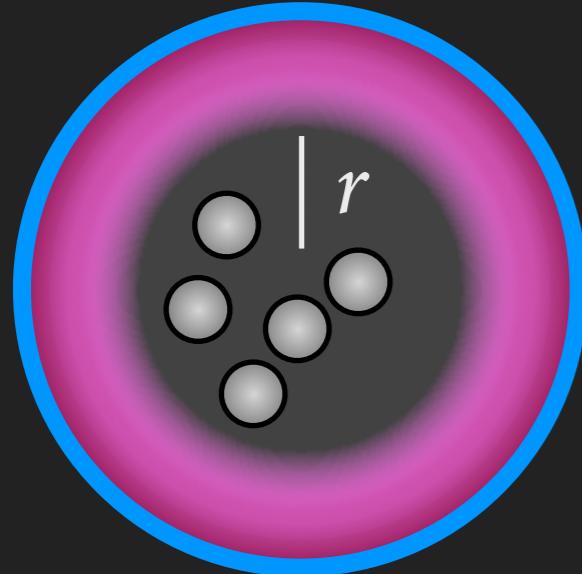


- { Black hole formation
- Halted by Fermi pressure

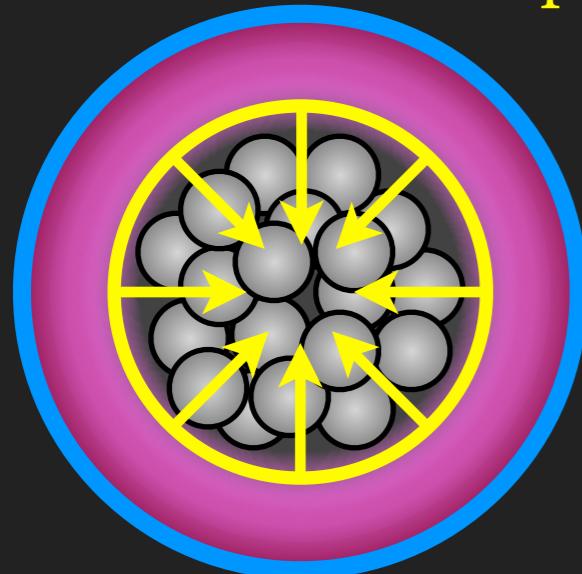
depending on  $\alpha$  and  $m_\phi$

# DM in the NS

## Virial theorem



gravitational  
collapse  $N_\chi > N_{\text{crit}}$



$$\langle 2E_k \rangle = \frac{8}{3}\pi G \rho_b m_\chi r^2 + \boxed{\frac{GN_\chi m_\chi^2}{r}} \quad \text{Increases as } N_\chi \text{ increasing}$$

$$+ \boxed{\sum_j^{N_\chi-1} \left( \frac{\alpha e^{-m_\phi r_j}}{r_j} + \alpha m_\phi e^{-m_\phi r_j} \right)}$$

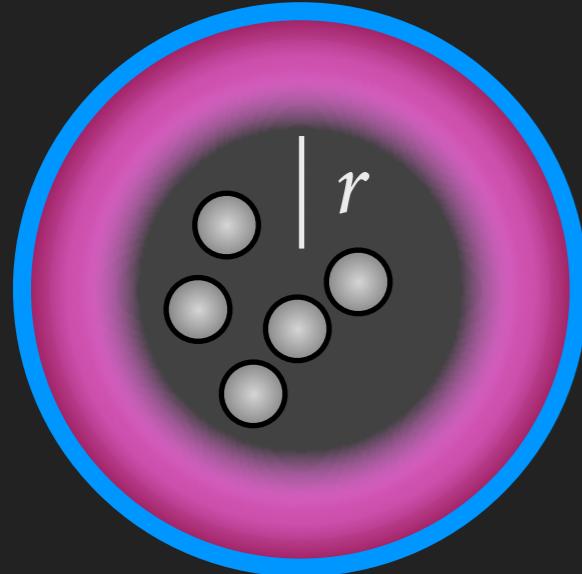
Contribution from DM self-interaction  
modeling by Yukawa potential

- |   |   |
|---|---|
| $\left\{ \begin{array}{l} \text{Black hole formation} \\ \text{Halted by Fermi pressure} \end{array} \right.$ | $\left\{ \begin{array}{l} \text{Star consumed} \\ \text{Evaporation} \end{array} \right.$ |
|---|---|

depending on  $\alpha$  and  $m_\phi$

# DM in the NS

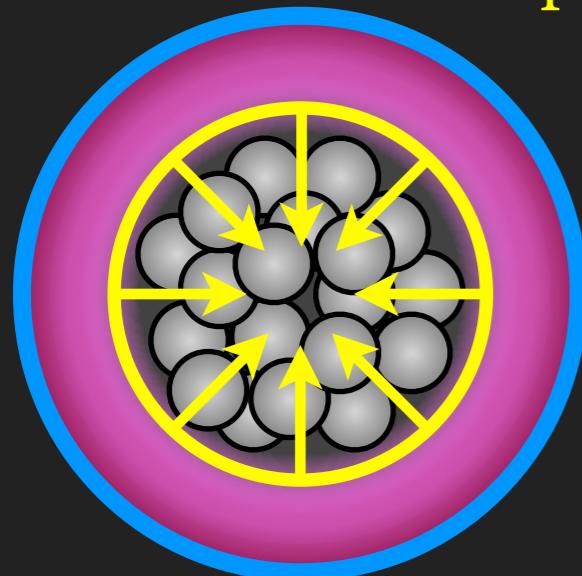
## Virial theorem



$$\langle 2E_k \rangle = \frac{8}{3}\pi G \rho_b m_\chi r^2 + \boxed{\frac{GN_\chi m_\chi^2}{r}} \quad \text{Increases as } N_\chi \text{ increasing}$$

$$+ \boxed{\sum_j^{N_\chi-1} \left( \frac{\alpha e^{-m_\phi r_j}}{r_j} + \alpha m_\phi e^{-m_\phi r_j} \right)}$$

gravitational collapse  $N_\chi > N_{\text{crit}}$



Contribution from DM self-interaction modeling by Yukawa potential

Black hole formation  
 Halted by Fermi pressure

Star consumed  $N_{\text{crit}} \gtrsim \frac{3 \times 10^{36}}{(m_\chi/\text{GeV})}$   
 Evaporation

depending on  $\alpha$  and  $m_\phi$



## Part III

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NS sensitivity on  
isospin violating  
 $\sigma_{\chi b}$

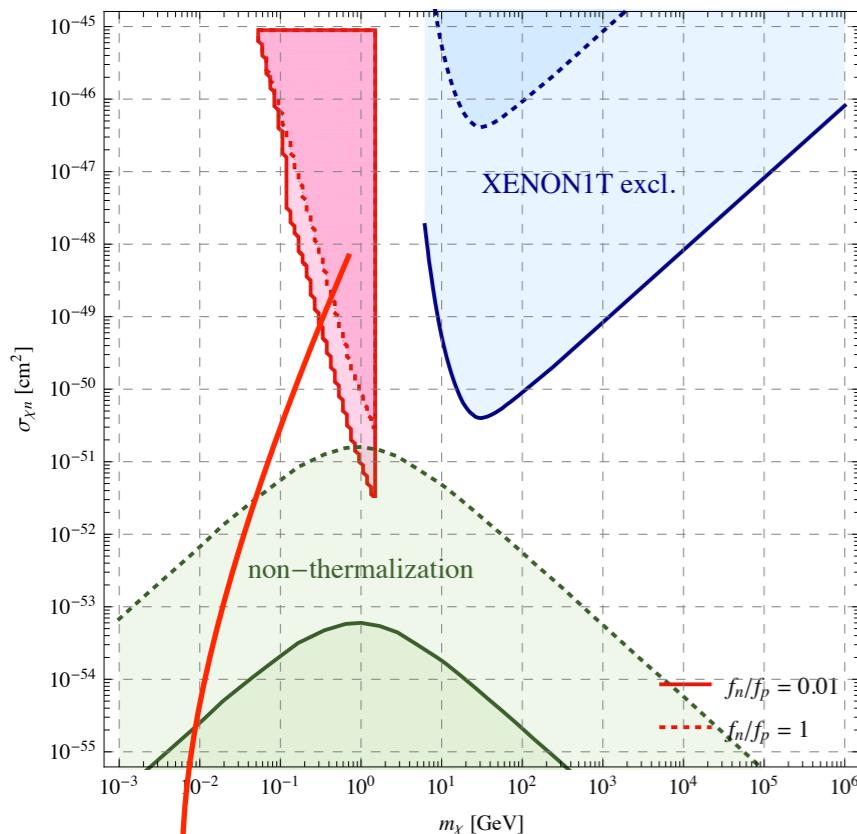
# DM-neutron cross section

age  $\sim$  Gyrs

fixed  $m_\phi = 1$  MeV

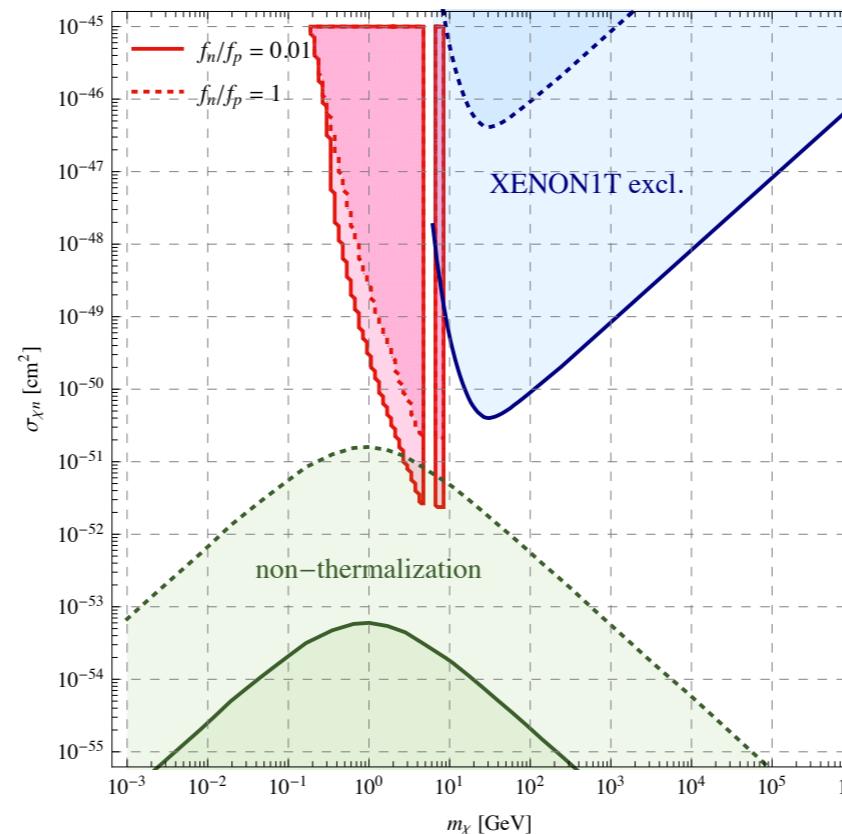
$$V(r) = \alpha_\chi \frac{e^{-m_\phi r}}{r}$$

$$\alpha_\chi = 1, m_\phi = 1 \text{ MeV}$$

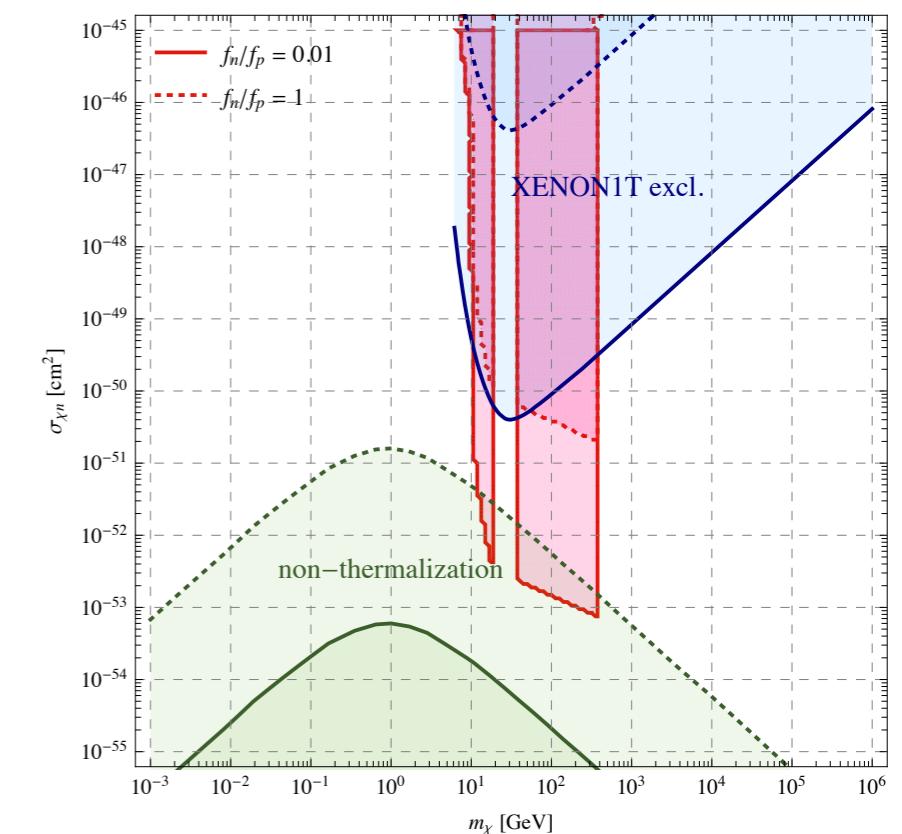


excluded

$$\alpha_\chi = 0.01, m_\phi = 1 \text{ MeV}$$



$$\alpha_\chi = 10^{-4}, m_\phi = 1 \text{ MeV}$$

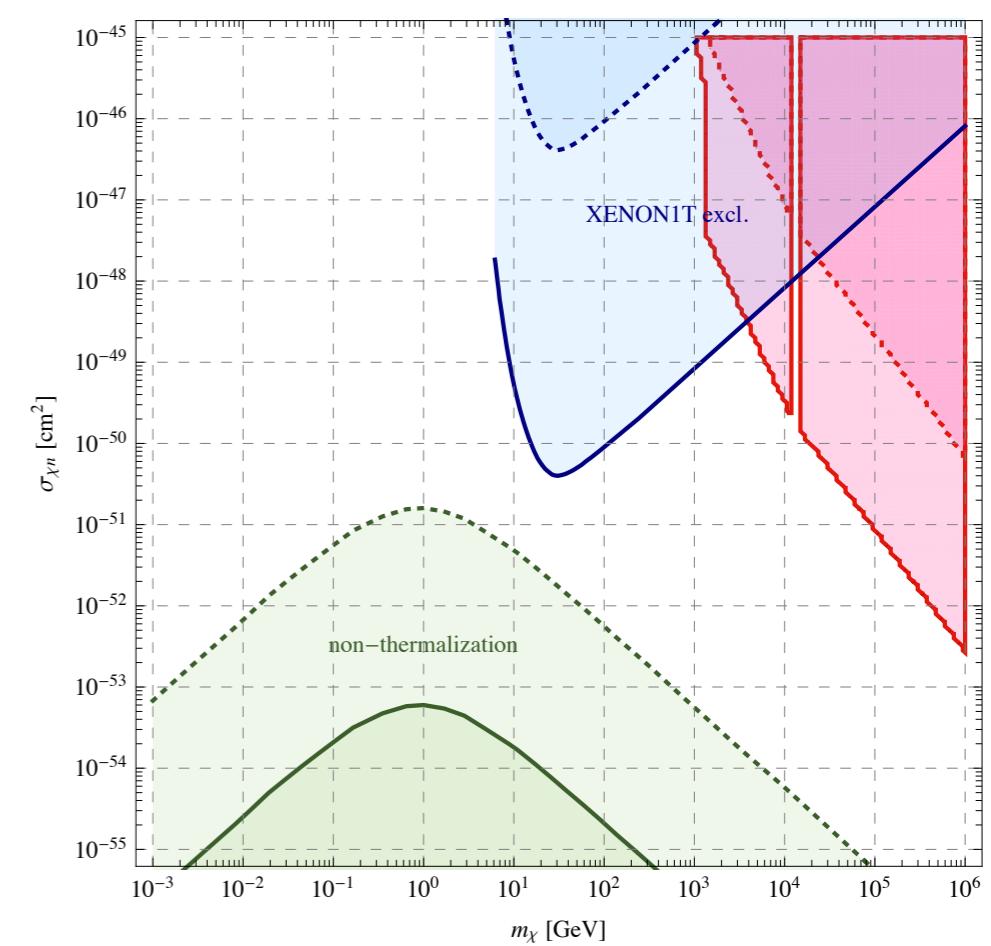
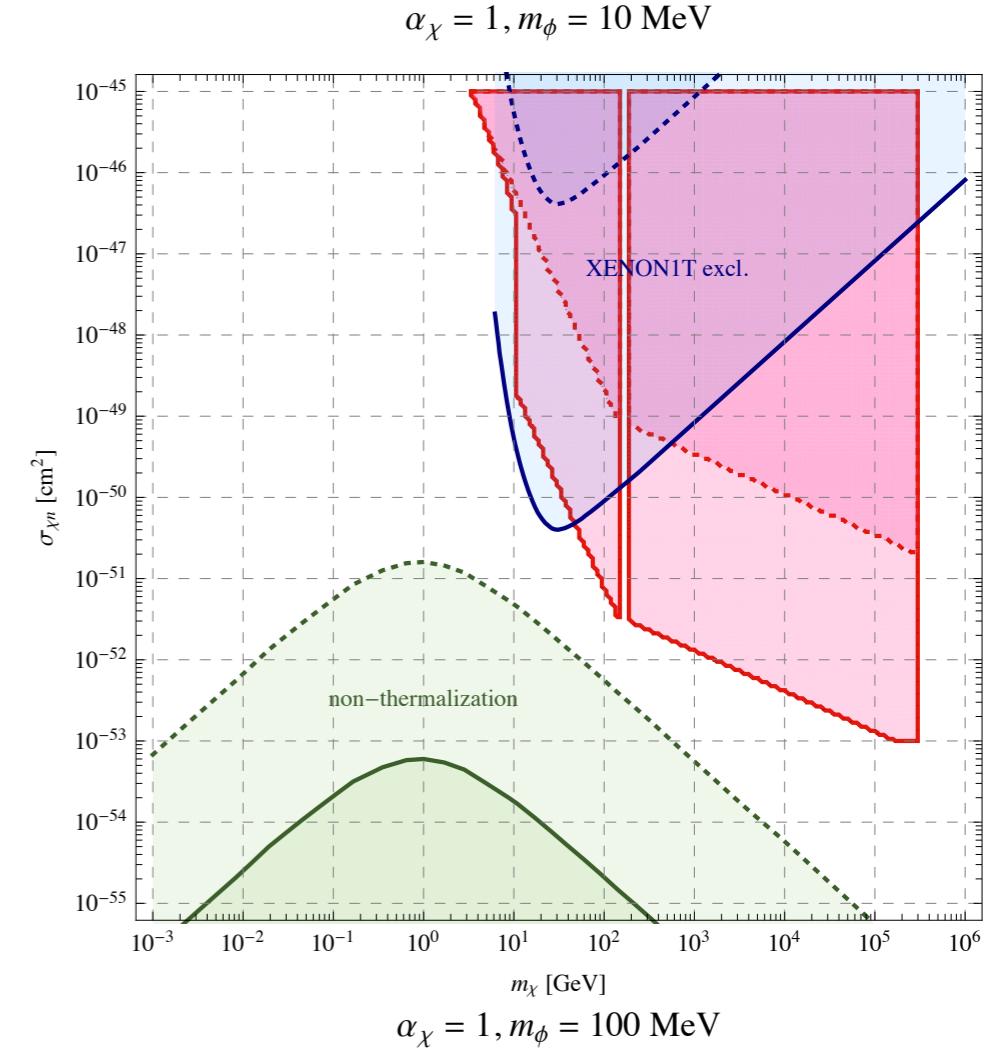
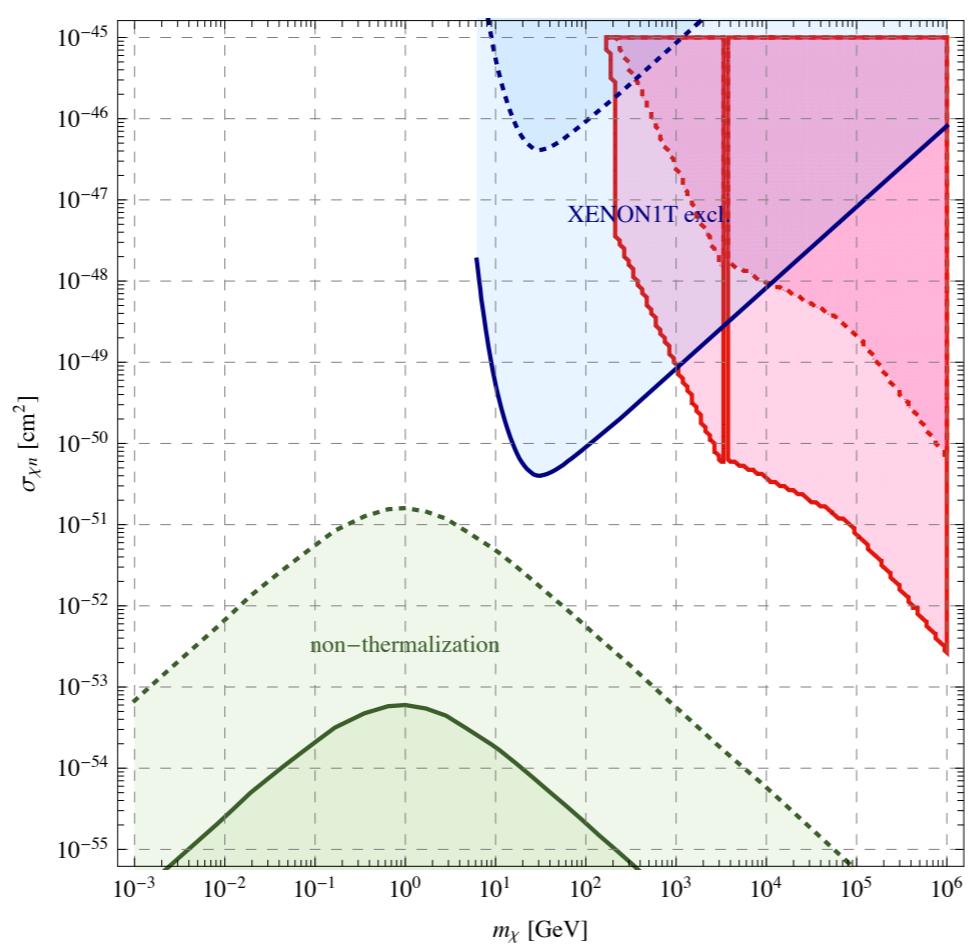
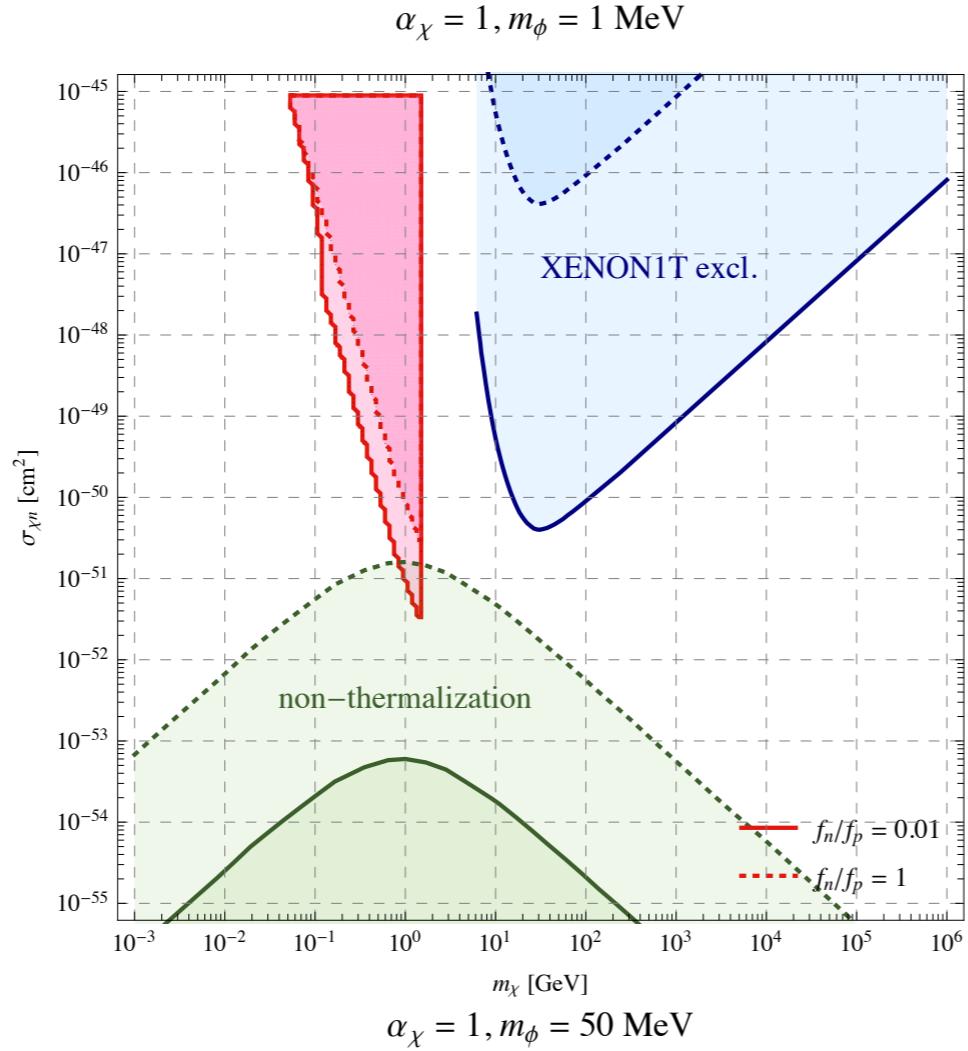


—  $f_n/f_p = 0.01$   
 .....  $f_n/f_p = 1$

**fixed**  $\alpha_\chi = 1$

$$V(r) = \alpha_\chi \frac{e^{-m_\phi r}}{r}$$

- $f_n/f_p = 0.01$
- $f_n/f_p = 1$





**Part IV**

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**Summary**

# Summary

- ▶ Isospin violation can affect the NS capture rate of DM
- ▶ Proton capture rate could be important if  $f_p > f_n$
- ▶ With attractive self-interaction, fermionic DM could overcome the Fermi pressure and form a BH in the star
- ▶ For  $m_\chi < 1$  GeV, the contributions from other light particles ( $e, \mu \dots$ ) to the capture rate in the NS could be important