

Minimal New Physics Explanation for Anomalies in Hadronic tau decays

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NCTS Annual Theory Meeting

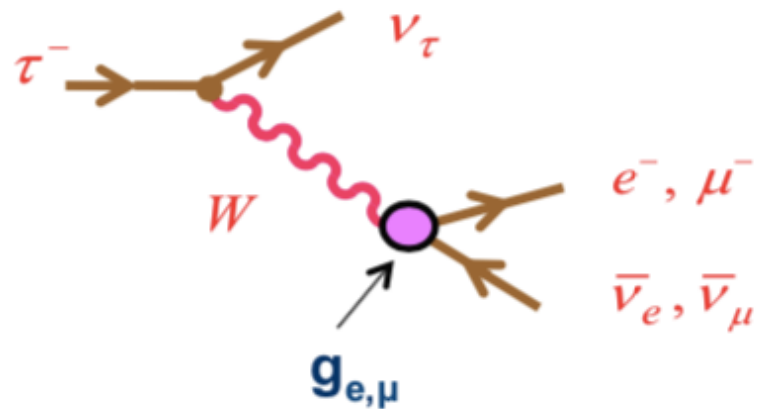
Dec 13, 2019, Hsinchu

In collaboration with Subhajit Ghosh, Amol Dighe, and Tuhin Roy

Based on [1902.09561 \(hep-ph\)](#)

Tau decays as probes of SM & beyond

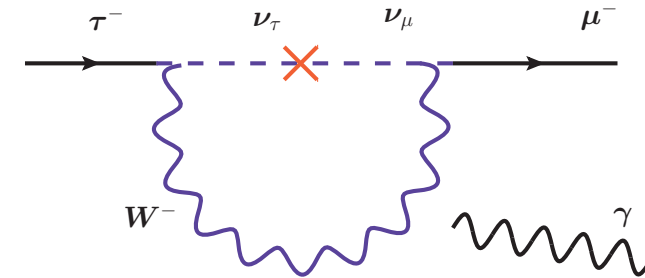
Lepton flavor universality



Charged lepton flavor violation

eg $\tau \rightarrow \mu \gamma$

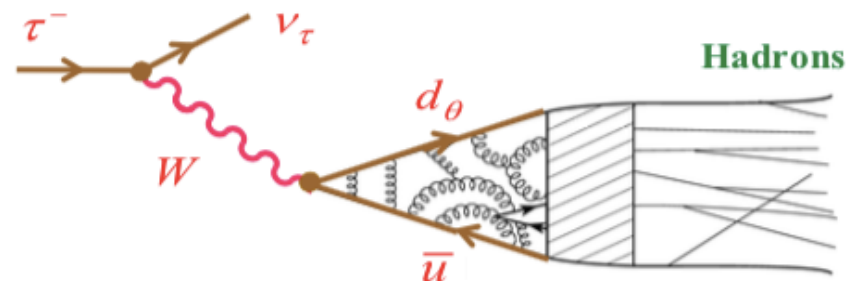
No SM background



$$\mathcal{L}_{\text{SM}} \supset \frac{g_2}{\sqrt{2}} (\bar{\tau}_L \gamma^\mu \nu_{\tau,L}) W_\mu^- + \text{h.c.}$$

Determination of the SM parameters

V_{us} , α_s , m_s



$$d_\theta = V_{ud} d + V_{us} s$$

Tests of CP violation

CP Violation in tau decays

$$A_{CP}^{\tau} = \frac{\Gamma(\tau^{+} \rightarrow \pi^{+} K_S \bar{\nu}_{\tau}) - \Gamma(\tau^{-} \rightarrow \pi^{-} K_S \nu_{\tau})}{\Gamma(\tau^{+} \rightarrow \pi^{+} K_S \bar{\nu}_{\tau}) + \Gamma(\tau^{-} \rightarrow \pi^{-} K_S \nu_{\tau})}$$

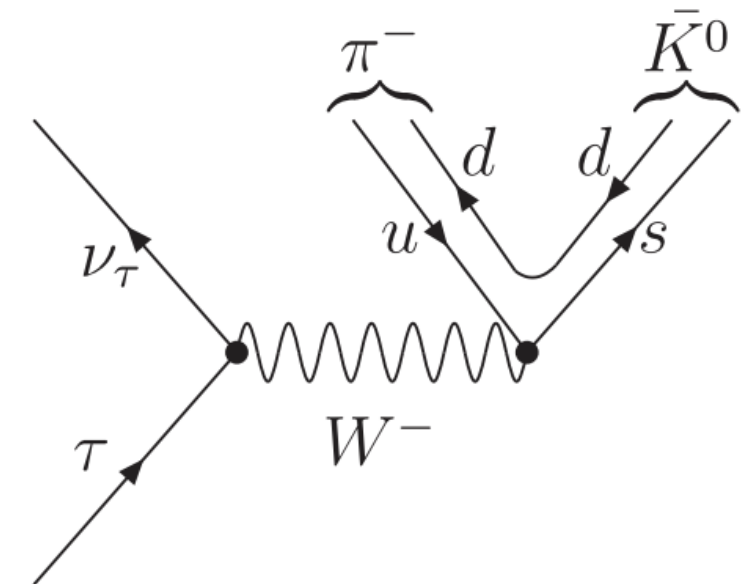
Bigi, Sanda, PLB 625, 2005

This asymmetry is nonzero in the SM, and comes from CPV in **neutral kaon mixing**

Using

$$|K_{S,L}\rangle = p|K^0\rangle \pm q|\bar{K}^0\rangle, \quad \frac{|p|^2 - |q|^2}{|p|^2 + |q|^2} \approx 2 \operatorname{Re}(\epsilon)$$

Indirect CPV parameter
($\sim 10^{-3}$)



The SM prediction is

$$A_{CP}^{\tau}(\text{SM}) \approx 2 \operatorname{Re}(\epsilon)$$

$$= (0.33 \pm 0.01) \%$$

CP Violation in tau decays

$\sim 3\sigma$ disagreement between theory and experiment

$$A_{CP}^{\tau}(\text{SM}) = (0.36 \pm 0.01) \%, \quad A_{CP}^{\tau}(\text{Exp}) = (-0.33 \pm 0.21 \pm 0.10) \%$$

BABAR Collab., 1109.1527



After taking into account exp.
conditions and time efficiencies

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After taking into account exp.
conditions and time efficiencies

A sidenote :

The same dynamics also yields **CPV** for **D meson decays**

$$A_D \equiv \frac{\Gamma(D^+ \rightarrow K_S \pi^+) - \Gamma(D^- \rightarrow K_S \pi^-)}{\Gamma(D^+ \rightarrow K_S \pi^+) + \Gamma(D^- \rightarrow K_S \pi^-)} \approx -2 \text{Re}(\epsilon)$$

Experimental and SM values for CP asymmetry in D meson are **consistent** with each other

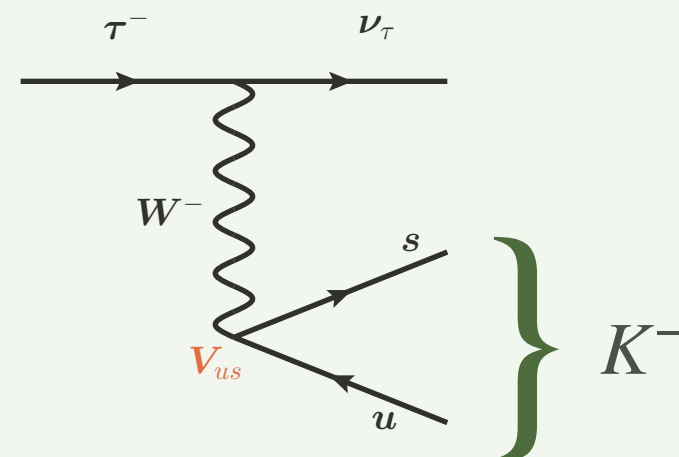
$$A_D(\text{SM}) = (-0.332 \pm 0.006) \% , \quad A_D(\text{Exp}) = (-0.41 \pm 0.09) \%$$

Extraction of V_{us}

Branching fraction	HFLAV Spring 2017 fit (%)
$K^- \nu_\tau$	0.6960 ± 0.0096
$K^- \pi^0 \nu_\tau$	0.4327 ± 0.0149
$K^- 2\pi^0 \nu_\tau$ (ex. K^0)	0.0640 ± 0.0220
$K^- 3\pi^0 \nu_\tau$ (ex. K^0, η)	0.0428 ± 0.0216
$\pi^- \bar{K}^0 \nu_\tau$	0.8386 ± 0.0141
$\pi^- \bar{K}^0 \pi^0 \nu_\tau$	0.3812 ± 0.0129
$\pi^- \bar{K}^0 \pi^0 \pi^0 \nu_\tau$ (ex. K^0)	0.0234 ± 0.0231
$\bar{K}^0 h^- h^- h^+ \nu_\tau$	0.0222 ± 0.0202
$K^- \eta \nu_\tau$	0.0155 ± 0.0008
$K^- \pi^0 \eta \nu_\tau$	0.0048 ± 0.0012
$\pi^- \bar{K}^0 \eta \nu_\tau$	0.0094 ± 0.0015
$K^- \omega \nu_\tau$	0.0410 ± 0.0092
$K^- \phi \nu_\tau$ ($\phi \rightarrow K^+ K^-$)	0.0022 ± 0.0008
$K^- \phi \nu_\tau$ ($\phi \rightarrow K_S^0 K_L^0$)	0.0015 ± 0.0006
$K^- \pi^- \pi^+ \nu_\tau$ (ex. K^0, ω)	0.2923 ± 0.0067
$K^- \pi^- \pi^+ \pi^0 \nu_\tau$ (ex. K^0, ω, η)	0.0410 ± 0.0143
$K^- 2\pi^- 2\pi^+ \nu_\tau$ (ex. K^0)	0.0001 ± 0.0001
$K^- 2\pi^- 2\pi^+ \pi^0 \nu_\tau$ (ex. K^0)	0.0001 ± 0.0001
$X_s^- \nu_\tau$	2.9087 ± 0.0482

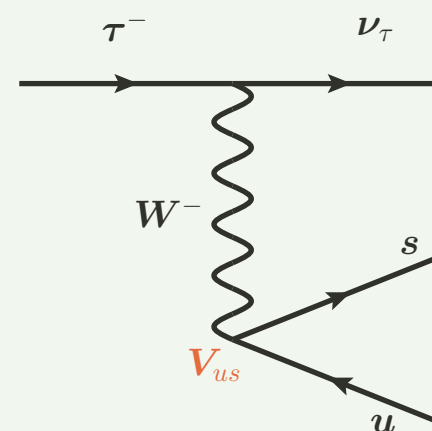
via exclusive mode:

$$\text{BR}(\tau \rightarrow K \nu_\tau) / \text{BR}(\tau \rightarrow \pi \nu_\tau)$$

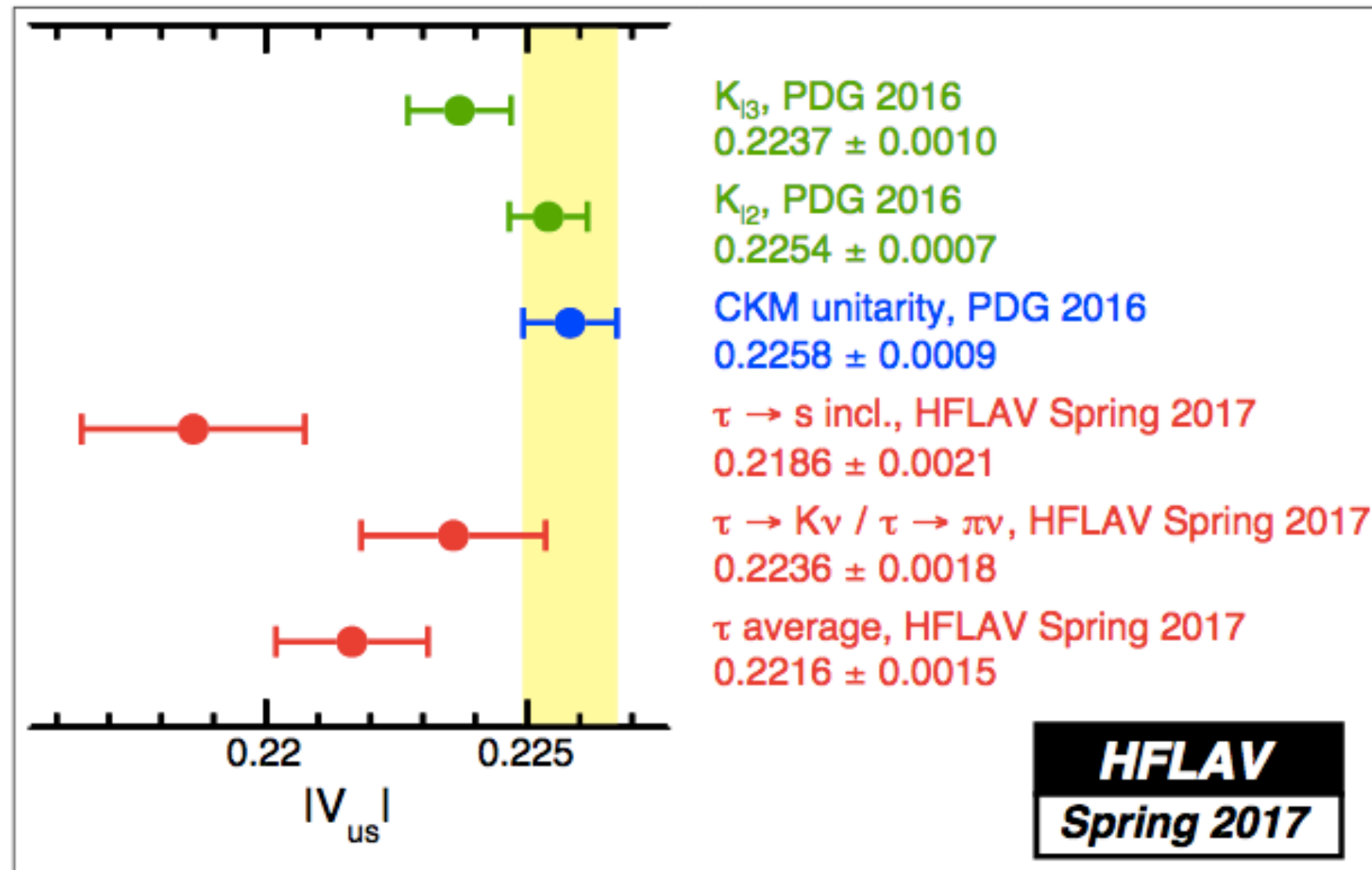


via inclusive mode:

$$\tau \rightarrow X_s + \nu_\tau$$



Status of V_{us}



$$|V_{us}|_{\text{uni}} = 0.22582(89)$$

$$\text{from } \sqrt{1 - |V_{ud}|^2} \quad (\text{CKM unitarity})$$

$$|V_{us}|_{\tau s} = 0.2186(21) \quad -3.1\sigma$$

$$\text{from } \Gamma(\tau^- \rightarrow X_s^- \nu_\tau)$$

$$|V_{us}|_{\tau K/\pi} = 0.2236(18) \quad -1.1\sigma$$

$$\text{from } \Gamma(\tau^- \rightarrow K^- \nu_\tau) / \Gamma(\tau^- \rightarrow \pi^- \nu_\tau)$$

New physics in $\tau \rightarrow s$?

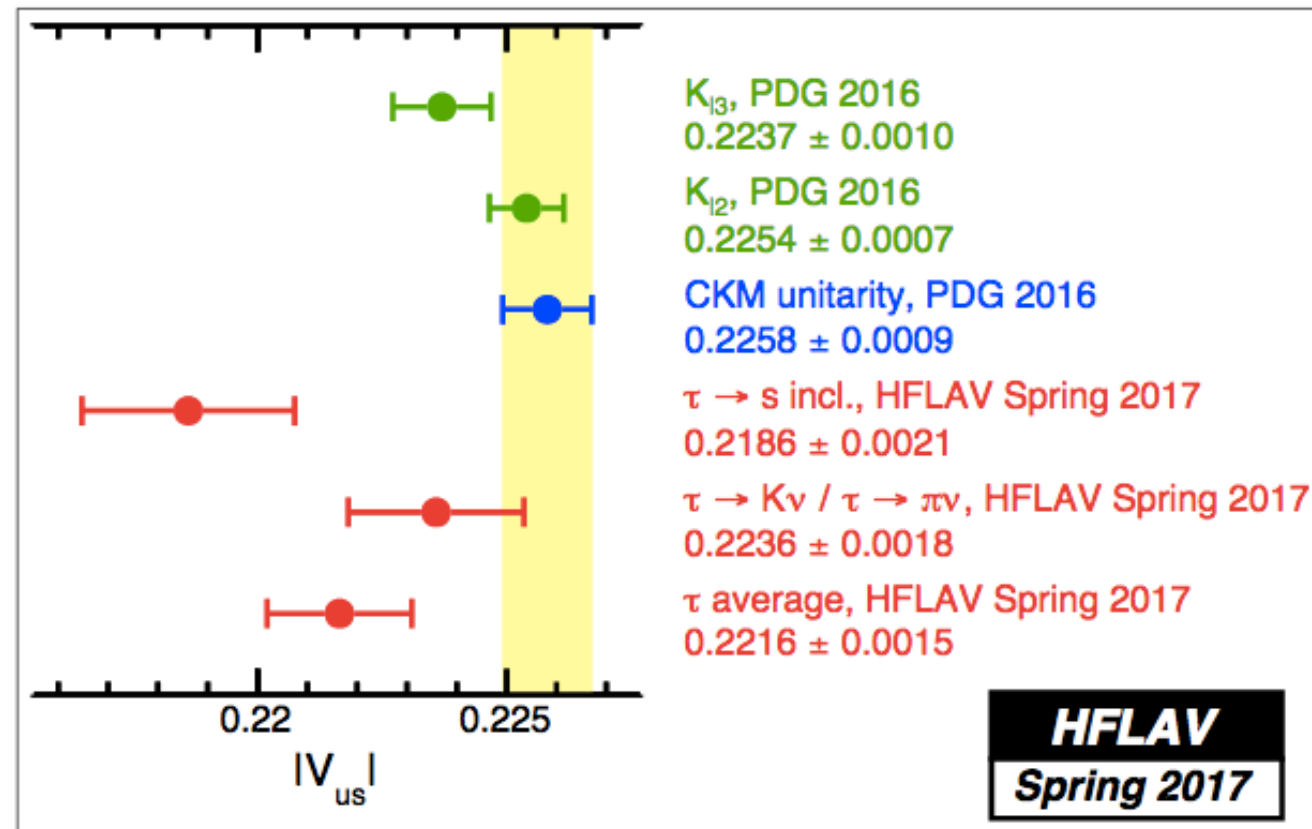
The low-energy effective Lagrangian

$$\mathcal{L}^{\Delta S=1} \supset -\frac{4G_F}{\sqrt{2}}V_{us} \left[\begin{aligned} & c_L^V \bar{\tau}_L \gamma^\mu \nu_{\tau L} \cdot \bar{u}_L \gamma_\mu s_L && + c_R^V \bar{\tau}_L \gamma^\mu \nu_{\tau L} \cdot \bar{u}_R \gamma_\mu s_R && \text{Vector} \\ & + c_L^S \bar{\tau}_R \nu_{\tau L} \cdot \bar{u}_R s_L && + c_R^S \bar{\tau}_R \nu_{\tau L} \cdot \bar{u}_L s_R && \text{Scalar} \\ & + c_T \bar{\tau}_R \sigma_{\mu\nu} \nu_{\tau L} \cdot \bar{u}_R \sigma_{\mu\nu} s_L && \end{aligned} \right] + \text{h.c.} \quad \text{Tensor}$$

In the SM : $c_L^V = 1$ and rest coefficients are zero

Nature of NP interaction?

V_{us} extraction from
EXCLUSIVE mode
is almost consistent



V_{us} extraction from
INCLUSIVE mode
is anomalous

NP keeps two body decay unaffected, but
modifies inclusive rate

Tensors !!



$\langle K^-(q) | \bar{s} \sigma_{\mu\nu} u | 0 \rangle = 0$ For $\tau \rightarrow K\nu$
 No antisymmetric structure is possible

Nature of NP interaction?

Need interference of two amplitudes to yield non-zero CP asymmetry

$$A_{CP} \propto |A_1 + A_2|^2 - |\bar{A}_1 + \bar{A}_2|^2$$

$$= -4 |A_1| |A_2| \sin(\delta_1^S - \delta_2^S) \sin(\delta_1^W - \delta_2^W)$$

$$A_j = |A_j| e^{i\delta_j^S} e^{i\delta_j^W}, (j = 1,2)$$

Both strong and weak phases
are necessary

$\tau \rightarrow K_S \pi^- \nu_\tau$:

$$\frac{d\Gamma}{ds} \propto \left| f_0(s) \left(c_V + \frac{s}{m_\tau(m_s - m_u)} c_S \right) \right|^2,$$

No strong phase in **scalar-vector** interference

$$\left| f_+(s) c_V - T(s) \right|^2$$

Relative strong phase in **tensor-vector** interference

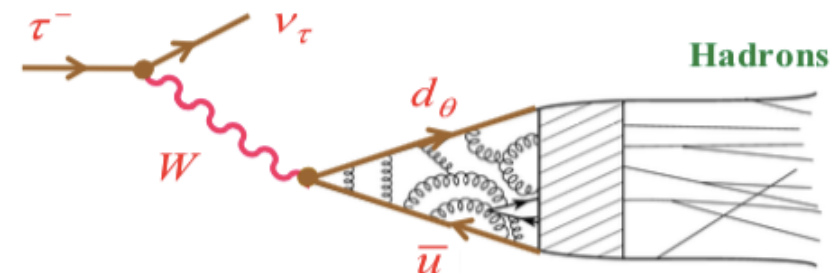
Only tensor operator can generate direct CPV !

Inclusive Hadronic Tau decay

$$\mathcal{L}_{\text{NP}} \supset -\frac{4G_F}{\sqrt{2}} V_{us} c_T \left[\bar{\tau}_R \sigma_{\mu\nu} \nu_{\tau L} \cdot \bar{u}_R \sigma_{\mu\nu} s_L \right]$$

Key observable is

$$R_\tau = \frac{\Gamma(\tau \rightarrow \nu_\tau + \text{hadrons})}{\Gamma(\tau \rightarrow \nu_\tau e^- \bar{\nu}_e)}$$



$$d_\theta = V_{ud} d + V_{us} s$$

SU(3) breaking quantity

$$\delta R_\tau \equiv \frac{R_\tau^{NS}}{|V_{ud}|^2} - \frac{R_\tau^S}{|V_{us}|^2}$$

Correction from :

$$m_s \leftrightarrow m_u, \langle \bar{s}s \rangle \leftrightarrow \langle \bar{u}u \rangle$$



$$\delta R_\tau^{\text{SM}} = 0.242(32)$$

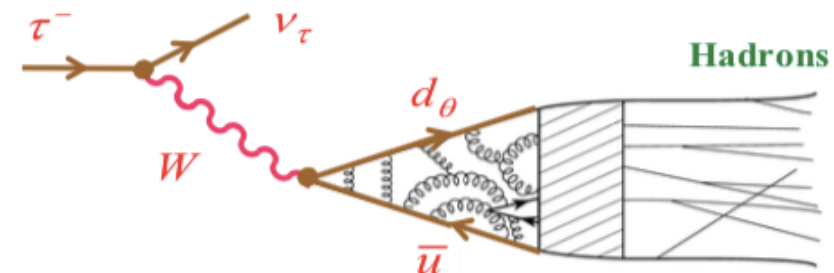
E. Gamiz et. al, PRL 94 (2005) 011803

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SU(3) breaking quantity

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In presence of
tensor contribution:

$$\delta R_{\tau, \text{theory}} \simeq \delta R_\tau^{\text{SM}} - 288\pi^2 \text{Re}[C_T] \frac{\langle 0 | \frac{1}{2}(\bar{u}u + \bar{s}s) | 0 \rangle}{m_\tau^3} - 18|C_T|^2$$

Pure tensor term

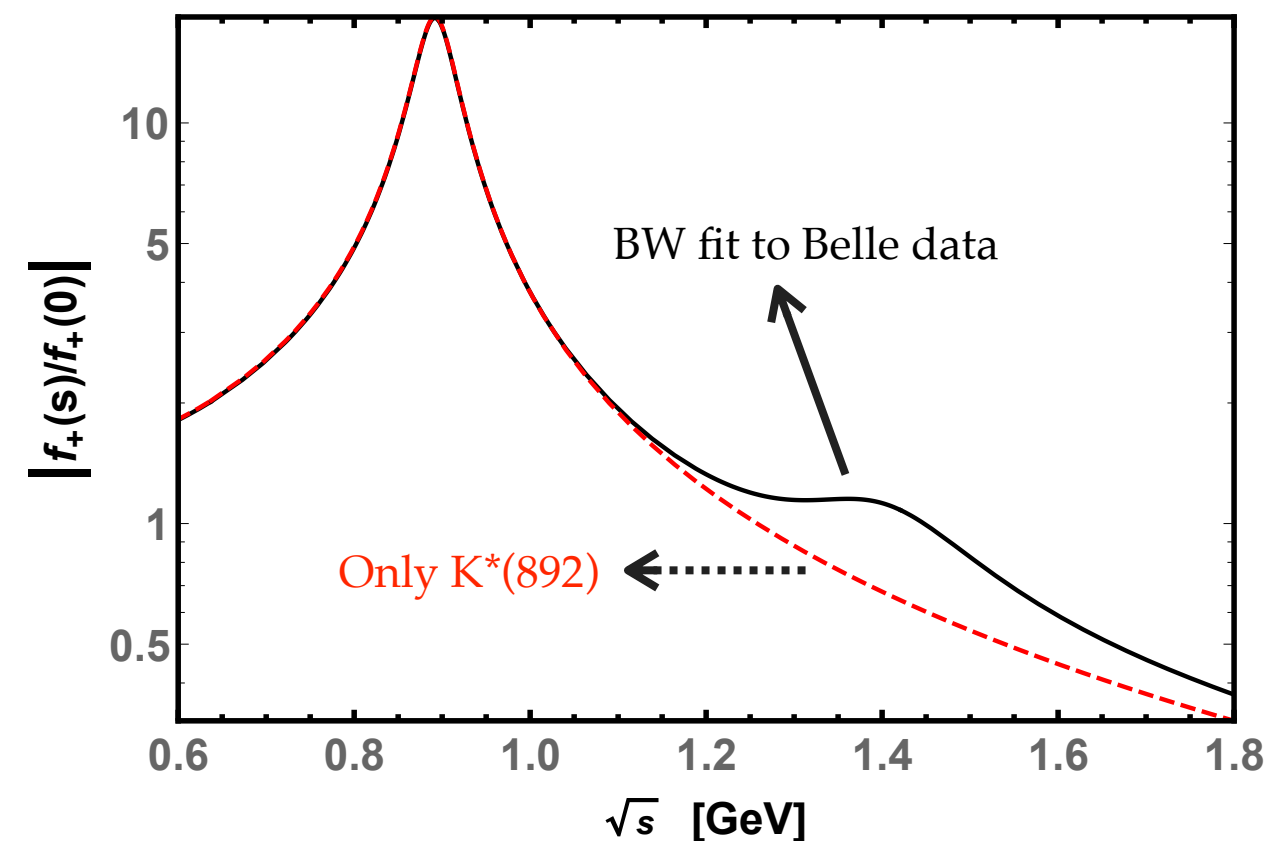
V-T interference term

CPV in $\tau \rightarrow K_S \pi^- \nu_\tau$

$$A_{CP}^\tau = \frac{\Gamma(\tau^+ \rightarrow \pi^+ K_S \bar{\nu}_\tau) - \Gamma(\tau^- \rightarrow \pi^- K_S \nu_\tau)}{\Gamma(\tau^+ \rightarrow \pi^+ K_S \bar{\nu}_\tau) + \Gamma(\tau^- \rightarrow \pi^- K_S \nu_\tau)}$$

Devi, Dhargyal, Sinha,
PRD 90, 013016 (2014)

$$A_{CP}^{\tau, \text{BSM}} = \frac{\sin \delta_T^W |c_T|}{\Gamma_\tau \text{BR}(\tau \rightarrow K_S \pi \nu_\tau)} \times \int_{s_{\pi K}}^{m_\tau^2} ds' \kappa(s) |f_+(s')| |B_T(s')| \sin[\delta_+(s') - \delta_T(s')]$$



Vector and Tensor Form factors :

Contribution from $K^*(892)$ and $K^*(1410)$,
dominated by elastic $K^*(892)$ resonance

Can be parametrised by **Omnes function**

$$\Omega(s) = \exp \left\{ \frac{s}{\pi} \int_{s_{\pi K}}^{\infty} \frac{\delta(s')}{s'(s' - s)} \right\}$$

In elastic region: Watson final state theorem
Phys. Rev. 95 (1954) 228

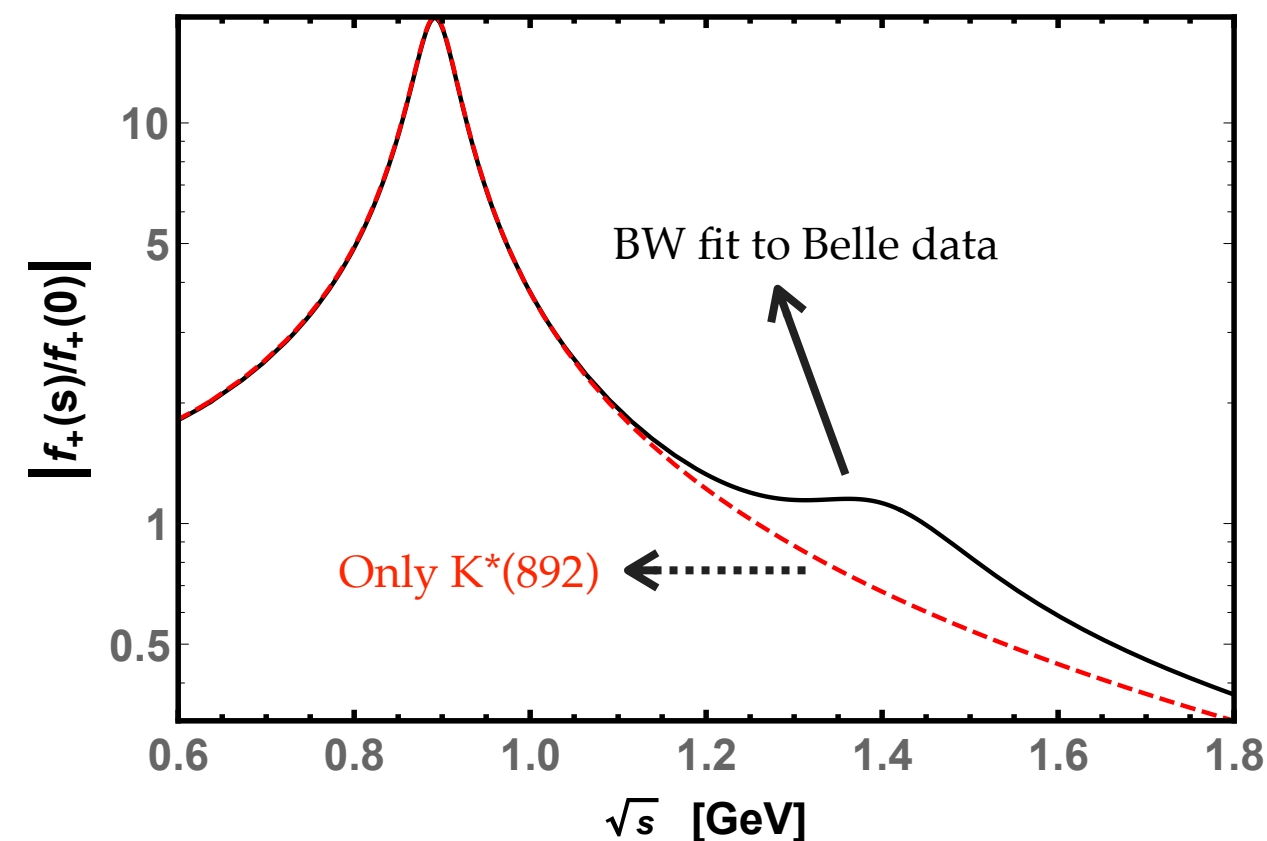
$$\delta_+(s) = \delta_T(s) = \delta_1^{1/2}(s)$$

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$$\delta_+(s) = \delta_T(s) = \delta_1^{1/2}(s)$$

Vector-Tensor interference vanishes up to inelastic corrections!!

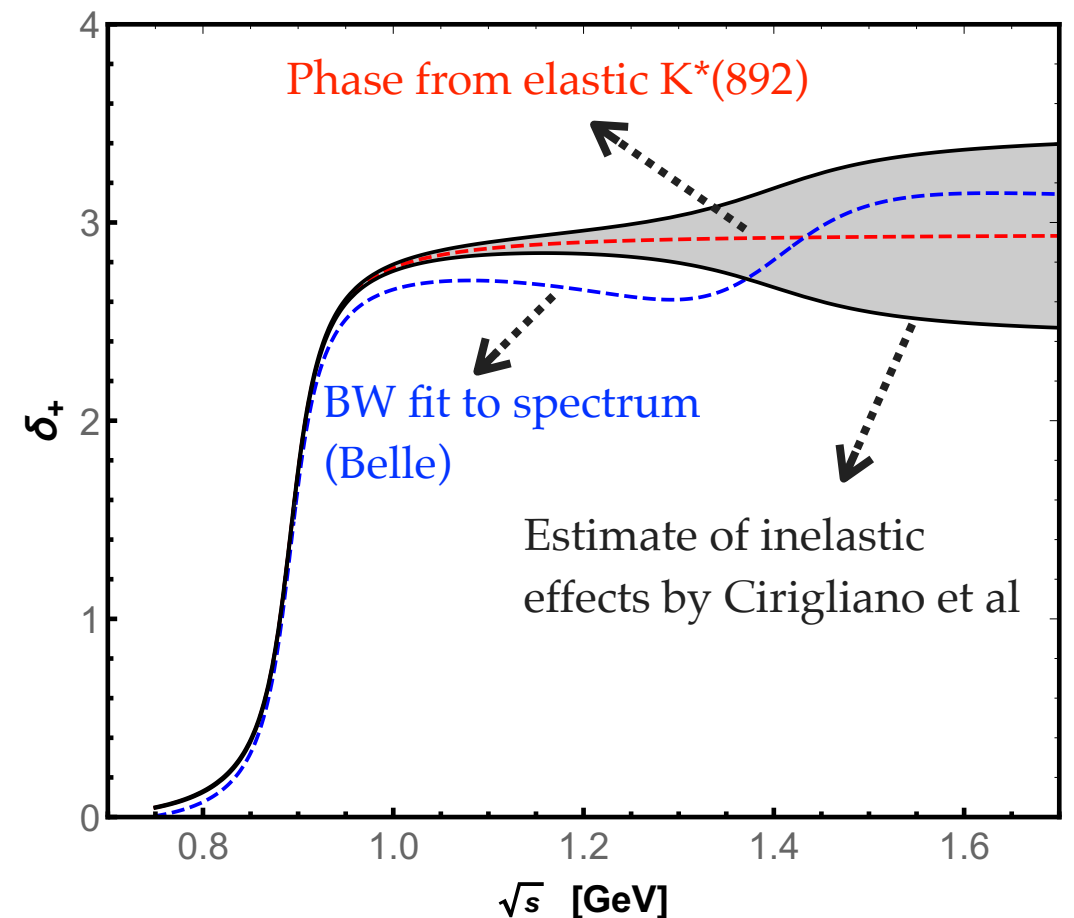
CPV in $\tau \rightarrow K_S \pi^- \nu_\tau$

Inelastic effects start around $K^*(1410)$ resonance

Inelastic phase shifts can't be extracted from experimental fits

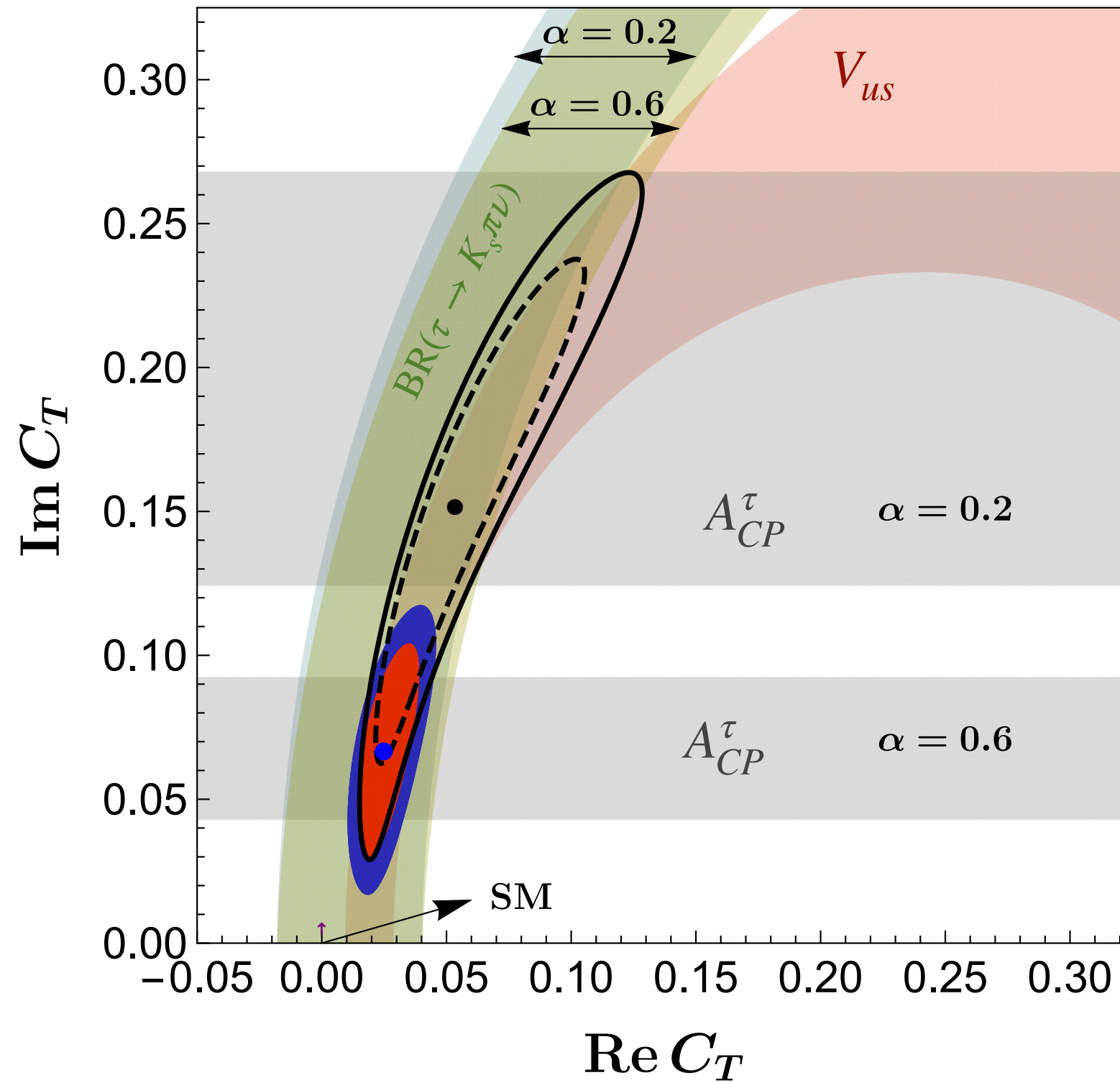
We take the following assumption:

$$\delta_T(s) - \delta_+(s) = \alpha \times \text{Arg}[\text{BW}(K^*(1410))]$$



Belle collab., PLB 654, 65 (2007)
Cirigliano et al, PRL 120, 141803 (2018)

Combined NP resolution



Implications from SM Gauge Invariance

$$\mathcal{L}_{eff}^{\text{Low-energy}} \supset c_T \bar{\tau}_R \sigma_{\mu\nu} \nu_{\tau L} \cdot \bar{u}_R \sigma_{\mu\nu} s_L$$

$$m_\tau \ll v < \Lambda$$

EW gauge inv.

$$\mathcal{L}_T \supset \frac{C}{\Lambda^2} \bar{\ell}^i \sigma_{\mu\nu} e_R \epsilon^{ij} \bar{q}_L^j \sigma^{\mu\nu} u_R + \text{h.c.}$$

$$\ell_3 = \begin{pmatrix} \nu_\tau \\ \tau_L \end{pmatrix}$$

$$q_2 = \begin{pmatrix} c_L \\ s_L \end{pmatrix}$$

$$= \frac{C}{\Lambda^2} \left[(\bar{\nu}_{\tau,L} \sigma_{\mu\nu} \tau_R) (\bar{s}_L \sigma^{\mu\nu} u_R) - V_{us} (\bar{\tau}_L \sigma_{\mu\nu} \tau_L) (\bar{u}_L \sigma^{\mu\nu} u_R) \right] + \text{h.c.}$$

Implications from SM Gauge Invariance

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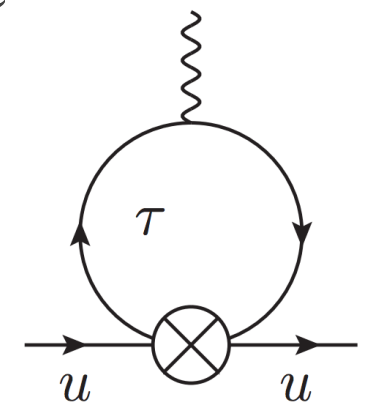
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$$= \frac{C}{\Lambda^2} \left[(\bar{\nu}_{\tau,L} \sigma_{\mu\nu} \tau_R) (\bar{s}_L \sigma^{\mu\nu} u_R) - \underline{V_{us} (\bar{\tau}_L \sigma_{\mu\nu} \tau_L) (\bar{u}_L \sigma^{\mu\nu} u_R)} \right] + \text{h.c.}$$

Bound from **neutron EDM** $|\text{Im } c_T| \lesssim 10^{-5}$



Cirigliano et al, PRL 120, 141803 (2018)

No heavy BSM explanation is possible for A_{CP} anomaly ???!

Breaking the no-go theorem !!

Matching of low energy EFT operator to
Gauge invariant operator is not unique

Breaking the no-go theorem !!

Matching of low energy EFT operator to
Gauge invariant operator is not unique

$$\begin{aligned}
 & -\frac{4G_F}{\sqrt{2}} V_{us} C_T \left[(\bar{\nu}_{\tau L} \sigma_{\mu\nu} \tau_R) (\bar{s}_L \sigma^{\mu\nu} u_R) \right] \xrightarrow{\text{EW gauge invariance}} \frac{\mathcal{K}}{\Lambda^4} \left[(\bar{\ell}_3 H^\dagger) \sigma_{\mu\nu} \tau_R \right] \left[(\bar{q}_2 H) \sigma^{\mu\nu} u_R \right] \\
 & \qquad \qquad \qquad \qquad \qquad \qquad \qquad \qquad \qquad \qquad \qquad \qquad \qquad \qquad \qquad \qquad \qquad \qquad \qquad \downarrow \\
 & \qquad \qquad \qquad \qquad \qquad \qquad \qquad \qquad \qquad \qquad \qquad \qquad \qquad \qquad \qquad \qquad \qquad \frac{\mathcal{K} v^2}{2\Lambda^4} \left[(\bar{\nu}_{\tau, L} \sigma_{\mu\nu} \tau_R) (\bar{s}_L \sigma^{\mu\nu} u_R) \right]
 \end{aligned}$$

No Neutron EDM operator
(Thanks to the Higgses)

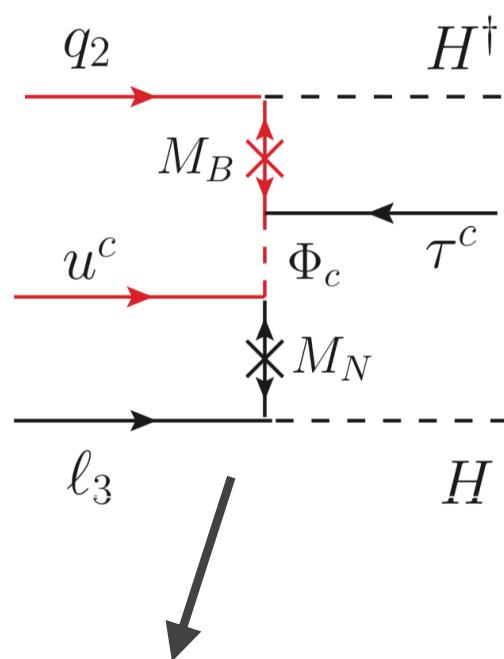
Heavy BSM explanation is possible for A_{CP} anomaly

A toy UV model

	$(SU(3)_C, SU(2)_W)_Y$	$U(1)_{q_2}$	$U(1)_{u_1}$	$U(1)_{\ell_3}$	$U(1)_{e_3}$
B	$(3, 1)_{-1/3}$	0	1	0	0
B^c	$(\bar{3}, 1)_{1/3}$	-1	0	0	0
N	$(1, 1)_0$	0	0	-1	0
N^c	$(1, 1)_0$	0	0	0	1
Φ_c	$(3, 1)_{2/3}$	0	+1	0	-1
Φ_y	$(1, 1)_1$	0	0	0	0

$$\mathcal{L} \supset k_1 H^\dagger q_2 B^c + k_2 H \ell_3 N + k_3 \Phi_c u_1^c N^c$$

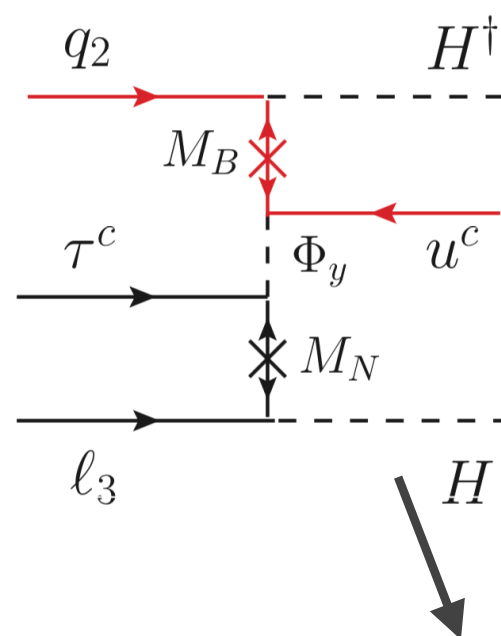
$$+ k_4 \Phi_c^\dagger e_3^c B + k_5 \Phi_y u_1^c B + k_6 \Phi_y^\dagger e_3^c N^c$$



$$\frac{4k_1 k_2 k_3 k_4}{M_N M_B m_c^2} \left[(q_2 H^\dagger e_3^c) (\ell_3 H u_1^c) \right]$$

Fierz Transformation

$$-\frac{1}{2} (q_2 H^\dagger u_1^c) (\ell_3 H e_3^c) - \frac{1}{2} (q_2 H^\dagger \sigma^{\mu\nu} u_1^c) (\ell_3 H \sigma_{\mu\nu} e_3^c)$$



$$\frac{4k_1 k_2 k_6 k_7}{M_N M_B m_y^2} \left[(q_2 H^\dagger u_1^c) (\ell_3 H e_3^c) \right]$$

Summary

Tau decays offer unique possibilities to test the SM and beyond.

We have explored the possibility of addressing the anomalies in **V_{us}** and **CP asymmetry** in tau decays via NP in a model-independent analysis.

A single effective tensor operator can account for both CP asymmetry and V_{us} anomaly.

EW gauge invariance implied constraints from neutron EDM are not general and arise only in particular class.

As a proof-of-principle, the UV model demonstrates how to generate the dim-8 gauge invariant operator, avoiding the dim-6 one that contributes to neutron EDM.

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Thank you

Back-up

τ : The Heaviest Lepton

Mass : 1776.86(12) MeV PDG 2018

Lifetime : 290.3(5) fs PDG 2018

The only known lepton heavy enough to decay into both leptons and hadrons

PDG 2018 lists 244 various decay modes of the tau

Decays to lighter leptons $\tau \rightarrow \ell \bar{\nu}_\ell \nu_\tau (\ell = e, \mu)$: 17 % each

Decays to hadrons $\tau \rightarrow \text{hadrons} + \nu_\tau$: 65 %

Largest BR $\tau^- \rightarrow \pi^- \pi^0 \nu_\tau$: 25 %

NP in Hadronic Tau decay

$$\mathcal{L}_{eff} = -\frac{4G_F}{\sqrt{2}}V_{us} \left[\bar{s}_L \gamma^\mu u_L \cdot \bar{\nu}_{\tau L} \gamma_\mu \tau_L \right] + \frac{Dv^2}{2\Lambda^4} \left[\bar{s}_L \sigma_{\mu\nu} u_R \cdot \bar{\nu}_{\tau L} \sigma^{\mu\nu} \tau_R \right]$$

$$c_T = \left(\frac{v}{\Lambda} \right)^4 \frac{D}{4V_{us}}, \quad c_T \text{ is a complex number}$$

$\text{Im } c_T$: Contributes to CP asymmetry

$\text{Re } c_T \text{ \& } \text{Im } c_T$: Contributes to $\tau \rightarrow X_s \nu_\tau$

Calculation of R_τ

$$\sum_n \Gamma(\tau \rightarrow \nu_\tau n) = \frac{1}{2m_\tau} \int \frac{d^3 p_\nu}{(2\pi)^3 2E_\nu} \frac{1}{2} \sum_{s,s'} \sum_n \int d\phi_n \left| \langle \nu_\tau n | \mathcal{H} | \tau \rangle \right|^2 (2\pi)^4 \delta^4(q - p_n)$$

Can be written in term of spectral functions using:

$$\begin{aligned} \rho_{ij,VV}^{\mu\nu} &\equiv \int d\phi_n (2\pi)^3 \delta^4(q - p_n) \sum_n \langle 0 | V_{ij}^\mu | n \rangle \langle n | V_{ij}^{\nu\dagger} | 0 \rangle \\ &= (q^\mu q^\nu - g^{\mu\nu} q^2) \rho_{ij,VV}^{(1)}(q^2) + q^\mu q^\nu \rho_{ij,VV}^{(0)}(q^2) \end{aligned}$$

Spectral functions are equal to imaginary part of the associated correlators

$$\Pi_{ij,VV}^{\mu\nu}(q) \equiv i \int d^4 x e^{iqx} \langle 0 | T \{ V_{ij}^\mu(x) V_{ij}^{\nu\dagger}(0) \} | 0 \rangle$$

Optical theorem

$$= (q^\mu q^\nu - g^{\mu\nu} q^2) \Pi_{ij,VV}^{(1)}(q^2) + q^\mu q^\nu \Pi_{ij,VV}^{(0)}(q^2)$$

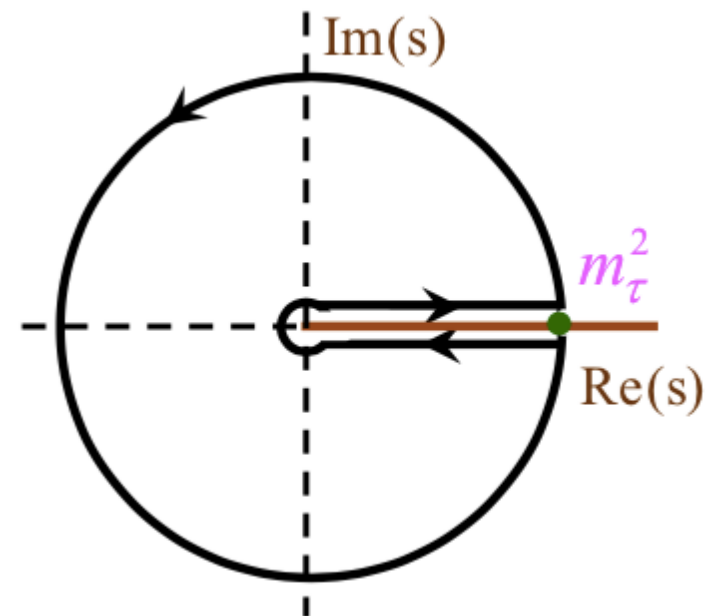
Calculation of R_τ

$$R_\tau^{S(NS)} = 12\pi |V_{us(d)}|^2 S_{EW} \int_0^{m_\tau^2} \frac{ds}{m_\tau^2} \left(1 - \frac{s}{m_\tau^2}\right) \left[\left(1 + 2\frac{s}{m_\tau^2}\right) \text{Im}\Pi^{(1)}(s) + \text{Im}\Pi^{(0)}(s) \right]$$

Braaten, Narison, Pich'92

Analyticity of Π : making use of **Cauchy theorem**

$$R_\tau^{S(NS)} = 6i\pi |V_{us(d)}|^2 S_{EW} \oint_{|s|=m_\tau^2} \frac{ds}{m_\tau^2} \left(1 - \frac{s}{m_\tau^2}\right) \left[\left(1 + 2\frac{s}{m_\tau^2}\right) \Pi^{(1)}(s) + \Pi^{(0)}(s) \right]$$



Use of OPE:

$$\Pi^J(s) = \sum_{D=2,4,\dots} \frac{1}{(-s)^{D/2}} \sum_{\dim O=D} C^{(J)}(s, \mu) \langle O_D(\mu) \rangle$$

New Physics in R_τ^S

The tensor contribution:

$$R_{\tau, BSM}^S = 6\pi i |V_{us}|^2 \oint_{|s|=m_\tau^2} \frac{ds}{m_\tau^2} \left(1 - \frac{s}{m_\tau^2}\right) \left[-12 \operatorname{Re}[C_T] \frac{\Pi_{TV}}{m_\tau} + 16 |C_T|^2 \left(1 + \frac{s}{2m_\tau^2}\right) \left(\Pi_{TT}^{(Q)} + \Pi_{TT}^{(R)}\right) \right]$$

Vector-tensor interference term

Pure tensor term

Using

$$\left. \begin{aligned} \Pi_{TV}(-Q^2) &\simeq -\frac{2}{Q^2} \langle 0 | \bar{q}q | 0 \rangle \\ \Pi_{TT}^{(Q)} = \Pi_{TT}^{(R)} &= -\frac{N_C}{24\pi^2} \log(Q^2) \end{aligned} \right\}$$

Ignored mass and α_s corrections

Craigie, Stern, PRD 26, 1982

Calculation of V_{us} in SM

$$\delta R_\tau \equiv \frac{R_\tau^{NS}}{|V_{ud}|^2} - \frac{R_\tau^S}{|V_{us}|^2} \quad : \text{SU(3) breaking quantity, depend on } m_s$$

$$\delta R_\tau \approx 24 S_{EW} \frac{m_s^2(m_\tau^2)}{m_\tau^2} \Delta(\alpha_s)$$

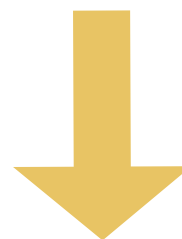
$$|V_{us}| = \sqrt{\frac{R_\tau^S}{\frac{R_\tau^{NS}}{|V_{ud}|^2} - \delta R_\tau}}$$

$$S_{EW} : \text{EW corrections,} \quad \Delta(\alpha_s) : \text{known upto } \mathcal{O}(\alpha_s^3)$$

$$\delta R_\tau = 0.242(32) \quad \text{Gamiz et al, hep-ph/0612154}$$

Experimental information

$$R_\tau^S = 0.1633(27) \quad R_\tau^{NS} = 3.4718(72) \quad |V_{ud}| = 0.97417(21) \quad \text{HFLAV report 2017}$$

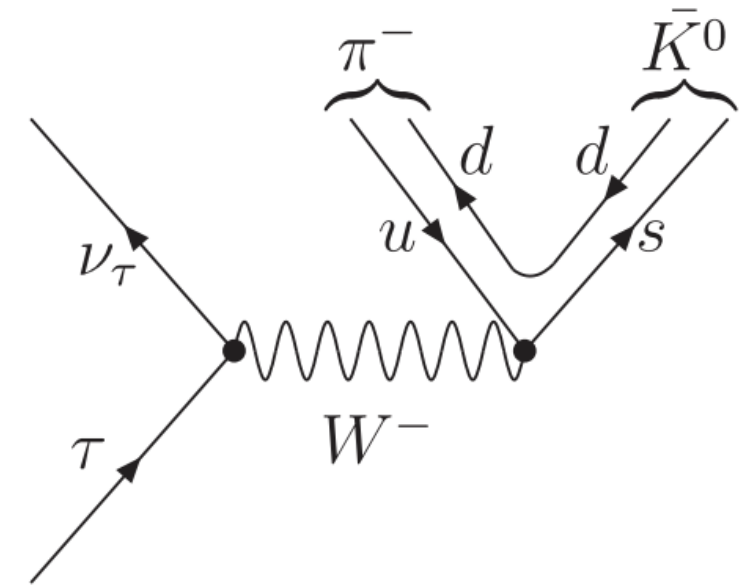


$$|V_{us}|_{\tau S} = 0.2186 \pm 0.0018_{\text{exp}} \pm 0.0010_{\text{theory}} \quad -3.1 \sigma \text{ away from unitarity!}$$

CP Violation in tau decays

In the SM, τ^+ (τ^-) decay first into a K^0 ($\bar{K}^0$) state

In experiments, intermediate K_S is not observed directly, rather defined via a final $\pi^+\pi^-$ state with $m_{\pi\pi} \approx m_K$ and decay time τ_S



Therefore, CP asymmetry depends on the integrated decay times and can be expressed as (reconstructed over a time interval $t_1 < \tau_S < t_2$)

$$A_{CP}^\tau(t_1, t_2) = \frac{\int_{t_1}^{t_2} dt [\Gamma(K^0(t) \rightarrow \pi\pi) - \Gamma(\bar{K}^0(t) \rightarrow \pi\pi)]}{\int_{t_1}^{t_2} dt [\Gamma(K^0(t) \rightarrow \pi\pi) + \Gamma(\bar{K}^0(t) \rightarrow \pi\pi)]}$$

Grossman, Nir, JHEP 04 (2012) 002

Form factors for $\tau \rightarrow K_S \pi^- \nu_\tau$

Vector and Tensor form factors are parametrized by **Omnés function**

$$\Omega(s) = \exp \left\{ \frac{s}{\pi} \int_{s_{\pi K}}^{\infty} \frac{\delta(s')}{s'(s' - s)} \right\}$$

with phase taken from Belle's fit

$$f_+(s) = f_+(0) \Omega(s),$$

$$B_T(s) = B_T(0) \Omega(s),$$

Cirigliano et al, PRL 120, 141803 (2018)

Decay Rate CP Asymmetry

BABAR result reanalysis

Measured asymmetry $A = \frac{f_1 A_1 + f_2 A_2 + f_3 A_3}{f_1 + f_2 + f_3}$

$A = (-0.27 \pm 0.18 \pm 0.08) \%$

$f_1 : \tau^- \rightarrow \pi^- K_S^0 \nu_\tau$ (signal)
 $f_2 : \tau^- \rightarrow K^- K_S^0 \nu_\tau$
 $f_3 : \tau^- \rightarrow \pi^- K^0 \bar{K}^0 \nu_\tau$

BABAR: $A_1 = -A_2 = A_Q$ (valid in SM)

$A_Q = (0.33 \pm 0.01) \%$

$A_Q = (-0.36 \pm 0.23 \pm 0.11) \%$

BABAR correction factor = 1.08

Correct extraction of asymmetry assuming NP in the signal :

Put $A_2 = (-0.33 \pm 0.01) \%$ and extract $A_1 = (-0.33 \pm 0.21 \pm 0.10) \%$