

Leptoquark effects in rare hyperon and kaon processes

Jusak Tandean

NCTS

Based on

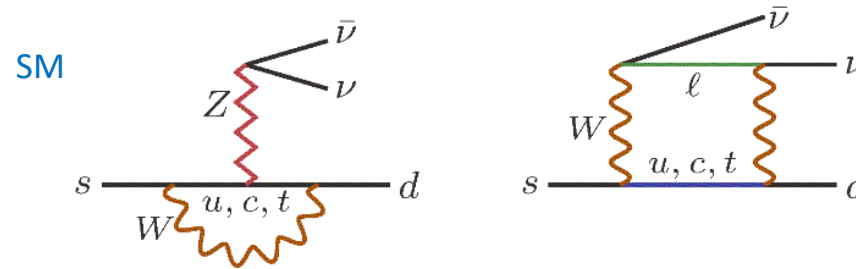
Jhih-Ying Su & JT, arXiv:1912.xxxxx

Annual Theory Meeting on Particles, Cosmology and String
National Center for Theoretical Sciences, Hsinchu, Taiwan

13 December 2019

- ❑ Introduction
 - Rare hadron decays with missing energy
- ❑ Kaon & hyperon decays as complementary probes of new ds quark interactions with invisible fermions
- ❑ Leptoquark contributions to rare hyperon and kaon decays
- ❑ Conclusions

- In the standard model (SM) the **strangeness-changing** neutral current decays of light hadrons with missing energy ($\#$) arise mainly from the loop-induced quark transition $s \rightarrow d \nu \bar{\nu}$.



- Such decays are therefore **highly suppressed** in the SM, with branching fractions of order 10^{-10} or less

➤ E.g. SM predictions:

$$\mathcal{B}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = (8.5^{+1.0}_{-1.2}) \times 10^{-11}$$

$$\mathcal{B}(K_L \rightarrow \pi^0 \nu \bar{\nu}) = (3.2^{+1.1}_{-0.7}) \times 10^{-11}$$

Bobeth & Buras, 2018

- Thus, observing significantly larger branching fractions of these processes at ongoing or upcoming experiments would likely be indicative of **new physics (NP)**.

- Measurements: $\mathcal{B}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = 1.7(1.1) \times 10^{-10}$ PDG, 2019
 $\mathcal{B}(K_L \rightarrow \pi^0 \nu \bar{\nu}) < 3.0 \times 10^{-9}$ at 90% CL KOTO, 2019
- SM predictions: $\mathcal{B}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = (8.5_{-1.2}^{+1.0}) \times 10^{-11}$ Bobeth & Buras, 2018
 $\mathcal{B}(K_L \rightarrow \pi^0 \nu \bar{\nu}) = (3.2_{-0.7}^{+1.1}) \times 10^{-11}$

- Two events in signal region observed in 2017 data
- 2016+2017 NA62 result

$$BR(K^+ \rightarrow \pi^+ \nu \nu) < 1.85 \times 10^{-10} \text{ @ 90 \% CL}$$

$$BR(K^+ \rightarrow \pi^+ \nu \nu) = 0.47^{+0.72}_{-0.47} \times 10^{-10}$$

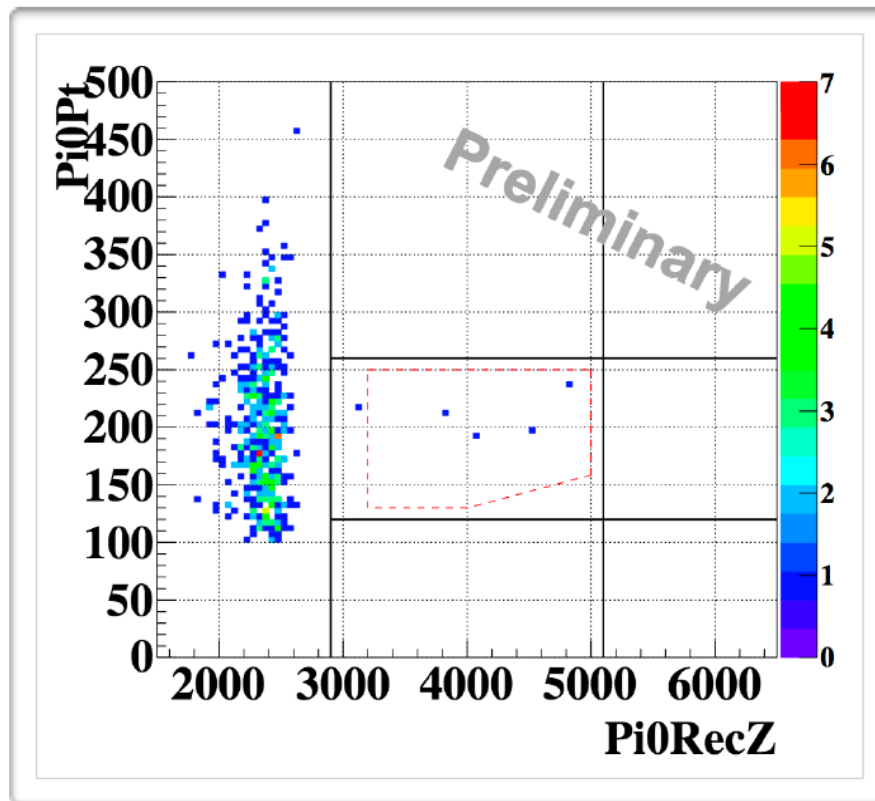
- Constraints on the largest enhancements allowed by NP models
- 2018 data analysis in progress (factor 2 more data)
 - ★ On-going studies to increase signal efficiency
- Hardware improvements foreseen from 2021 to mitigate the upstream background

R Marchevski @ PIC 2019

$K_L \rightarrow \pi^0 \nu \nu$ (2016-2018 data)

- $SES = 6.9 \times 10^{-10}$
- Four candidate events observed in the signal region.
- Will study the nature of the events inside the box.

KOTO preliminary result



Preliminary

	#BG
KLpi0pi0	<0.18
KLpi+pi-pi0	<0.02
KL3pi0 (overlapped pulse)	<0.04
Ke3 (overlapped pulse)	<0.09
KL2gamma	0.00 ± 0.00
Upstream π^0	0.00 ± 0.01
Hadron cluster	0.02 ± 0.00
CV-pi0	<0.10
CV-eta	0.03 ± 0.01
Total	0.05 ± 0.02

YC Tung @ PIC 2019

□ $K \rightarrow \pi \cancel{E}$

Measurements: $\mathcal{B}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = 1.7(1.1) \times 10^{-10}$ E949 2008, PDG 2019
 $\mathcal{B}(K_L \rightarrow \pi^0 \nu \bar{\nu}) < 3.0 \times 10^{-9}$ at 90% CL KOTO, 2019

□ $K \rightarrow \pi \pi' \cancel{E}$

Measurements: $\mathcal{B}(K^+ \rightarrow \pi^+ \pi^0 \nu \bar{\nu}) < 4.3 \times 10^{-5}$ at 90% CL E787, 2001
 $\mathcal{B}(K_L \rightarrow \pi^0 \pi^0 \nu \bar{\nu}) < 8.1 \times 10^{-7}$ at 90% CL E391a, 2011

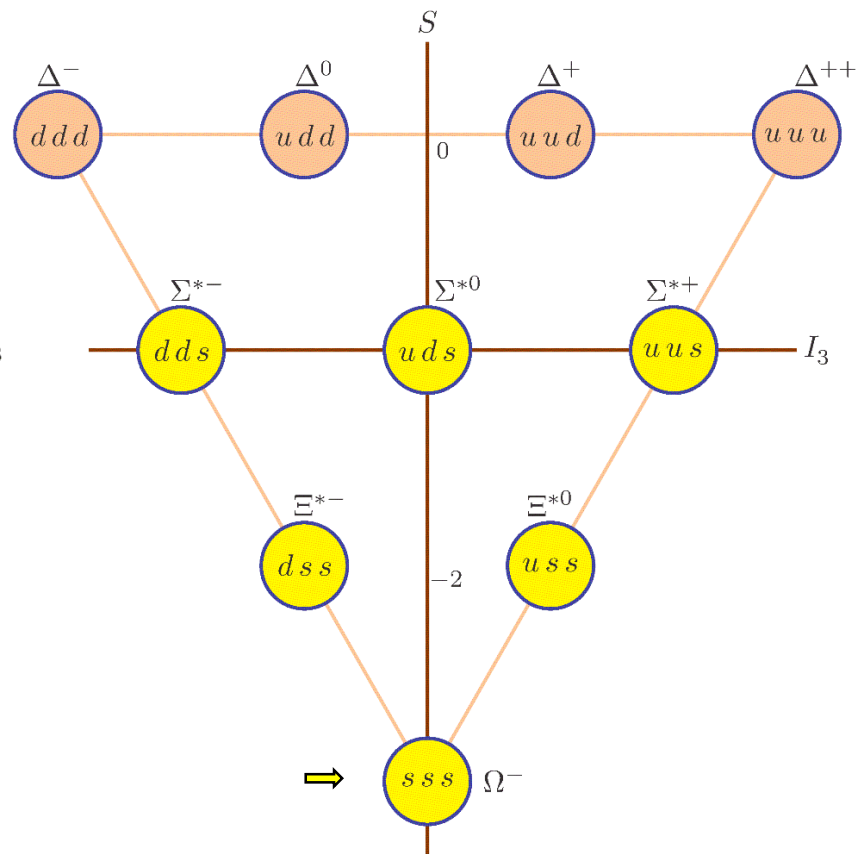
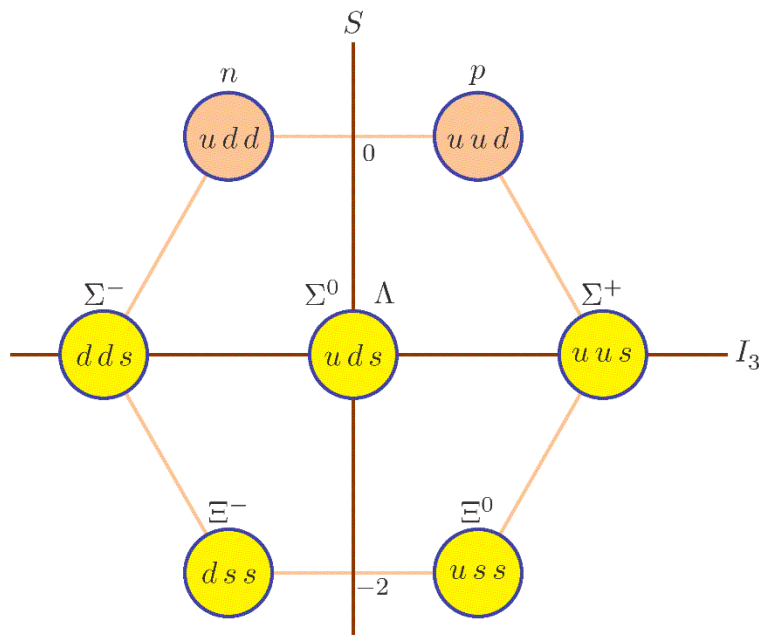
□ $K_{L,S} \rightarrow \cancel{E}$ still have no direct-search limits, but indirectly limits can be inferred from the data on their visible decay channels:

$\mathcal{B}(K_L \rightarrow \cancel{E}) < 6.3 \times 10^{-4}$ & $\mathcal{B}(K_S \rightarrow \cancel{E}) < 1.1 \times 10^{-4}$ at 95% CL Gninenko, 2015

□ No data yet in the baryon sector.

Flavor-SU(3) octet of spin-1/2 baryons & decuplet of spin-3/2 baryons

► **Hyperons**



* Effective Lagrangian for $sd\mathbf{f}\bar{\mathbf{f}}$ interactions at low energies

$$\mathcal{L}_f = - \left[\bar{d}\gamma^\eta s \bar{\mathbf{f}}\gamma_\eta (\mathbf{C}_f^V + \gamma_5 \mathbf{C}_f^A) \mathbf{f} + \bar{d}\gamma^\eta \gamma_5 s \bar{\mathbf{f}}\gamma_\eta (\tilde{\mathbf{C}}_f^V + \gamma_5 \tilde{\mathbf{C}}_f^A) \mathbf{f} \right. \\ \left. + \bar{d}s \bar{\mathbf{f}} (\mathbf{C}_f^S + \gamma_5 \mathbf{C}_f^P) \mathbf{f} + \bar{d}\gamma_5 s \bar{\mathbf{f}} (\tilde{\mathbf{C}}_f^S + \gamma_5 \tilde{\mathbf{C}}_f^P) \mathbf{f} \right] + \text{H.c.}$$

$\mathbf{f}$ describes an electrically neutral, colorless, invisible, spin- $\frac{1}{2}$, Dirac particle.

Model-independently $\mathbf{C}_f^{V,A,S,P}$ & $\tilde{\mathbf{C}}_f^{V,A,S,P}$ are generally complex free parameters.

* It contributes to $|\Delta S| = 1$ kaon and hyperon decays with missing energy.

- $K \rightarrow \pi f \bar{\mathbf{f}}$

- $K \rightarrow \pi \pi' f \bar{\mathbf{f}}$

- $K \rightarrow f \bar{\mathbf{f}}$

- $\mathfrak{B} \rightarrow \mathfrak{B}' f \bar{\mathbf{f}}$, $\mathfrak{B}\mathfrak{B}' = \Lambda n, \Sigma^+ p, \Xi^0 \Lambda, \Xi^0 \Sigma^0, \Xi^- \Sigma^-$

- $\Omega^- \rightarrow \Xi^- f \bar{\mathbf{f}}$

* $\mathcal{L}_f$ can accommodate $s \rightarrow d\nu\bar{\nu}$ in the SM, with $\mathbf{C}_\nu^V = -\mathbf{C}_\nu^A = -\tilde{\mathbf{C}}_\nu^V = \tilde{\mathbf{C}}_\nu^A$ and $\mathbf{C}_\nu^{S,P} = \tilde{\mathbf{C}}_\nu^{S,P} = 0$

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□ Mesonic matrix elements which don't vanish:

$$\langle 0 | \bar{d} \gamma^\eta \gamma_5 s | \bar{K}^0 \rangle = \langle 0 | \bar{s} \gamma^\eta \gamma_5 d | K^0 \rangle = -i f_K p_K^\eta, \quad \langle 0 | \bar{d} \gamma_5 s | \bar{K}^0 \rangle = \langle 0 | \bar{s} \gamma_5 d | K^0 \rangle = i B_0 f_K$$

$$\langle \pi^- | \bar{d} \gamma^\eta s | K^- \rangle = -\langle \pi^+ | \bar{s} \gamma^\eta d | K^+ \rangle = (p_K^\eta + p_\pi^\eta) f_+ + (f_0 - f_+) q_{K\pi}^\eta \frac{m_K^2 - m_\pi^2}{q_{K\pi}^2}$$

$$\langle \pi^- | \bar{d} s | K^- \rangle = \langle \pi^+ | \bar{s} d | K^+ \rangle = B_0 f_0, \quad B_0 = \frac{m_K^2}{\hat{m} + m_s}, \quad q_{K\pi} = p_K - p_\pi$$

$$\langle \pi^0(p_0) \pi^-(p_-) | \bar{d}(\gamma^\eta, 1) \gamma_5 s | K^- \rangle = \frac{i\sqrt{2}}{f_K} \left[(p_0^\eta - p_-^\eta, 0) + \frac{(p_0 - p_-) \cdot \tilde{q}}{m_K^2 - \tilde{q}^2} (\tilde{q}^\eta, -B_0) \right]$$

$$\langle \pi^0(p_1) \pi^0(p_2) | \bar{d}(\gamma^\eta, 1) \gamma_5 s | \bar{K}^0 \rangle = \frac{i}{f_K} \left[(p_1^\eta + p_2^\eta, 0) + \frac{(p_1 + p_2) \cdot \tilde{q}}{m_K^2 - \tilde{q}^2} (\tilde{q}^\eta, -B_0) \right]$$

f_K is the kaon decay constant, $f_{+,0}$ represent form factors depending on $q_{K\pi}^2$

$$\tilde{q} = p_{K^-} - p_0 - p_- = p_{\bar{K}^0} - p_1 - p_2$$

□ Vanishing ones:

$$\langle 0 | \bar{d}(\gamma^\eta, 1) s | \bar{K}^0 \rangle = \langle 0 | \bar{s}(\gamma^\eta, 1) d | K^0 \rangle = (0, 0)$$

$$\langle \pi^- | \bar{d}(\gamma^\eta, 1) \gamma_5 s | K^- \rangle = \langle \pi^+ | \bar{s}(\gamma^\eta, 1) \gamma_5 d | K^+ \rangle = (0, 0)$$

- The baryonic matrix elements are estimated with aid of chiral perturbation theory (χ PT) at leading order:

$$\begin{aligned}\langle \mathfrak{B}' | \bar{d} \gamma^\eta s | \mathfrak{B} \rangle &= \mathcal{V}_{\mathfrak{B}'\mathfrak{B}} \bar{u}_{\mathfrak{B}'} \gamma^\eta u_{\mathfrak{B}}, & \langle \mathfrak{B}' | \bar{d} \gamma^\eta \gamma_5 s | \mathfrak{B} \rangle &= \bar{u}_{\mathfrak{B}'} \left(\gamma^\eta \mathcal{A}_{\mathfrak{B}'\mathfrak{B}} - \frac{\mathcal{P}_{\mathfrak{B}'\mathfrak{B}}}{B_0} \mathcal{Q}^\eta \right) \gamma_5 u_{\mathfrak{B}}, \\ \langle \mathfrak{B}' | \bar{d} s | \mathfrak{B} \rangle &= \mathcal{S}_{\mathfrak{B}'\mathfrak{B}} \bar{u}_{\mathfrak{B}'} u_{\mathfrak{B}}, & \langle \mathfrak{B}' | \bar{d} \gamma_5 s | \mathfrak{B} \rangle &= \mathcal{P}_{\mathfrak{B}'\mathfrak{B}} \bar{u}_{\mathfrak{B}'} \gamma_5 u_{\mathfrak{B}}, & \mathcal{Q} &= p_{\mathfrak{B}} - p_{\mathfrak{B}'}\end{aligned}$$

$\mathfrak{B}'\mathfrak{B}$	$n\Lambda$	$p\Sigma^+$	$\Lambda\Xi^0$	$\Sigma^0\Xi^0$	$\Sigma^-\Xi^-$
$\mathcal{V}_{\mathfrak{B}'\mathfrak{B}}$	$-\sqrt{\frac{3}{2}}$	-1	$\sqrt{\frac{3}{2}}$	$\frac{-1}{\sqrt{2}}$	1
$\mathcal{A}_{\mathfrak{B}'\mathfrak{B}}$	$\frac{-1}{\sqrt{6}}(D+3F)$	$D-F$	$\frac{-1}{\sqrt{6}}(D-3F)$	$\frac{-1}{\sqrt{2}}(D+F)$	$D+F$

$$\mathcal{S}_{\mathfrak{B}'\mathfrak{B}} = \frac{m_{\mathfrak{B}} - m_{\mathfrak{B}'}}{m_s - \hat{m}} \mathcal{V}_{\mathfrak{B}'\mathfrak{B}}, \quad \mathcal{P}_{\mathfrak{B}'\mathfrak{B}} = \mathcal{A}_{\mathfrak{B}'\mathfrak{B}} B_0 \frac{m_{\mathfrak{B}'} + m_{\mathfrak{B}}}{m_K^2 - \mathcal{Q}^2}$$

$$\begin{aligned}\langle \Xi^- | \bar{d} \gamma^\eta \gamma_5 s | \Omega^- \rangle &= \mathcal{C} \bar{u}_\Xi \left(u_\Omega^\eta + \frac{\tilde{\mathcal{Q}}^\eta \tilde{\mathcal{Q}}_\kappa}{m_K^2 - \tilde{\mathcal{Q}}^2} u_\Omega^\kappa \right), & \langle \Xi^- | \bar{d} \gamma_5 s | \Omega^- \rangle &= \frac{B_0 \mathcal{C} \tilde{\mathcal{Q}}_\kappa}{\tilde{\mathcal{Q}}^2 - m_K^2} \bar{u}_\Xi u_\Omega^\kappa \\ \langle \Xi^- | \bar{d} \gamma^\eta s | \Omega^- \rangle &= \langle \Xi^- | \bar{d} s | \Omega^- \rangle = 0, & \tilde{\mathcal{Q}} &= p_{\Omega^-} - p_{\Xi^-}\end{aligned}$$

- Most of them don't vanish in leading-order χ PT.

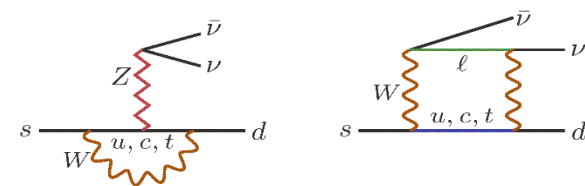
$$\square \quad \mathcal{L}_f = - \left[\bar{d} \gamma^\eta s \, \bar{f} \gamma_\eta (C_f^V + \gamma_5 C_f^A) f + \bar{d} \gamma^\eta \gamma_5 s \, \bar{f} \gamma_\eta (\tilde{C}_f^V + \gamma_5 \tilde{C}_f^A) f \right. \\ \left. + \bar{d} s \, \bar{f} (C_f^S + \gamma_5 C_f^P) f + \bar{d} \gamma_5 s \, \bar{f} (\tilde{C}_f^S + \gamma_5 \tilde{C}_f^P) f \right] + \text{H.c.}$$

Decay mode	$K \rightarrow \pi f \bar{f}$	$K \rightarrow f \bar{f}$	$K \rightarrow \pi \pi' f \bar{f}$	$\mathfrak{B} \rightarrow \mathfrak{B}' f \bar{f}$	$\Omega^- \rightarrow \Xi^- f \bar{f}$
Couplings	$C_f^{V,A,S,P}$	$\tilde{C}_f^{A,S,P}$	$\tilde{C}_f^{V,A,S,P}$	$C_f^{V,A,S,P}, \tilde{C}_f^{V,A,S,P}$	$\tilde{C}_f^{V,A,S,P}$

NP couplings affecting FCNC kaon & hyperon decays with missing energy carried by spin-1/2 fermions $f \bar{f}$ with nonzero mass, $m_f > 0$.

$\tilde{C}_f^A$ no longer contributes to $K \rightarrow f \bar{f}$ if $m_f = 0$.

SM predictions for hyperon decays with missing energy



* Lagrangian for $s \rightarrow d\nu\bar{\nu}$

$$\mathcal{L}_{\text{SM}} = \frac{-\alpha_e G_F}{\sqrt{8} \pi s_W^2} \sum_{l=e,\mu,\tau} (V_{td}^* V_{ts} X_t + V_{cd}^* V_{cs} X_c^l) \bar{d} \gamma^\eta (1 - \gamma_5) s \bar{\nu}_l \gamma_\eta (1 - \gamma_5) \nu_l + \text{H.c.}$$

$X_{t,c}$ are t - and c -quark contributions

* Branching fractions $\mathcal{B}(\mathfrak{B} \rightarrow \mathfrak{B}' \nu \bar{\nu})_{\text{SM}} = \sum_l \mathcal{B}(\mathfrak{B} \rightarrow \mathfrak{B}' \nu_l \bar{\nu}_l)_{\text{SM}}$

for $\mathfrak{B}\mathfrak{B}' = \Lambda n, \Sigma^+ p, \Xi^0 \Lambda, \Xi^0 \Sigma^0, \Xi^- \Sigma^-$

with $C_{\nu_l}^V = -C_{\nu_l}^A = -\tilde{C}_{\nu_l}^V = \tilde{C}_{\nu_l}^A = \frac{\alpha_e G_F}{\sqrt{8} \pi s_W^2} (\lambda_t X_t + \lambda_c X_c^l)$ and $C_{\nu_l}^{S,P} = \tilde{C}_{\nu_l}^{S,P} = 0$

Similarly for $\mathcal{B}(\Omega^- \rightarrow \Xi^- \nu \bar{\nu})_{\text{SM}}$

* Predictions for branching fractions

$\Lambda \rightarrow n \nu \bar{\nu}$	$\Sigma^+ \rightarrow p \nu \bar{\nu}$	$\Xi^0 \rightarrow \Lambda \nu \bar{\nu}$	$\Xi^0 \rightarrow \Sigma^0 \nu \bar{\nu}$	$\Xi^- \rightarrow \Sigma^- \nu \bar{\nu}$	$\Omega^- \rightarrow \Xi^- \nu \bar{\nu}$
7.1×10^{-13}	4.3×10^{-13}	6.3×10^{-13}	1.0×10^{-13}	1.3×10^{-13}	4.9×10^{-12}

JT, 1901.10447

* Estimated BESIII sensitivity for branching fractions

HB Li, 1612.01775

$\Lambda \rightarrow n \nu \bar{\nu}$	$\Sigma^+ \rightarrow p \nu \bar{\nu}$	$\Xi^0 \rightarrow \Lambda \nu \bar{\nu}$	$\Xi^0 \rightarrow \Sigma^0 \nu \bar{\nu}$	$\Xi^- \rightarrow \Sigma^- \nu \bar{\nu}$	$\Omega^- \rightarrow \Xi^- \nu \bar{\nu}$
3×10^{-7}	4×10^{-7}	8×10^{-7}	9×10^{-7}	—	2.6×10^{-5}

- ◆ $K_{L,S} \rightarrow \cancel{E}$ still have no direct-search limits, but indirectly upper limits on them can be inferred from the data on their **visible** decay channels:

Gninenko, 2015

$$\mathcal{B}(K_L \rightarrow \cancel{E}) < 6.3 \times 10^{-4} \quad \& \quad \mathcal{B}(K_S \rightarrow \cancel{E}) < 1.1 \times 10^{-4} \quad \text{both at 95\% CL}$$

$$\text{SM predictions: } \mathcal{B}(K_L \rightarrow \cancel{E}) \sim 1 \times 10^{-10} \quad \& \quad \mathcal{B}(K_S \rightarrow \cancel{E}) \sim 2 \times 10^{-14}$$

- ◆ $K \rightarrow \pi\pi'\cancel{E}$

$$\text{Measurements: } \mathcal{B}(K^+ \rightarrow \pi^+\pi^0\nu\bar{\nu}) < 4.3 \times 10^{-5} \quad \text{at 90\% CL}$$

$$\mathcal{B}(K_L \rightarrow \pi^0\pi^0\nu\bar{\nu}) < 8.1 \times 10^{-7} \quad \text{at 90\% CL}$$

PDG 2019

$$\text{SM predictions: } \mathcal{B}(K^+ \rightarrow \pi^+\pi^0\nu\bar{\nu}) \sim 10^{-14}$$

$$\mathcal{B}(K_L \rightarrow \pi^0\pi^0\nu\bar{\nu}) \sim 10^{-13}$$

Littenberg & Valencia, 1996

Chiang & Gilman, 2000

Kamenik & Smith, 2012

- ◆ Implication: NP effects on $K \rightarrow \cancel{E}$ and $K \rightarrow \pi\pi'\cancel{E}$ can still be large.
NP that contributes via operators having mainly/only parity-odd quark parts (and coupling constants $\tilde{\mathbf{c}}_f^{V,A,S,P}$) is not yet stringently constrained.

Decay mode	$K \rightarrow \pi f \bar{f}$	$K \rightarrow f \bar{f}$	$K \rightarrow \pi\pi' f \bar{f}$
Couplings	$\mathbf{C}_f^V, \mathbf{C}_f^A, \mathbf{C}_f^S, \mathbf{C}_f^P$	$\tilde{\mathbf{c}}_f^A, \tilde{\mathbf{c}}_f^S, \tilde{\mathbf{c}}_f^P$	$\tilde{\mathbf{c}}_f^V, \tilde{\mathbf{c}}_f^A, \tilde{\mathbf{c}}_f^S, \tilde{\mathbf{c}}_f^P$

$$m_f > 0$$

- NP contributing only via operators with axial-vector ds part
 - with the couplings assumed to be real.

$$\mathcal{L}_f \supset -\bar{d}\gamma^\eta\gamma_5 s \bar{f}\gamma_\eta(\tilde{\mathbf{c}}_f^V + \gamma_5\tilde{\mathbf{c}}_f^A)f + \text{H.c.}$$

- The constraints come mainly from $K_L \rightarrow \pi^0\pi^0 \cancel{E}$ and lead to

$$\left(\text{Re } \tilde{\mathbf{c}}_f^V\right)^2 + \left(\text{Re } \tilde{\mathbf{c}}_f^A\right)^2 < 9.4 \times 10^{-14} \text{ GeV}^{-4}$$

This translates into

$$\mathcal{B}(\Lambda \rightarrow n f \bar{f}) < 6.6 \times 10^{-6},$$

$$\mathcal{B}(\Sigma^+ \rightarrow p f \bar{f}) < 1.7 \times 10^{-6}$$

$$\mathcal{B}(\Xi^0 \rightarrow \Lambda f \bar{f}) < 9.4 \times 10^{-7},$$

$$\mathcal{B}(\Xi^0 \rightarrow \Sigma^0 f \bar{f}) < 1.3 \times 10^{-6}$$

$$\mathcal{B}(\Omega^- \rightarrow \Xi^- f \bar{f}) < 7.5 \times 10^{-5}$$

JT, 1901.10447

- The upper values of these limits exceed the BESIII sensitivity levels.

Estimated BESIII sensitivity for branching fractions

Li, 2017

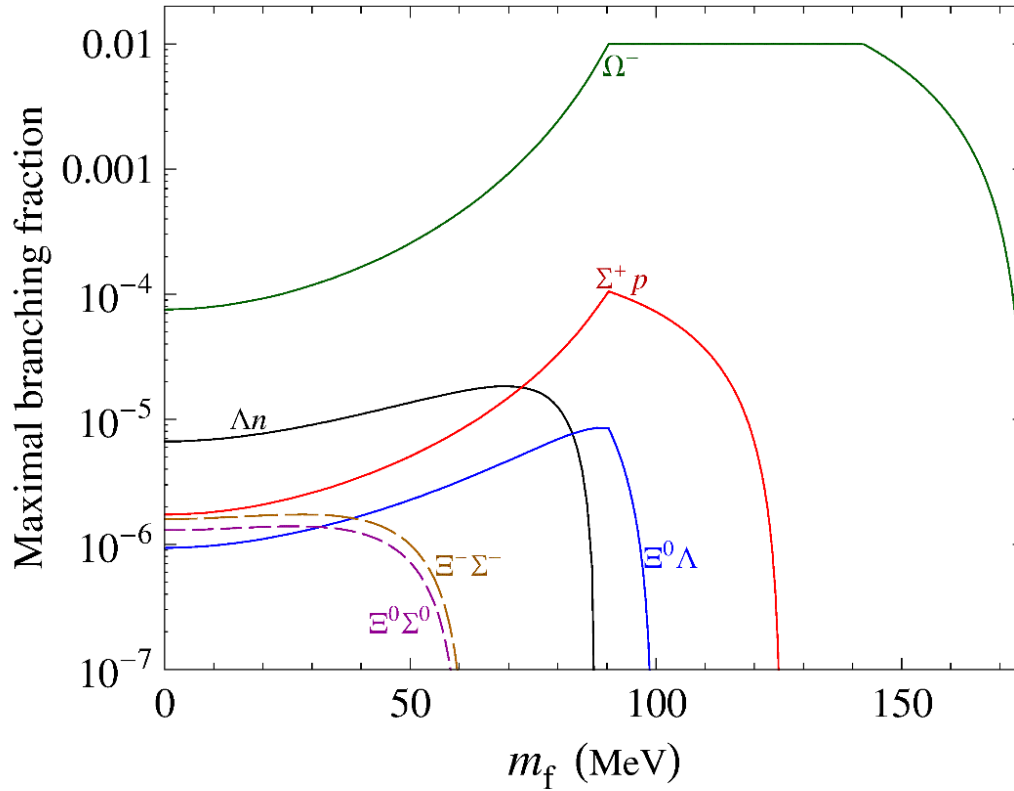
$\Lambda \rightarrow n \nu \bar{\nu}$	$\Sigma^+ \rightarrow p \nu \bar{\nu}$	$\Xi^0 \rightarrow \Lambda \nu \bar{\nu}$	$\Xi^0 \rightarrow \Sigma^0 \nu \bar{\nu}$	$\Omega^- \rightarrow \Xi^- \nu \bar{\nu}$
3×10^{-7}	4×10^{-7}	8×10^{-7}	9×10^{-7}	2.6×10^{-5}

- With $m_f > 0$, maximal branching fractions of hyperon modes can be higher.

$$\mathcal{L}_f \supset -\bar{d}\gamma_5 s \bar{f}(\tilde{\mathbf{c}}_f^S + \gamma_5 \tilde{\mathbf{c}}_f^P)f - \bar{d}\gamma^\eta \gamma_5 s \bar{f}\gamma_\eta(\tilde{\mathbf{c}}_f^V + \gamma_5 \tilde{\mathbf{c}}_f^A)f + \text{H.c.}$$

Decay mode	$K \rightarrow f\bar{f}$	$K \rightarrow \pi\pi'f\bar{f}$	$\mathfrak{B} \rightarrow \mathfrak{B}'f\bar{f}$	$\Omega^- \rightarrow \Xi^-f\bar{f}$
Couplings	$\tilde{\mathbf{c}}_f^A, \tilde{\mathbf{c}}_f^S, \tilde{\mathbf{c}}_f^P$	$\tilde{\mathbf{c}}_f^V, \tilde{\mathbf{c}}_f^A, \tilde{\mathbf{c}}_f^S, \tilde{\mathbf{c}}_f^P$	$\tilde{\mathbf{c}}_f^V, \tilde{\mathbf{c}}_f^A, \tilde{\mathbf{c}}_f^S, \tilde{\mathbf{c}}_f^P$	$\tilde{\mathbf{c}}_f^V, \tilde{\mathbf{c}}_f^A, \tilde{\mathbf{c}}_f^S, \tilde{\mathbf{c}}_f^P$

 $m_f > 0$

 Ignoring $\mathbf{c}_f^{V,A,S,P}$


Li, Su, JT, 1905.08759

FIG. 3: The maximal branching fractions of $\mathfrak{B} \rightarrow \mathfrak{B}'f\bar{f}$ with $\mathfrak{B}\mathfrak{B}' = \Lambda n, \Sigma^+ p, \Xi^0 \Lambda, \Xi^0 \Sigma^0, \Xi^- \Sigma^-$ and of $\Omega^- \rightarrow \Xi^- f\bar{f}$ versus m_f , induced by the contribution of $\text{Re}\tilde{\mathbf{c}}_f^V$ alone, subject to the $K_L \rightarrow \pi^0 \pi^0 \cancel{f}$ constraint and the perturbativity and Ω^- data requirements for $m_f > 90$ MeV.

Scalar leptoquark contributions

$$\square \quad \tilde{S}_1\left(\bar{\mathbf{3}}, 1, \frac{1}{3}\right) = \tilde{S}_1^{1/3}, \quad \tilde{S}_2\left(\mathbf{3}, 2, \frac{1}{6}\right) = \begin{pmatrix} \tilde{S}_2^{2/3} \\ \tilde{S}_2^{-1/3} \end{pmatrix}, \quad S_3\left(\bar{\mathbf{3}}, \mathbf{3}, \frac{1}{3}\right) = \begin{pmatrix} S_3^{1/3} & \sqrt{2} S_3^{4/3} \\ \sqrt{2} S_3^{-2/3} & -S_3^{1/3} \end{pmatrix}$$

$$\square \quad \tilde{S}_1\left(\bar{3}, 1, \frac{1}{3}\right) = \tilde{S}_1^{1/3}, \quad \tilde{S}_2\left(3, 2, \frac{1}{6}\right) = \begin{pmatrix} \tilde{S}_2^{2/3} \\ \tilde{S}_2^{-1/3} \end{pmatrix}, \quad S_3\left(\bar{3}, 3, \frac{1}{3}\right) = \begin{pmatrix} S_3^{1/3} & \sqrt{2} S_3^{4/3} \\ \sqrt{2} S_3^{-2/3} & -S_3^{1/3} \end{pmatrix}$$

□ Yukawa Lagrangian

$$\mathcal{L}_{\text{LQ}} = \left(Y_{1,jy}^{\text{LL}} \bar{q}_j^c \epsilon l_y + \tilde{Y}_{1,jy}^{\text{RR}} \bar{d}_j^c N_y \right) \tilde{S}_1 + Y_{2,jy}^{\text{RL}} \bar{d}_j \tilde{S}_2^T \epsilon l_y + \tilde{Y}_{2,jy}^{\text{LR}} \bar{q}_j \tilde{S}_2 N_y + Y_{3,jy}^{\text{LL}} \bar{q}_j^c \epsilon S_3 l_y + \text{H.c.}$$

family indices $j, y = 1, 2, 3$ are summed over, q_j (l_y) and d_j denote LH quark (lepton) doublet and RH down-type quark singlet, respectively, and $\epsilon = i\tau_2$

$$\tilde{S}_1\left(\bar{3}, 1, \frac{1}{3}\right) = \tilde{S}_1^{1/3}, \quad \tilde{S}_2\left(3, 2, \frac{1}{6}\right) = \begin{pmatrix} \tilde{S}_2^{2/3} \\ \tilde{S}_2^{-1/3} \end{pmatrix}, \quad S_3\left(\bar{3}, 3, \frac{1}{3}\right) = \begin{pmatrix} S_3^{1/3} & \sqrt{2} S_3^{4/3} \\ \sqrt{2} S_3^{-2/3} & -S_3^{1/3} \end{pmatrix}$$

Yukawa Lagrangian

$$\mathcal{L}_{\text{LQ}} = \left(Y_{1,jy}^{\text{LL}} \bar{q}_j^c \epsilon l_y + \tilde{Y}_{1,jy}^{\text{RR}} \bar{d}_j^c N_y \right) \tilde{S}_1 + Y_{2,jy}^{\text{RL}} \bar{d}_j \tilde{S}_2^T \epsilon l_y + \tilde{Y}_{2,jy}^{\text{LR}} \bar{q}_j \tilde{S}_2 N_y + Y_{3,jy}^{\text{LL}} \bar{q}_j^c \epsilon S_3 l_y + \text{H.c.}$$

family indices $j, y = 1, 2, 3$ are summed over, q_j (l_y) and d_j denote LH quark (lepton) doublet and RH down-type quark singlet, respectively, and $\epsilon = i\tau_2$

At tree level the LQs can mediate $sdff'$ interactions, $f = \nu$ or N

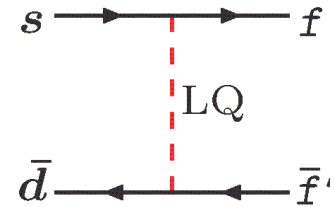
$$\mathcal{L}_{ff'} = -\left[\bar{d} \gamma^\eta s \bar{f} \gamma_\eta (C_{ff'}^V + \gamma_5 C_{ff'}^A) f' + \bar{d} \gamma^\eta \gamma_5 s \bar{f} \gamma_\eta (\tilde{C}_{ff'}^V + \gamma_5 \tilde{C}_{ff'}^A) f' \right] + \text{H.c.}$$

$$C_{\nu\nu'}^V = -C_{\nu\nu'}^A = \frac{-Y_{1,1x}^{\text{LL}*} Y_{1,2y}^{\text{LL}}}{8m_{\tilde{S}_1}^2} + \frac{Y_{2,2x}^{\text{RL}*} Y_{2,1y}^{\text{RL}}}{8m_{\tilde{S}_2}^2} - \frac{Y_{3,1x}^{\text{LL}*} Y_{3,2y}^{\text{LL}}}{8m_{S_3}^2}$$

$$\tilde{C}_{\nu\nu'}^V = -\tilde{C}_{\nu\nu'}^A = \frac{Y_{1,1x}^{\text{LL}*} Y_{1,2y}^{\text{LL}}}{8m_{\tilde{S}_1}^2} + \frac{Y_{2,2x}^{\text{RL}*} Y_{2,1y}^{\text{RL}}}{8m_{\tilde{S}_2}^2} + \frac{Y_{3,1x}^{\text{LL}*} Y_{3,2y}^{\text{LL}}}{8m_{S_3}^2}$$

$$C_{NN'}^V = C_{NN'}^A = \frac{-\tilde{Y}_{1,1x}^{\text{RR}*} \tilde{Y}_{1,2y}^{\text{RR}}}{8m_{\tilde{S}_1}^2} + \frac{\tilde{Y}_{2,2x}^{\text{LR}*} \tilde{Y}_{2,1y}^{\text{LR}}}{8m_{\tilde{S}_2}^2}$$

$$\tilde{C}_{NN'}^V = \tilde{C}_{NN'}^A = \frac{-\tilde{Y}_{1,1x}^{\text{RR}*} \tilde{Y}_{1,2y}^{\text{RR}}}{8m_{\tilde{S}_1}^2} - \frac{\tilde{Y}_{2,2x}^{\text{LR}*} \tilde{Y}_{2,1y}^{\text{LR}}}{8m_{\tilde{S}_2}^2}$$



$$\mathcal{L}_{ff'} = - \left[\bar{d} \gamma^\eta s \bar{f} \gamma_\eta (C_{ff'}^V + \gamma_5 C_{ff'}^A) f' + \bar{d} \gamma^\eta \gamma_5 s \bar{f} \gamma_\eta (\tilde{C}_{ff'}^V + \gamma_5 \tilde{C}_{ff'}^A) f' \right] + \text{H.c.}$$

$$C_{\nu\nu'}^V = -C_{\nu\nu'}^A = \frac{-Y_{1,1x}^{\text{LL}*} Y_{1,2y}^{\text{LL}}}{8m_{\tilde{S}_1}^2} + \frac{Y_{2,2x}^{\text{RL}*} Y_{2,1y}^{\text{RL}}}{8m_{\tilde{S}_2}^2} - \frac{Y_{3,1x}^{\text{LL}*} Y_{3,2y}^{\text{LL}}}{8m_{\tilde{S}_3}^2}$$

$$\tilde{C}_{\nu\nu'}^V = -\tilde{C}_{\nu\nu'}^A = \frac{Y_{1,1x}^{\text{LL}*} Y_{1,2y}^{\text{LL}}}{8m_{\tilde{S}_1}^2} + \frac{Y_{2,2x}^{\text{RL}*} Y_{2,1y}^{\text{RL}}}{8m_{\tilde{S}_2}^2} + \frac{Y_{3,1x}^{\text{LL}*} Y_{3,2y}^{\text{LL}}}{8m_{\tilde{S}_3}^2}$$

$$C_{NN'}^V = C_{NN'}^A = \frac{-\tilde{Y}_{1,1x}^{\text{RR}*} \tilde{Y}_{1,2y}^{\text{RR}}}{8m_{\tilde{S}_1}^2} + \frac{\tilde{Y}_{2,2x}^{\text{LR}*} \tilde{Y}_{2,1y}^{\text{LR}}}{8m_{\tilde{S}_2}^2}$$

$$\tilde{C}_{NN'}^V = \tilde{C}_{NN'}^A = \frac{-\tilde{Y}_{1,1x}^{\text{RR}*} \tilde{Y}_{1,2y}^{\text{RR}}}{8m_{\tilde{S}_1}^2} - \frac{\tilde{Y}_{2,2x}^{\text{LR}*} \tilde{Y}_{2,1y}^{\text{LR}}}{8m_{\tilde{S}_2}^2}$$

Decay mode	$K \rightarrow \pi f \bar{f}$	$K \rightarrow f \bar{f}$	$K \rightarrow \pi \pi' f \bar{f}$	$\mathcal{B} \rightarrow \mathcal{B}' f \bar{f}$	$\Omega^- \rightarrow \Xi^- f \bar{f}$
Couplings	$\mathbf{C}_f^{\text{V,A,S,P}}$	$\tilde{\mathbf{C}}_f^{\text{A,S,P}}$	$\tilde{\mathbf{C}}_f^{\text{V,A,S,P}}$	$\mathbf{C}_f^{\text{V,A,S,P}}, \tilde{\mathbf{C}}_f^{\text{V,A,S,P}}$	$\tilde{\mathbf{C}}_f^{\text{V,A,S,P}}$

Scalar leptoquark contributions

$$\mathcal{L}_{ff'} = - \left[\bar{d} \gamma^\eta s \bar{f} \gamma_\eta (C_{ff'}^V + \gamma_5 C_{ff'}^A) f' + \bar{d} \gamma^\eta \gamma_5 s \bar{f} \gamma_\eta (\tilde{C}_{ff'}^V + \gamma_5 \tilde{C}_{ff'}^A) f' \right] + \text{H.c.}$$

$$C_{\nu\nu'}^V = -C_{\nu\nu'}^A = \frac{-Y_{1,1x}^{LL*} Y_{1,2y}^{LL}}{8m_{\tilde{S}_1}^2} + \frac{Y_{2,2x}^{RL*} Y_{2,1y}^{RL}}{8m_{\tilde{S}_2}^2} - \frac{Y_{3,1x}^{LL*} Y_{3,2y}^{LL}}{8m_{\tilde{S}_3}^2} \approx 0$$

$$\tilde{C}_{\nu\nu'}^V = -\tilde{C}_{\nu\nu'}^A = \frac{Y_{1,1x}^{LL*} Y_{1,2y}^{LL}}{8m_{\tilde{S}_1}^2} + \frac{Y_{2,2x}^{RL*} Y_{2,1y}^{RL}}{8m_{\tilde{S}_2}^2} + \frac{Y_{3,1x}^{LL*} Y_{3,2y}^{LL}}{8m_{\tilde{S}_3}^2}$$

$$C_{NN'}^V = C_{NN'}^A = \frac{-\tilde{Y}_{1,1x}^{RR*} \tilde{Y}_{1,2y}^{RR}}{8m_{\tilde{S}_1}^2} + \frac{\tilde{Y}_{2,2x}^{LR*} \tilde{Y}_{2,1y}^{LR}}{8m_{\tilde{S}_2}^2} \approx 0$$

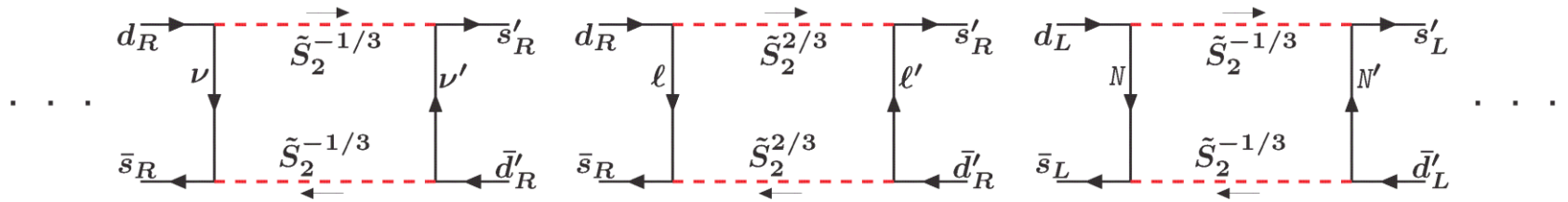
$$\tilde{C}_{NN'}^V = \tilde{C}_{NN'}^A = \frac{-\tilde{Y}_{1,1x}^{RR*} \tilde{Y}_{1,2y}^{RR}}{8m_{\tilde{S}_1}^2} - \frac{\tilde{Y}_{2,2x}^{LR*} \tilde{Y}_{2,1y}^{LR}}{8m_{\tilde{S}_2}^2}$$

Decay mode	$K \rightarrow \pi f \bar{f}$	$K \rightarrow f \bar{f}$	$K \rightarrow \pi \pi' f \bar{f}$	$\mathcal{B} \rightarrow \mathcal{B}' f \bar{f}$	$\Omega^- \rightarrow \Xi^- f \bar{f}$
Couplings	$\mathbf{C}_f^{V,A,S,P}$	$\tilde{\mathbf{C}}_f^{A,S,P}$	$\tilde{\mathbf{C}}_f^{V,A,S,P}$	$\mathbf{C}_f^{V,A,S,P}, \tilde{\mathbf{C}}_f^{V,A,S,P}$	$\tilde{\mathbf{C}}_f^{V,A,S,P}$

- At least two different LQs are needed.

Constraints from kaon mixing

□



$$\mathcal{H}_{|\Delta S|=2}^{\text{LQ}} = \left[\frac{(\sum_x Y_{1,1x}^{\text{LL}} Y_{1,2x}^{\text{LL}*})^2}{128\pi^2 m_{\tilde{S}_1}^2} + \frac{(\sum_n \tilde{Y}_{2,2n}^{\text{LR}} \tilde{Y}_{2,1n}^{\text{LR}*})^2}{128\pi^2 m_{\tilde{S}_2}^2} + \frac{5(\sum_x Y_{3,1x}^{\text{LL}} Y_{3,2x}^{\text{LL}*})^2}{128\pi^2 m_{\tilde{S}_3}^2} \right] \bar{s}_L \gamma^\eta d_L \bar{s}_L \gamma_\eta d_L$$

$$+ \left[\frac{(\sum_n \tilde{Y}_{1,1n}^{\text{RR}} \tilde{Y}_{1,2n}^{\text{RR}*})^2}{128\pi^2 m_{\tilde{S}_1}^2} + \frac{(\sum_x Y_{2,2x}^{\text{RL}} Y_{2,1x}^{\text{RL}*})^2}{64\pi^2 m_{\tilde{S}_2}^2} \right] \bar{s}_R \gamma^\eta d_R \bar{s}_R \gamma_\eta d_R$$

Kaon mixing constraints can be avoided by assigning the nonzero elements of the 1st and 2nd rows of each contributing Yukawa matrix to different columns.

- At tree level the LQs can mediate lepton-flavor-violating $sd\ell\ell'$ interactions

$$\mathcal{L}_{\ell\ell'} = -\left[\bar{d}\gamma^\eta s \bar{\ell}\gamma_\eta(V_{\ell\ell'} + \gamma_5 A_{\ell\ell'})\ell' + \bar{d}\gamma^\eta\gamma_5 s \bar{\ell}\gamma_\eta(\tilde{V}_{\ell\ell'} + \gamma_5\tilde{A}_{\ell\ell'})\ell'\right] + \text{H.c.}$$

$$V_{\ell\ell'} = -A_{\ell\ell'} = \frac{Y_{2,2x}^{\text{RL}*} Y_{2,1y}^{\text{RL}}}{8m_{\tilde{S}_2}^2} - \frac{Y_{3,1x}^{\text{LL}*} Y_{3,2y}^{\text{LL}}}{4m_{S_3}^2}, \quad \tilde{V}_{\ell\ell'} = -\tilde{A}_{\ell\ell'} = \frac{Y_{2,2x}^{\text{RL}*} Y_{2,1y}^{\text{RL}}}{8m_{\tilde{S}_2}^2} + \frac{Y_{3,1x}^{\text{LL}*} Y_{3,2y}^{\text{LL}}}{4m_{S_3}^2}$$

- If $xy = 12, 21$, corresponding to $\ell\ell' = e\mu, \mu e$, the first (last) 2 terms induce $K \rightarrow \pi e\mu$ ($K_L \rightarrow e\mu$). Their bounds can be evaded with $xy \neq 12, 21$.
Likewise, constraints from $\mu \rightarrow e\gamma, 3e$ and $\mu \rightarrow e$ transitions are avoided.

- If $xy = 13, 31, 23, 32$, the tau decays $\tau \rightarrow eK^{(*)}, \mu K^{(*)}$ are induced but their bounds are not too severe.
- With only $\tilde{S}_1$ and $\tilde{S}_2$ being present and the choices

$$Y_1^{\text{LL}} = \begin{pmatrix} 0 & y_{1,12} & 0 \\ 0 & 0 & y_{1,23} \\ 0 & 0 & 0 \end{pmatrix}, \quad Y_2^{\text{RL}} = \begin{pmatrix} 0 & 0 & y_{2,13} \\ 0 & y_{2,22} & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

the $\tau \rightarrow \ell K^{(*)}$ restrictions translate into ($ff' = \nu_\mu \nu_\tau$)

$$\mathcal{B}(\Lambda \rightarrow nf\bar{f}') < 1.7 \times 10^{-7}, \quad \mathcal{B}(\Sigma^+ \rightarrow pf\bar{f}') < 4.7 \times 10^{-8}$$

$$\mathcal{B}(\Xi^0 \rightarrow \Lambda f\bar{f}') < 2.5 \times 10^{-8}, \quad \mathcal{B}(\Xi^0 \rightarrow \Sigma^0 f\bar{f}') < 3.5 \times 10^{-8}$$

$$\mathcal{B}(\Omega^- \rightarrow \Xi^- f\bar{f}') < 2.0 \times 10^{-6}$$

These are not far below the proposed BESIII sensitivity reach

Li, 2017

$\Lambda \rightarrow n\nu\bar{\nu}$	$\Sigma^+ \rightarrow p\nu\bar{\nu}$	$\Xi^0 \rightarrow \Lambda\nu\bar{\nu}$	$\Xi^0 \rightarrow \Sigma^0\nu\bar{\nu}$	$\Omega^- \rightarrow \Xi^-\nu\bar{\nu}$
3×10^{-7}	4×10^{-7}	8×10^{-7}	9×10^{-7}	2.6×10^{-5}

- The kaon mixing restrictions can be evaded as before.
- The constraints come mainly from $K_L \rightarrow \pi^0 \pi^0 \cancel{E}$ and lead to

$$(\text{Re } \tilde{\mathbf{c}}_{NN'}^V)^2 + (\text{Re } \tilde{\mathbf{c}}_{NN'}^A)^2 < 9.4 \times 10^{-14} \text{ GeV}^{-4}$$

This translates into

$$\mathcal{B}(\Lambda \rightarrow n N \bar{N}') < 6.6 \times 10^{-6}, \quad \mathcal{B}(\Sigma^+ \rightarrow p N \bar{N}') < 1.7 \times 10^{-6}$$

$$\mathcal{B}(\Xi^0 \rightarrow \Lambda N \bar{N}') < 9.4 \times 10^{-7}, \quad \mathcal{B}(\Xi^0 \rightarrow \Sigma^0 N \bar{N}') < 1.3 \times 10^{-6}$$

$$\mathcal{B}(\Omega^- \rightarrow \Xi^- N \bar{N}') < 7.5 \times 10^{-5}$$

JT, 1901.10447

- Their upper values exceed the proposed BESIII sensitivity reach.

Li, 2017

$\Lambda \rightarrow n \nu \bar{\nu}$	$\Sigma^+ \rightarrow p \nu \bar{\nu}$	$\Xi^0 \rightarrow \Lambda \nu \bar{\nu}$	$\Xi^0 \rightarrow \Sigma^0 \nu \bar{\nu}$	$\Omega^- \rightarrow \Xi^- \nu \bar{\nu}$
3×10^{-7}	4×10^{-7}	8×10^{-7}	9×10^{-7}	2.6×10^{-5}

- ❑ FCNC hyperon & kaon decays with missing energy are potentially **sensitive** to physics beyond the SM, but they do not probe the same set of the underlying **NP** operators.
- ❑ Ongoing & future experiments on the **hyperon ones** can provide **useful information** on possible **NP** effects which is **complementary** to that from the kaon sector.
- ❑ The forthcoming measurements by **BESIII**, and future ones at **super charm-tau factories**, on the **hyperon modes** can help test different **NP** scenarios.