



A Variant Two-Higgs Doublet Model with A New Abelian Gauge Symmetry

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12/13/2019 @ NCTS Annual Theory Meeting 2019

CRC, Cheng-Wei Chiang, Kuo-Yen Lin, PLB795 (2019), 22



Outline

Motivation

muon $g-2$ & dark matter

Benchmark Model

4th generation lepton, singlet scalar and U(1) extension

Constraints

charged lepton decays, Z-boson flavor-changing decay

Dark Matter Phenomenology

relic density, elastic scattering w/ nucleon

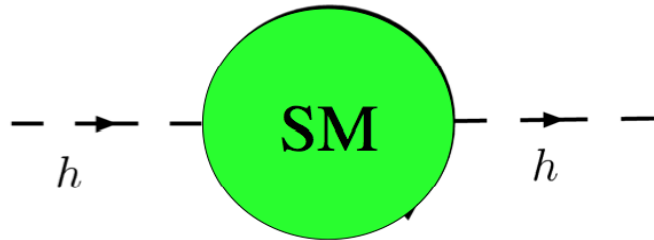
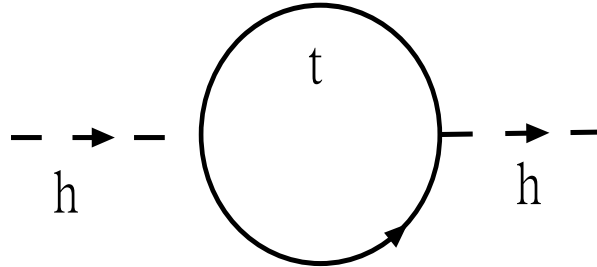
Summary



BSM?

Naturalness "Problem"

$$m_h^2 = m_{h0}^2 + \delta m_h^2$$



Λ^2 terms are canceled !!

BSM $\rightarrow$ new particles

ATLAS Exotics Searches* - 95% CL Upper Exclusion Limits

Status: July 2018

ATLAS Preliminary

$$\int \mathcal{L} dt = (3.2 - 79.8) \text{ fb}^{-1}$$

$$\sqrt{s} = 8, 13 \text{ TeV}$$

	Model	ℓ, γ	Jets [†]	$E_{\text{T}}^{\text{miss}}$	$\int \mathcal{L} dt [\text{fb}^{-1}]$	Limit	Reference
Extra dimensions	ADD $G_{KK} + g/q$	$0\ e, \mu$	$1-4\ j$	Yes	36.1	M_D 7.7 TeV	$n = 2$ 1711.03301
	ADD non-resonant $\gamma\gamma$	$2\ \gamma$	—	—	36.7	M_S 8.6 TeV	$n = 3$ HLZ NLO 1707.04147
	ADD QBH	—	$2\ j$	—	37.0	M_{th} 8.9 TeV	$n = 6$ 1703.09127
	ADD BH high Σp_T	$\geq 1\ e, \mu$	$\geq 2\ j$	—	3.2	M_{th} 8.2 TeV	$n = 6, M_D = 3\ \text{TeV, rot BH}$ 1606.02265
	ADD BH multijet	—	$\geq 3\ j$	—	3.6	M_{th} 9.55 TeV	$n = 6, M_D = 3\ \text{TeV, rot BH}$ 1512.02586
	RS1 $G_{KK} \rightarrow \gamma\gamma$	$2\ \gamma$	—	—	36.7	G_{KK} mass 4.1 TeV	$k/\overline{M}_{Pl} = 0.1$ 1707.04147
	Bulk RS $G_{KK} \rightarrow WW/ZZ$	multi-channel	—	—	36.1	G_{KK} mass 2.3 TeV	$k/\overline{M}_{Pl} = 1.0$ CERN-EP-2018-179
	Bulk RS $g_{KK} \rightarrow tt$	$1\ e, \mu$	$\geq 1\ b, \geq 1J/2j$	Yes	36.1	g_{KK} mass 3.8 TeV	$\Gamma/m = 15\%$ 1804.10823
	2UED / RPP	$1\ e, \mu$	$\geq 2\ b, \geq 3\ j$	Yes	36.1	KK mass 1.8 TeV	Tier (1,1), $\mathcal{B}(A^{(1,1)} \rightarrow tt) = 1$ 1803.09678
Gauge bosons	SSM $Z' \rightarrow \ell\ell$	$2\ e, \mu$	—	—	36.1	Z' mass 4.5 TeV	$\Gamma/m = 1\%$ 1707.02424
	SSM $Z' \rightarrow \tau\tau$	$2\ \tau$	—	—	36.1	Z' mass 2.42 TeV	1709.07242
	Leptophobic $Z' \rightarrow bb$	—	$2\ b$	—	36.1	Z' mass 2.1 TeV	1805.09299
	Leptophobic $Z' \rightarrow tt$	$1\ e, \mu$	$\geq 1\ b, \geq 1J/2j$	Yes	36.1	Z' mass 3.0 TeV	1804.10823
	SSM $W' \rightarrow \ell\nu$	$1\ e, \mu$	—	Yes	79.8	W' mass 5.6 TeV	ATLAS-CONF-2018-017
	SSM $W' \rightarrow \tau\nu$	$1\ \tau$	—	Yes	36.1	W' mass 3.7 TeV	1801.06992
	HVT $V' \rightarrow WV \rightarrow qq\bar{q}\bar{q}$ model B	$0\ e, \mu$	$2\ J$	—	79.8	V' mass 4.15 TeV	$g_V = 3$ ATLAS-CONF-2018-016
	HVT $V' \rightarrow WH/ZH$ model B	multi-channel	—	—	36.1	V' mass 2.93 TeV	$g_V = 3$ 1712.06518
	LRS $W'_R \rightarrow tb$	multi-channel	—	—	36.1	W'_R mass 3.25 TeV	CERN-EP-2018-142
CI	CI $qq\bar{q}\bar{q}$	—	$2\ j$	—	20.0	Λ 21.8 TeV	η_{LL}^- 1703.09127
	CI $\ell\ell\bar{q}\bar{q}$	$2\ e, \mu$	—	—	36.1	Λ 40.0 TeV	η_{LL}^- 1707.02424
	CI $tt\bar{t}\bar{t}$	$\geq 1\ e, \mu$	$\geq 1\ b, \geq 1\ j$	Yes	36.1	Λ 2.57 TeV	$ C_4 = 4\pi$ CERN-EP-2018-174
DM	Axial-vector mediator (Dirac DM)	$0\ e, \mu$	$1-4\ j$	Yes	36.1	m_{med} 1.55 TeV	$g_q = 0.25, g_b = 1.0, m(\chi) = 1\ \text{GeV}$ 1711.03301
	Colored scalar mediator (Dirac DM)	$0\ e, \mu$	$1-4\ j$	Yes	36.1	m_{med} 1.67 TeV	$g = 1.0, m(\chi) = 1\ \text{GeV}$ 1711.03301
	$VV_{\chi\chi}$ EFT (Dirac DM)	$0\ e, \mu$	$1\ J, \leq 1\ j$	Yes	3.2	M_χ 700 GeV	$m(\chi) < 150\ \text{GeV}$ 1608.02372
LQ	Scalar LQ 1 st gen	$2\ e$	$\geq 2\ j$	—	3.2	LQ mass 1.05 TeV	$\beta = 1$ 1605.06035
	Scalar LQ 2 nd gen	$2\ \mu$	$\geq 2\ j$	—	3.2	LQ mass 1.05 TeV	$\beta = 1$ 1605.06035
	Scalar LQ 3 rd gen	$1\ e, \mu$	$\geq 1\ b, \geq 3\ j$	Yes	20.3	LQ mass 640 GeV	$\beta = 0$ 1508.04735
Heavy quarks	VLQ $TT \rightarrow Ht/Zt/Wb + X$	multi-channel	—	—	36.1	T mass 1.37 TeV	SU(2) doublet ATLAS-CONF-2018-032
	VLQ $BB \rightarrow Wt/Zb + X$	multi-channel	—	—	36.1	B mass 1.34 TeV	SU(2) doublet ATLAS-CONF-2018-032
	VLQ $T_{5/3} T_{5/3} T_{5/3} \rightarrow Wt + X$	$2(SS)/\geq 3\ e, \mu$	$\geq 1\ b, \geq 1\ j$	Yes	36.1	$T_{5/3}$ mass 1.64 TeV	$\mathcal{B}(T_{5/3} \rightarrow Wt) = 1, c(T_{5/3} Wt) = 1$ CERN-EP-2018-171
	VLQ $Y \rightarrow Wb + X$	$1\ e, \mu$	$\geq 1\ b, \geq 1\ j$	Yes	3.2	Y mass 1.44 TeV	$\mathcal{B}(Y \rightarrow Wb) = 1, c(Y Wb) = 1/\sqrt{2}$ ATLAS-CONF-2016-072
	VLQ $B \rightarrow Hb + X$	$0\ e, \mu, 2\ \gamma$	$\geq 1\ b, \geq 1\ j$	Yes	79.8	B mass 1.21 TeV	$\kappa_B = 0.5$ ATLAS-CONF-2018-024
	VLQ $QQ \rightarrow WqWq$	$1\ e, \mu$	$\geq 4\ j$	Yes	20.3	Q mass 690 GeV	1509.04261
Excited fermions	Excited quark $q^* \rightarrow qg$	—	$2\ j$	—	37.0	q^* mass 6.0 TeV	only u^* and d^* , $\Lambda = m(q^*)$ 1703.09127
	Excited quark $q^* \rightarrow q\gamma$	$1\ \gamma$	$1\ j$	—	36.7	q^* mass 5.3 TeV	only u^* and d^* , $\Lambda = m(q^*)$ 1709.10440
	Excited quark $b^* \rightarrow bg$	—	$1\ b, 1\ j$	—	36.1	b^* mass 2.6 TeV	1805.09299
	Excited lepton ℓ^*	$3\ e, \mu$	—	—	20.3	ℓ^* mass 3.0 TeV	$\Lambda = 3.0\ \text{TeV}$ 1411.2921
	Excited lepton ν^*	$3\ e, \mu, \tau$	—	—	20.3	ν^* mass 1.6 TeV	$\Lambda = 1.6\ \text{TeV}$ 1411.2921
	Type III Seesaw	$1\ e, \mu$	$\geq 2\ j$	Yes	79.8	N^0 mass 560 GeV	$m(W_R) = 2.4\ \text{TeV, no mixing}$ ATLAS-CONF-2018-020
Other	LRS Majorana ν	$2\ e, \mu$	$2\ j$	—	20.3	N^0 mass 2.0 TeV	1506.06020
	Higgs triplet $H^{\pm\pm} \rightarrow \ell\ell$	$2, 3, 4\ e, \mu$ (SS)	—	—	36.1	$H^{\pm\pm}$ mass 870 GeV	DY production 1710.09748
	Higgs triplet $H^{\pm\pm} \rightarrow \ell\tau$	$3\ e, \mu, \tau$	—	—	20.3	$H^{\pm\pm}$ mass 400 GeV	DY production, $\mathcal{B}(H_L^{\pm\pm} \rightarrow \ell\tau) = 1$ 1411.2921
	Monotop (non-res prod)	$1\ e, \mu$	$1\ b$	Yes	20.3	spin-1 invisible particle mass 657 GeV	$a_{\text{non-res}} = 0.2$ 1410.5404
	Multi-charged particles	—	—	—	20.3	multi-charged particle mass 785 GeV	DY production, $ q = 5e$ 1504.04188
	Magnetic monopoles	—	—	—	7.0	monopole mass 1.34 TeV	DY production, $ g = 1g_D, \text{spin } 1/2$ 1509.08059

$\sqrt{s} = 8\ \text{TeV}$

$\sqrt{s} = 13\ \text{TeV}$

10^{-1}

1

10

Mass scale [TeV]

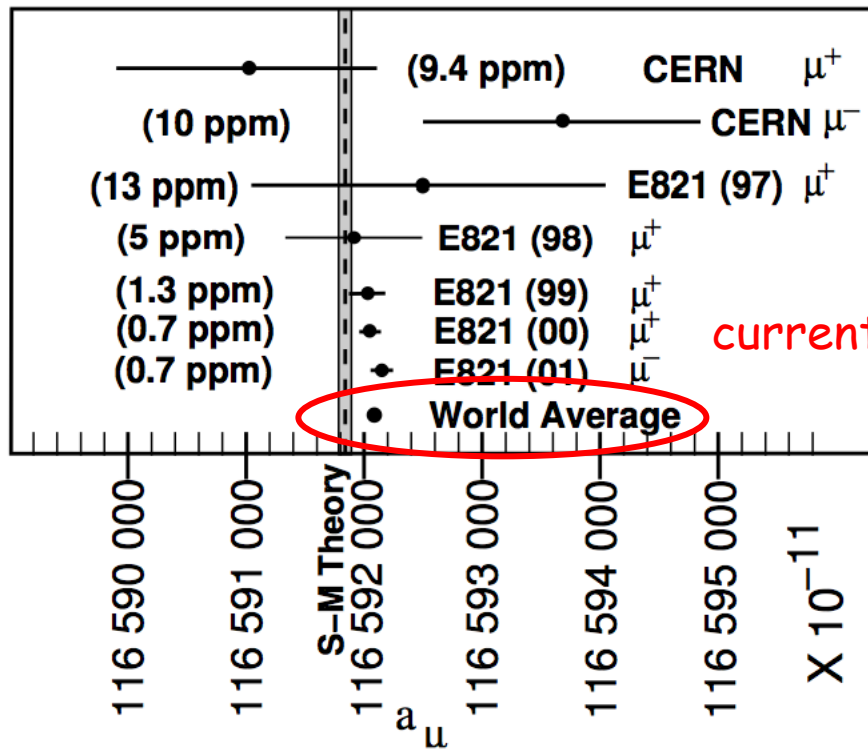
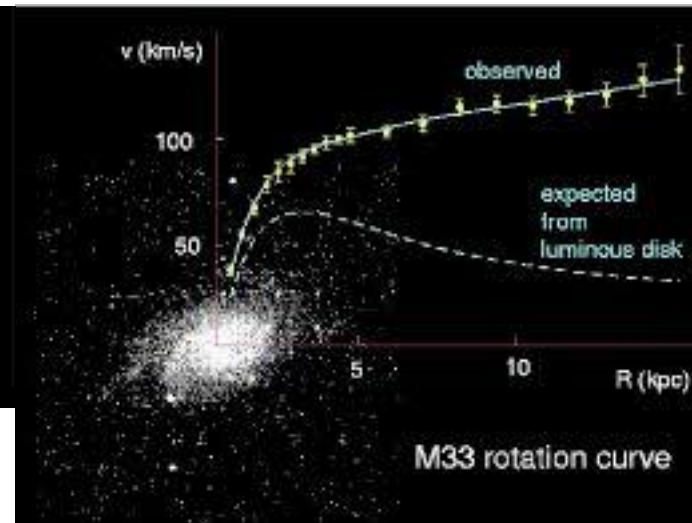
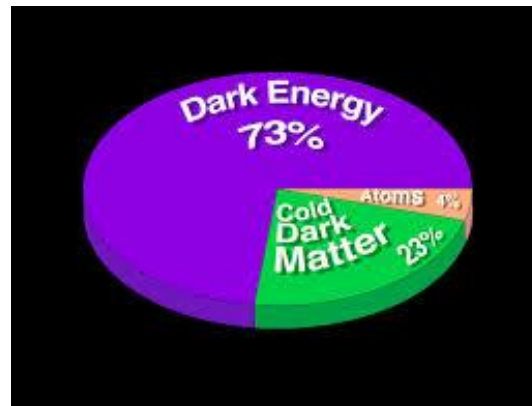
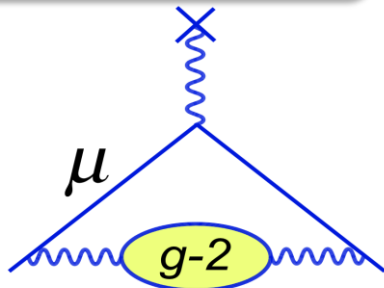
$\sqrt{s} = 8 \text{ TeV}$ $\sqrt{s} = 13 \text{ TeV}$

10⁻¹ 1 10 Mass scale [TeV]

*Only a selection of the available mass limits on new states or phenomena is shown.

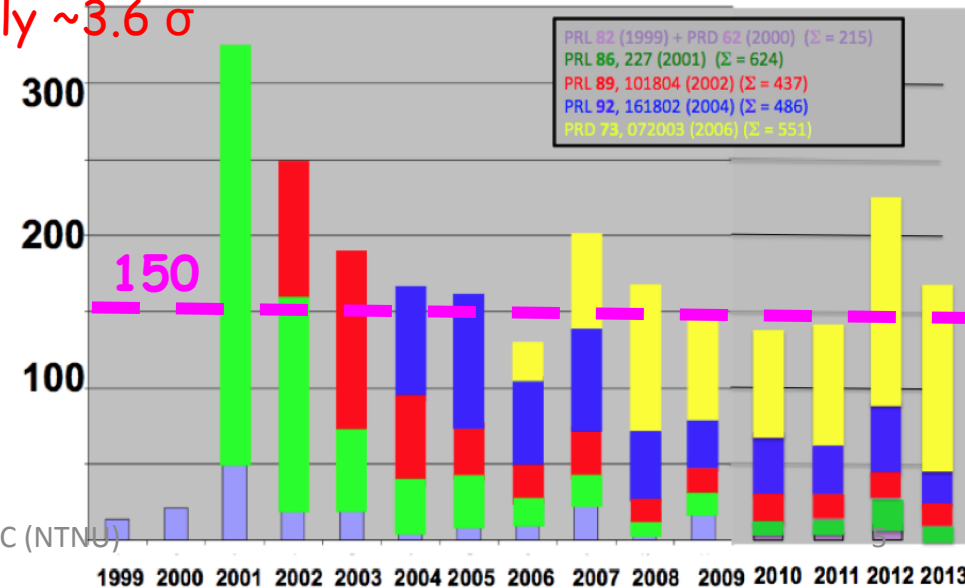
[†]Small-radius (large-radius) jets are denoted by the letter j (J).

BSM Here(?)



currently $\sim 3.6 \sigma$

BNL E821 Citations

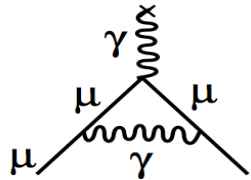


projected $> 7 \sigma$,
if central values of both TH and EXP remain

muon g-2

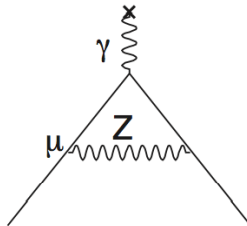
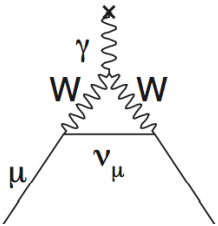
$$\vec{\mu}_\ell = g_\ell \frac{Qe}{2m_\ell} \vec{s}, \quad \underbrace{g_\ell = 2(1 + a_\ell)}_{\text{Dirac}}, \quad a_\ell = \frac{g_\ell - 2}{2}$$

$$a^{SM} = a^{QED} + a^{Had} + a^{Weak}$$



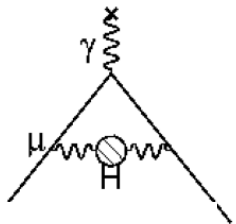
$$+ \dots a_\mu^{QED} = 116\,584\,718.951 (0.009)(0.019)(0.007)(.077) \times 10^{-11}$$

Aoyama, Hayakawa, Kinoshita and Nio, PRL109(2012),111808



$$a_\mu^{EW} = (153.6 \pm 1.0) \times 10^{-11}$$

Miller, de Rafael, Dobson, Stockinger, Ann Rev Nucl Part Sci 62 (2012) 227



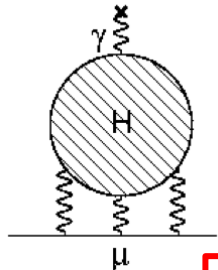
+ ...

$$a_\mu^{\text{had;LO}}$$

$$a_\mu^{\text{had;NLO}}$$

Hagiwara, Li

$$a_\mu^{\text{HLbL}} = (105 \pm 26) \times 10^{-11}$$



	VALUE ($\times 10^{-11}$) UNITS
QED	116 584 718.95 $\pm$ 0.08
HVP	6 850.6 $\pm$ 43
HLbL	105 $\pm$ 26
EW	153.6 $\pm$ 1.0
Total SM	116 591 828 $\pm$ 49

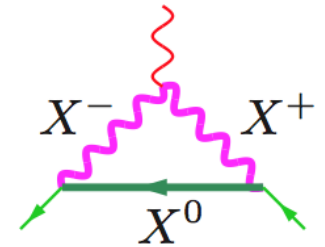
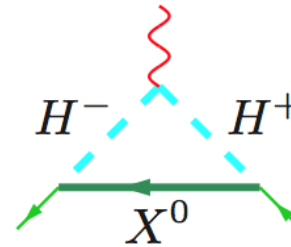
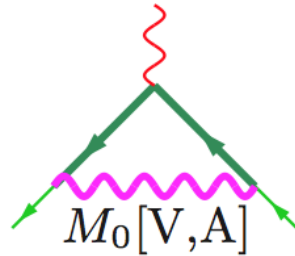
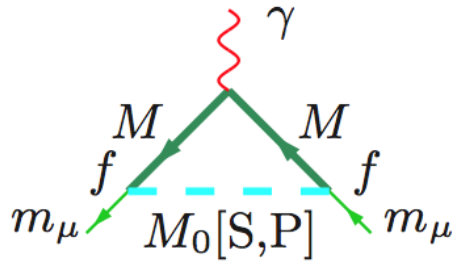
3.6 σ

$$a_\mu^{\text{E821}} = (116\,592\,089 \pm 63) \times 10^{-11}$$

$$\Delta a_\mu(\text{E821} - \text{SM}) = (287 \pm 80) \times 10^{-11}$$

NP & g_μ -2

Lautrup, Peterman, de Rafael, Phys. Reports 3C(1972), 193
Leveille, NPB137(1978), 63



$$\Delta a_\mu^{\text{NP}} = \frac{f^2}{4\pi^2} \frac{m_\mu^2}{M_0^2} L,$$

$$L = \frac{1}{2} \int_0^1 dx \frac{Q(x)}{(1-x)(1-\lambda^2 x) + (\epsilon\lambda)^2 x}, \quad \text{neutral boson}$$

$$L = \frac{1}{2} \int_0^1 dx \frac{Q(x)}{(\epsilon\lambda)^2 (1-x)(1-\epsilon^{-2} x) + x}$$

$$\epsilon = M/m_\mu$$

$$\lambda = m_\mu/M_0$$

$$Q_V = 2x(1-x)(x-2(1-\epsilon)) + \lambda^2(1-\epsilon)^2 Q_S$$

$$Q_A = 2x(1-x)(x-2(1+\epsilon)) + \lambda^2(1+\epsilon)^2 Q_P$$

$$Q_S = x^2(1+\epsilon-x)$$

$$Q_P = x^2(1-\epsilon-x)$$

charged boson

$$Q_S = -x(1-x)(x+\epsilon)$$

$$Q_P = -x(1-x)(x-\epsilon)$$

$$Q_V = 2x^2(1+x-2\epsilon) - \lambda^2(1-\epsilon)^2 Q_S$$

$$\text{CRC (NTNI)} \quad Q_A = 2x^2(1+x+2\epsilon) - \lambda^2(1+\epsilon)^2 Q_P$$



Heavy Fermions

Sequential 4th generation --- chiral fermions

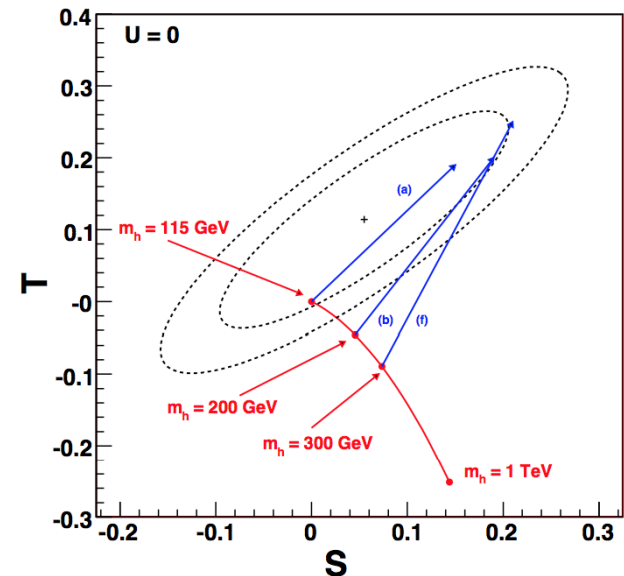
b' , t' , ℓ_4 , ν_4

✓ why not !?

✓ new CP phases $\rightarrow$ BAU(?) Hou, Chin. J. Phys 47 (2009) 134

✓ accommodate to a heavy Higgs boson He, Polonsky, Su, PRD64(2001) 053004
Kribs, Plehn, Spannowsky, Tait, PRD76(2007) 075016

◆ unitary bound: $m \lesssim 600$ GeV



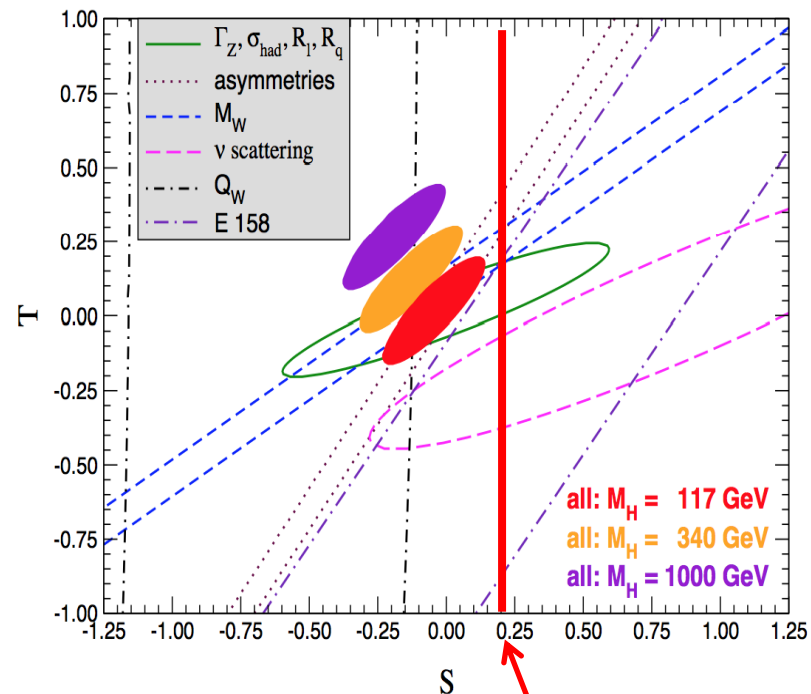
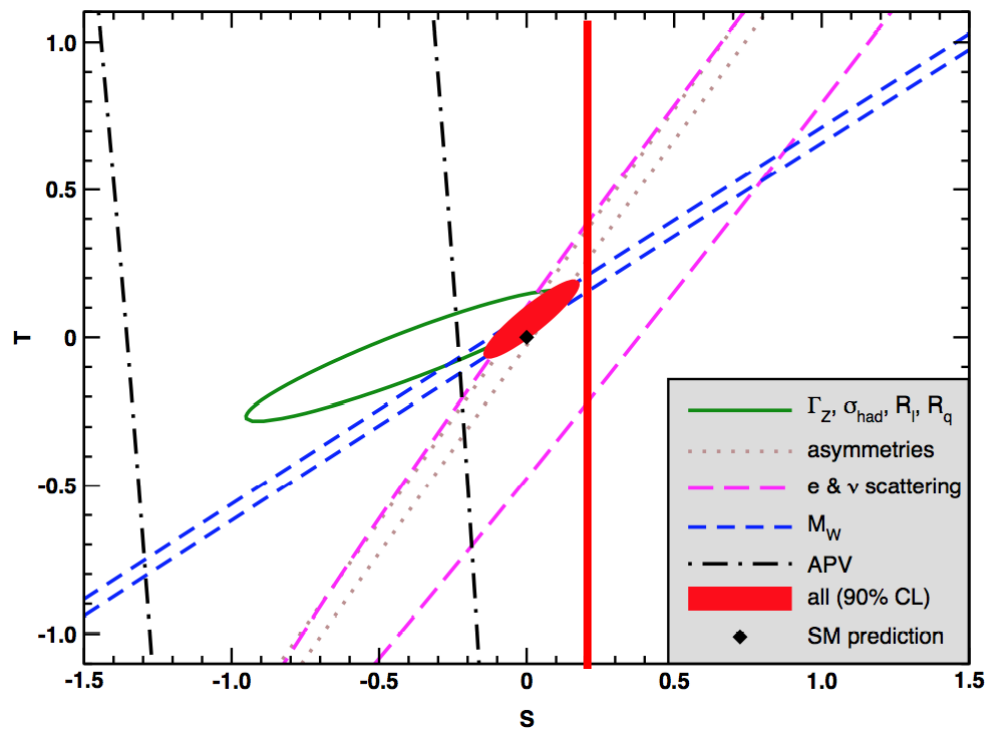
EWPO & SM4

✗ "An extra generation of ordinary fermions is excluded at the 6σ level on the basis of S parameter alone, ..."

PDG 2008

$$S = -0.04 \pm 0.09$$

$$T = 0.02 \pm 0.09$$



PDG 2018

$$S = 0.02 \pm 0.07$$

$$T = 0.06 \pm 0.06$$

$$\frac{2\pi}{3} \simeq 0.21$$

LHC search

b' (4^{th} Generation) Quark, Searches PDG 2018

$b'(-1/3)-q$ in $p\bar{p}$ and pp collisions			
VALUE (GeV)	CL%	DOCUMENT ID	TECN COMMENT
>730	95	17L	SIRUNYAN 17AU CMS

t' (4^{th} Generation) Quark, Searches for

t' (2/3)-quark/hadron mass limits in $p\bar{p}$ and pp collisions

VALUE (GeV)	CL%	DOCUMENT ID	TECN	COMMENT
>1160 (CL = 95%)	95	17L	ATLS	$B(t' \rightarrow Z t) = 1$ $t' \rightarrow Z t$
>1160	95	12BC	ATLS	$B(t' \rightarrow W q) = 1$ ($q=d,s,b$) $t' \rightarrow W q$
> 350	95	12C	ATLS	$t' \rightarrow X t$ ($m_X < 140$ GeV) $t' \rightarrow X t$
> 420	95			

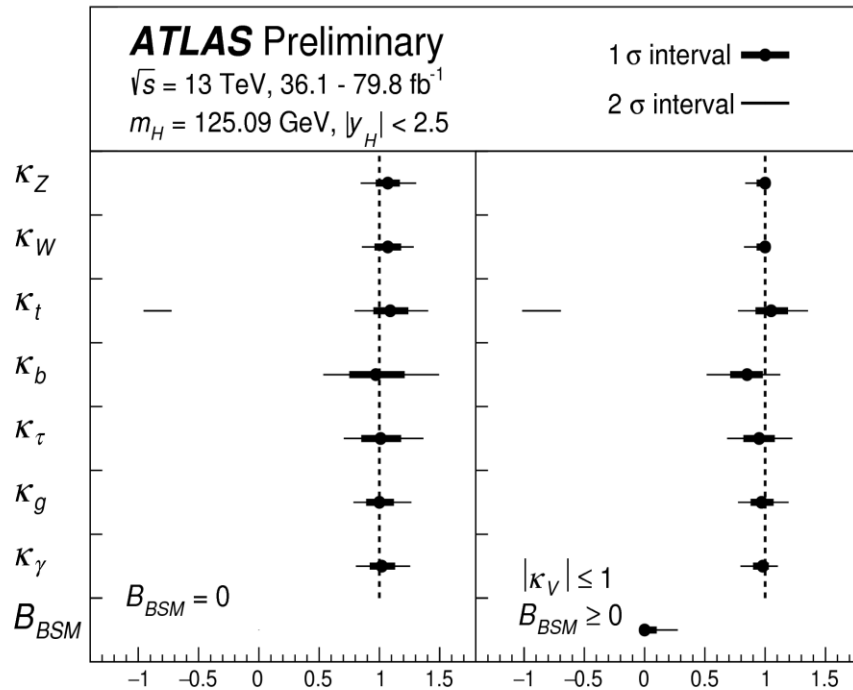
Heavy Charged Lepton Searches

Charged Heavy Lepton MASS LIMITS

Sequential Charged Heavy Lepton ($L^\pm$) MASS LIMITS

VALUE (GeV)	CL%	DOCUMENT ID	TECN	COMMENT
>100.8	95	1B	L3	Decay to νW

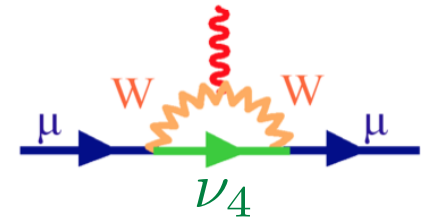
SM4 & Other Data



$$R_{gg} = \frac{\left| \kappa_t F_{1/2}(\tau_t) + \sum_{f=t',b'} \kappa_f F_{1/2}(\tau_f) \right|^2}{\left| F_{1/2}(\tau_t) \right|^2} = 9$$

$$a_\mu^{\text{SM}}(W^+W^-N) \sim 233 \times 10^{-11} |V_{N\mu}|^2 F(x), \quad x = m_N^2/M_W^2$$

$$|V_{N\mu}| > 0.7 \quad \text{excluded by } Br(\mu \rightarrow e\gamma)$$

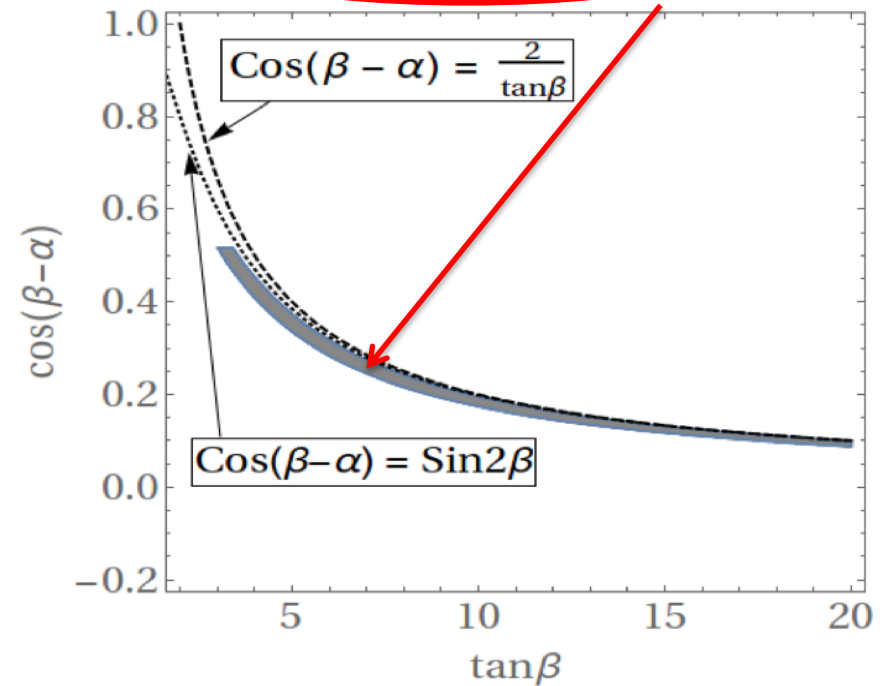
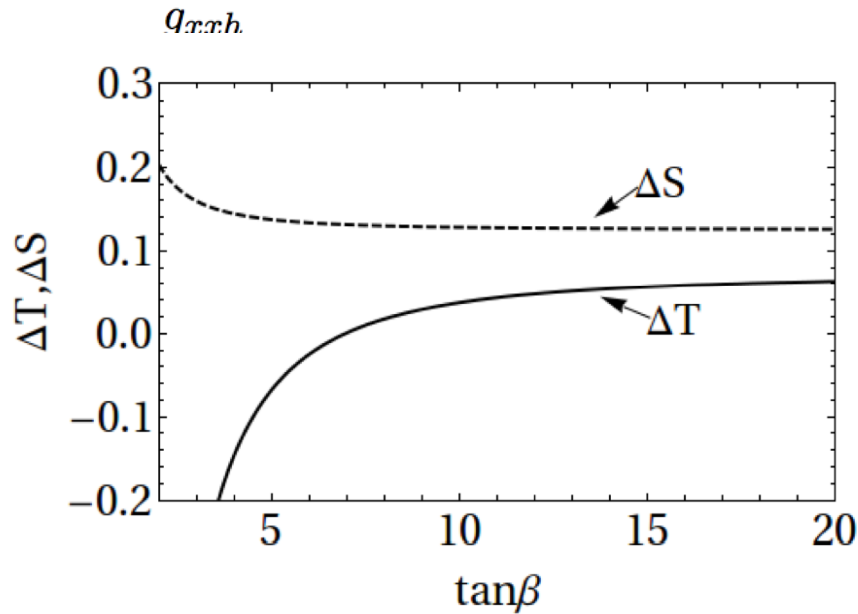


Huo, Feng, hep-ph/0301153

Hou et al., ICHEP2008 Proceedings

4th + 2HDM

Das, Kundu, Saha, 1707.03000,
Wang, Shi, Han, 1708.0681

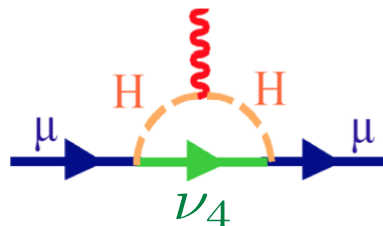


$$a_{\mu}^{2\text{HDM-II}}(H^+ H^- N) \sim -233 \times 10^{-11} |V_{N\mu}|^2 [f_{H^+}(x) + g_{H^+}(x) \cot^2 \beta + x_{\mu} q_{H^+}(x) \tan^2 \beta],$$

goes to wrong direction

Huo, Feng, hep-ph/0301153

Hou et al., ICHEP2008 Proceedings



Non-canonical 4th Generation

Langacker and London, PRD 38 (1988), 886

Sequential fermions

$$\begin{bmatrix} N \\ E^- \end{bmatrix}_L \quad E_R^-, \quad \begin{bmatrix} U \\ D \end{bmatrix}_L \quad U_R \quad D_R$$

Noncanonical $SU(2) \times U(1)$ assignments

(a) Mirror fermions

$$E_L^- \quad \begin{bmatrix} N \\ E^- \end{bmatrix}_R, \quad U_L \quad \begin{bmatrix} U \\ D \end{bmatrix}_R$$

(b) Vector doublets

$$\begin{bmatrix} N \\ E^- \end{bmatrix}_L \quad \begin{bmatrix} N \\ E^- \end{bmatrix}_R, \quad \begin{bmatrix} U \\ D \end{bmatrix}_L \quad \begin{bmatrix} U \\ D \end{bmatrix}_R$$

(c) Vector singlets

$$E_L^- \quad E_R^-, \quad U_L \quad U_R, \quad D_L \quad D_R$$

Non-canonical L4 + 2HD + U(1)

non-canonical
4th generation leptons
w/ dark matter
+ U(1)_x
2HDM

CRC, Chiang, Lin, to appear

	SM fermions						Higgs	
	$Q_L \equiv \begin{pmatrix} u \\ d \end{pmatrix}_L$	u_R	d_R	$L_L \equiv \begin{pmatrix} \nu \\ e \end{pmatrix}_L$	e_R	ν_R	Φ_1	Φ_2
$SU(3)_C$	3	3	3	1	1	1	1	1
$SU(2)_L$	2	1	1	2	1	1	2	2
$U(1)_Y$	1/6	2/3	-1/3	-1/2	-1	0	1/2	1/2
$U(1)_X$	x_q	x_q	x_q	0	0	0	0	0
Z_2	+	+	-	+	-	+	+	-

	Fourth generation fermions						Scalar
	$Q_4 \equiv \begin{pmatrix} u \\ d \end{pmatrix}_{L4}$	u_{R4}	d_{R4}	$L_4 \equiv \begin{pmatrix} \nu \\ e \end{pmatrix}_{R4}$	e_{L4}	ν_{L4}	ϕ
$SU(3)_C$	3	3	3	1	1	1	1
$SU(2)_L$	2	1	1	2	1	1	1
$U(1)_Y$	1/6	2/3	-1/3	-1/2	-1	0	0
$U(1)_X$	x_{q4}	x_{q4}	x_{q4}	x_{L4}	x_{L4}	x_{L4}	x_ϕ
Z_2	+	+	-	+	-	+	+

CRC (NTNU)

additional decay mode of 4th generation fermions:

$$\text{e.g. } q_4 \rightarrow Z' + q_{SM} \text{ or } \phi + q_{SM}$$

$$L_4 \rightarrow \phi + L_{SM}$$

dark matter

Benchmark point

$$\begin{array}{lll} m_{u4} = 550 \text{ GeV} & m_H = 400 \text{ GeV} & m_{e4} = m_{\nu4} = 400 \text{ GeV} \\ m_{d4} = 500 \text{ GeV} & m_A = 810 \text{ GeV} & m_{H^\pm} = 600 \text{ GeV} \end{array}$$

Non-canonical L4

$$\mathcal{L}_{\text{Yukawa}} = - \left[f_{4i}^L \bar{L}_{R4} L_{Li} + f_{4i}^e \bar{e}_{L4} e_{Ri} + f_{4i} \bar{\nu}_{L4} \nu_{Ri} \right] \phi + h.c.$$

$$V_{2\text{HDM}} = m_{11}^2 |\Phi_1|^2 + m_{22}^2 |\Phi_2|^2 - m_{12}^2 (\Phi_1^\dagger \Phi_2 + \Phi_1 \Phi_2^\dagger) + \frac{\lambda_1}{2} |\Phi_1|^4 + \frac{\lambda_2}{2} |\Phi_2|^4 + \lambda_3 |\Phi_1|^2 |\Phi_2|^2 \\ + \lambda_4 |\Phi_1^\dagger \Phi_2|^2 + \frac{\lambda_5}{2} [(\Phi_1^\dagger \Phi_2)^2 + (\Phi_1 \Phi_2^\dagger)^2]$$

$$V_\phi = m_0^2 |\phi|^2 + \mu_\phi |\phi|^4 + \kappa_1 |\phi|^2 |\Phi_1|^2 + \kappa_2 |\phi|^2 |\Phi_2|^2$$

$$m_\phi = m_0^2 + \frac{1}{2} \kappa_1 v^2 \cos^2 \beta + \frac{1}{2} \kappa_2 v^2 \sin^2 \beta$$

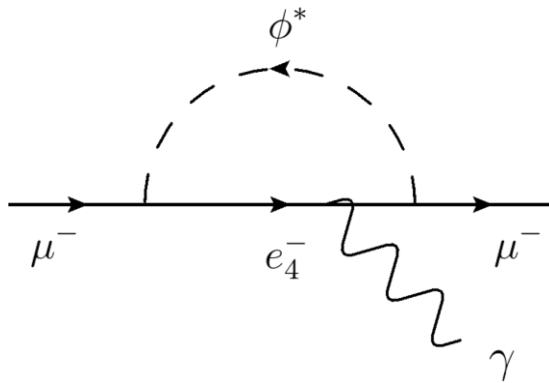
$$\lambda_h = v(-\kappa_1 \sin \alpha \cos \beta + \kappa_2 \cos \alpha \sin \beta)$$

$$\lambda_H = v(\kappa_1 \cos \alpha \cos \beta + \kappa_2 \sin \alpha \sin \beta).$$

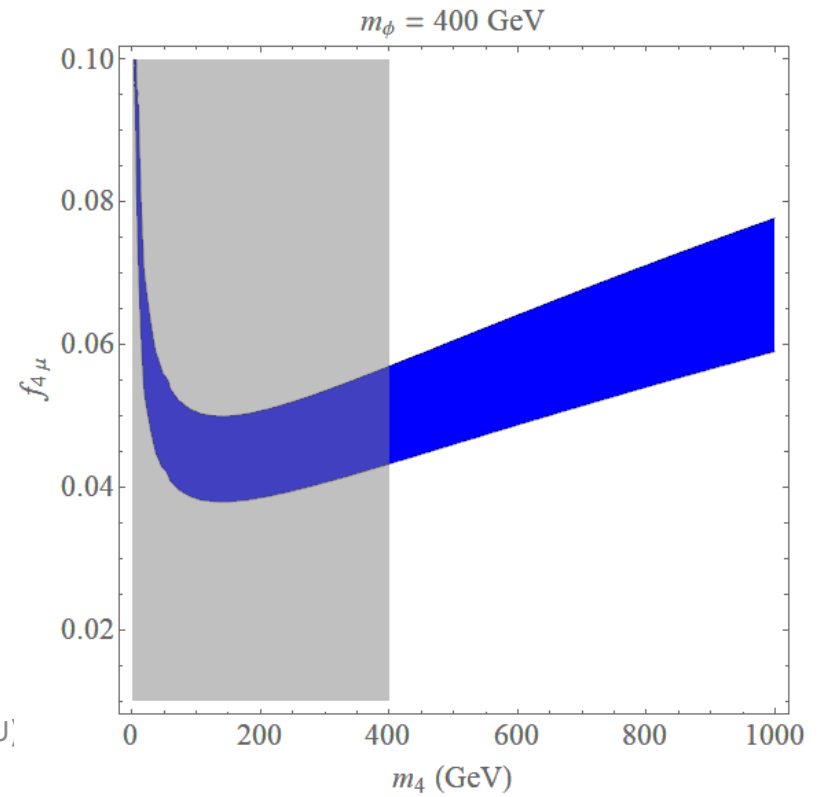
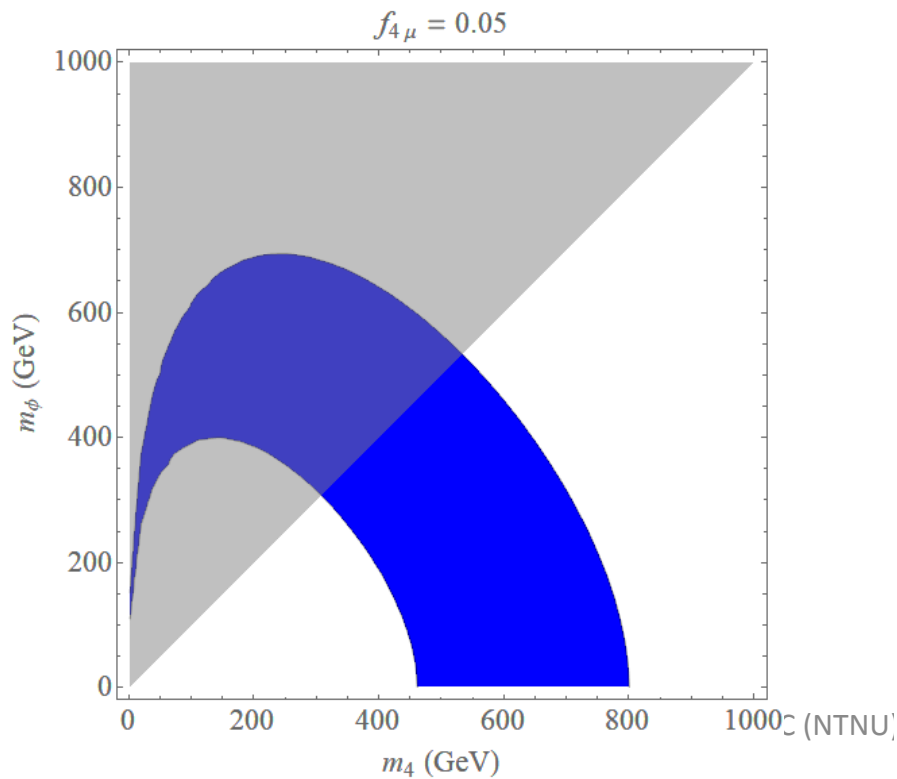
$$y_u^h = \frac{\cos \alpha}{\sin \beta} = \cos(\beta - \alpha) \cot \beta + \sin(\beta - \alpha)$$

$$y_d^h = -\frac{\sin \alpha}{\cos \beta} = \sin(\beta - \alpha) - \cos(\beta - \alpha) \tan \beta.$$

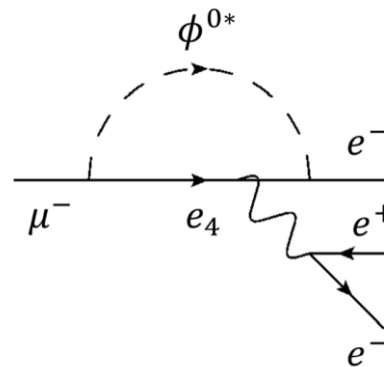
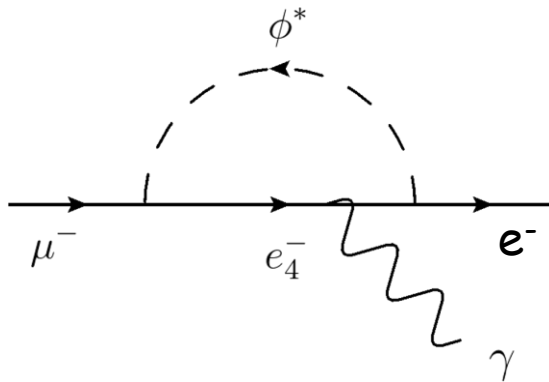
Muon g-2



$$\Delta a_\mu = \frac{|f_{4\mu}|^2}{8\pi^2} \int_0^1 dx \frac{x^2(m_\mu^2(1-x) + m_\mu m_4)}{(1-x)(m_\phi^2 - m_\mu^2 x) + m_4^2 x}$$



Lepton rare decay



$$\text{BR}(\mu^- \rightarrow e^- \gamma) < 4.2 \times 10^{-13}$$

$$\text{BR}(\tau^- \rightarrow e^- \gamma) < 3.3 \times 10^{-8}$$

$$\text{BR}(\tau^- \rightarrow \mu^- \gamma) < 4.4 \times 10^{-8}$$

$$\text{BR}(\mu^- \rightarrow e^- e^- e^+) < 1 \times 10^{-12}$$

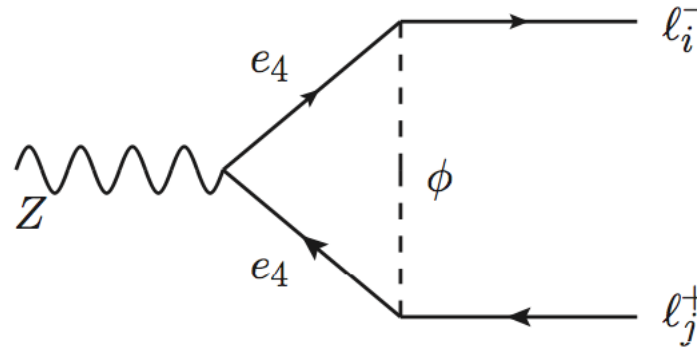
$$\propto \begin{aligned} & (f_{4e} f_{4\mu})^2 \\ & (f_{4e} f_{4\tau})^2 \\ & (f_{4\mu} f_{4\tau})^2 \\ & (f_{4e} f_{4\mu})^2 \end{aligned}$$

$$\text{take } f_{4\mu} \simeq 0.05 \quad f_{4e} \lesssim 5 \times 10^{-7}$$

$$f_{4\tau} \lesssim 5 \times 10^{-5}$$

A.M. Baldini, et al., MEG Collaboration, Eur. Phys. J. C 76 (8) (2016) 434, <https://doi.org/10.1140/epjc/s10052-016-4271-x>, arXiv:1605.05081 [hep-ex].
 C. Patrignani, et al., Particle Data Group, Chin. Phys. C 40 (10) (2016) 100001, <https://doi.org/10.1088/1674-1137/40/10/100001>.
 G.M. Pruna, EPJ Web Conf. 179 (2018) 01019, <https://doi.org/10.1051/epjconf/201817901019>, arXiv:1801.04709 [hep-ph].

Z rare decay



$$\text{BR}(Z \rightarrow e_i^\pm e_j^\mp) = \frac{m_Z}{12\pi\Gamma_Z} [2(f_V^2 + f_A^2) + (f_M^2 + f_E^2)m_Z^2]$$

$$\text{BR}(Z \rightarrow e^\pm \mu^\mp) < 1.7 \times 10^{-6}$$

$$\text{BR}(Z \rightarrow e^\pm \tau^\mp) < 9.8 \times 10^{-6}$$

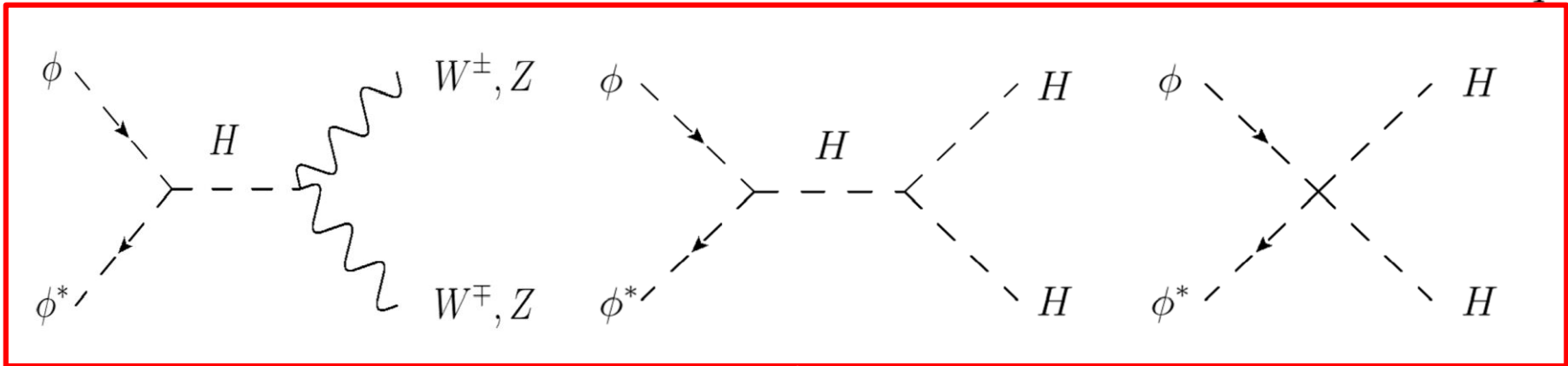
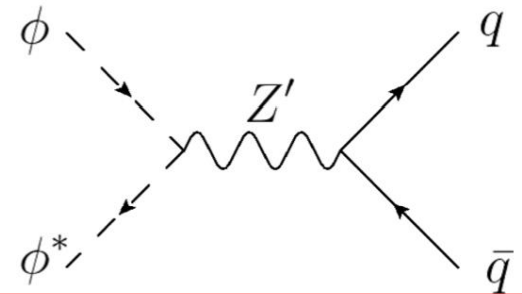
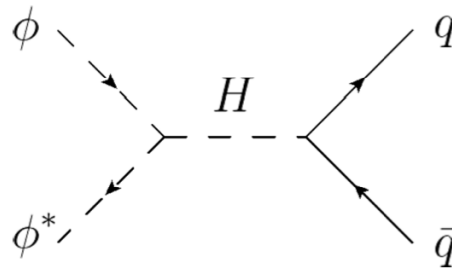
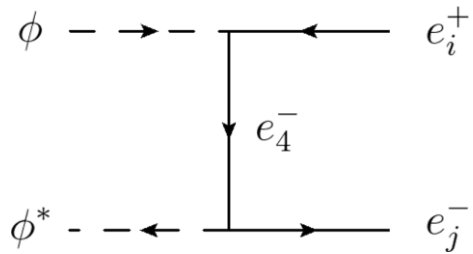
$$\text{BR}(Z \rightarrow \mu^\pm \tau^\mp) < 1.2 \times 10^{-5}$$

J.I. Illana, T. Riemann, Phys. Rev. D 63 (2001) 053004, <https://doi.org/10.1103/PhysRevD.63.053004>, arXiv:hep-ph/0010193.

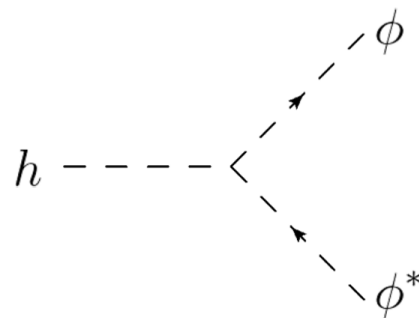
the constraints on f_{4e} and $f_{4\tau}$ are NOT as stringent as the limits from charged lepton rare decays.

Dark Matter

dark matter annihilation



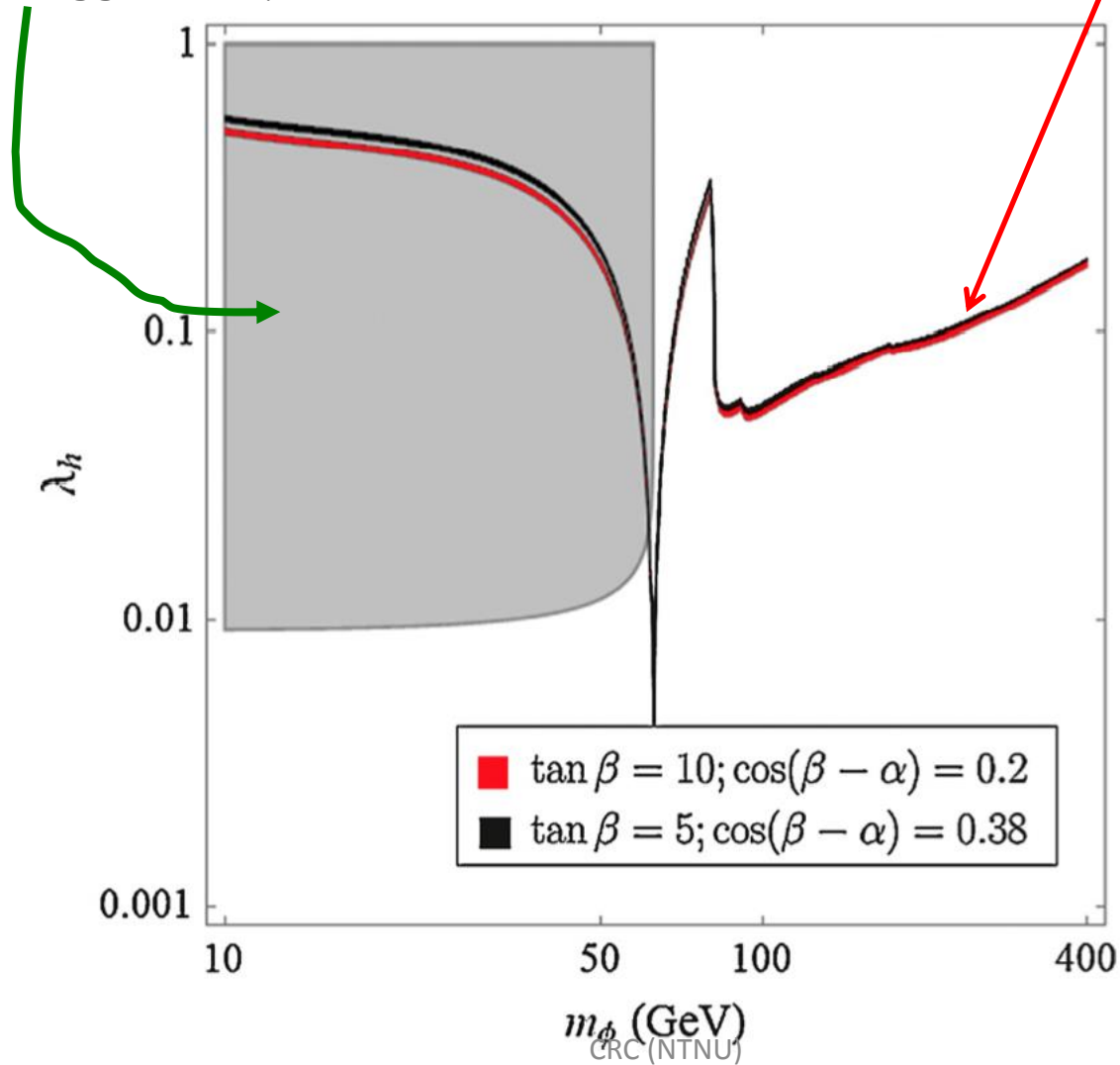
Higgs invisible decay



Dark Matter

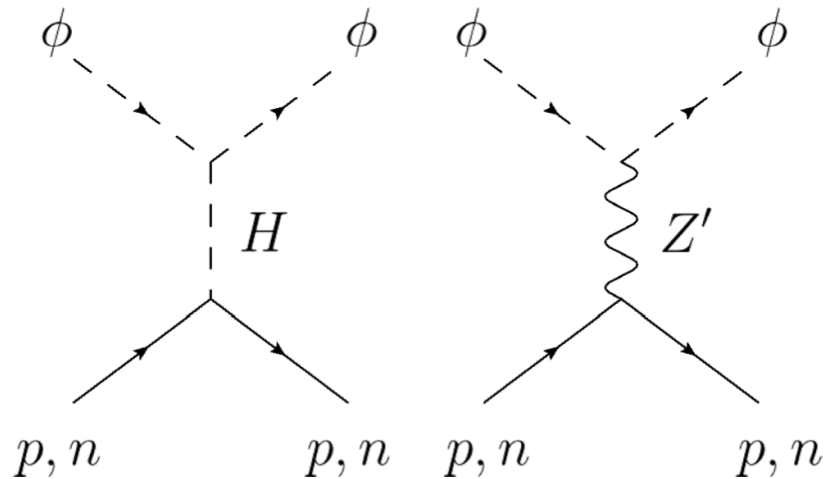
$$\Omega h^2 = 0.12 \pm 0.0012$$

invisible Higgs decay



Dark Matter

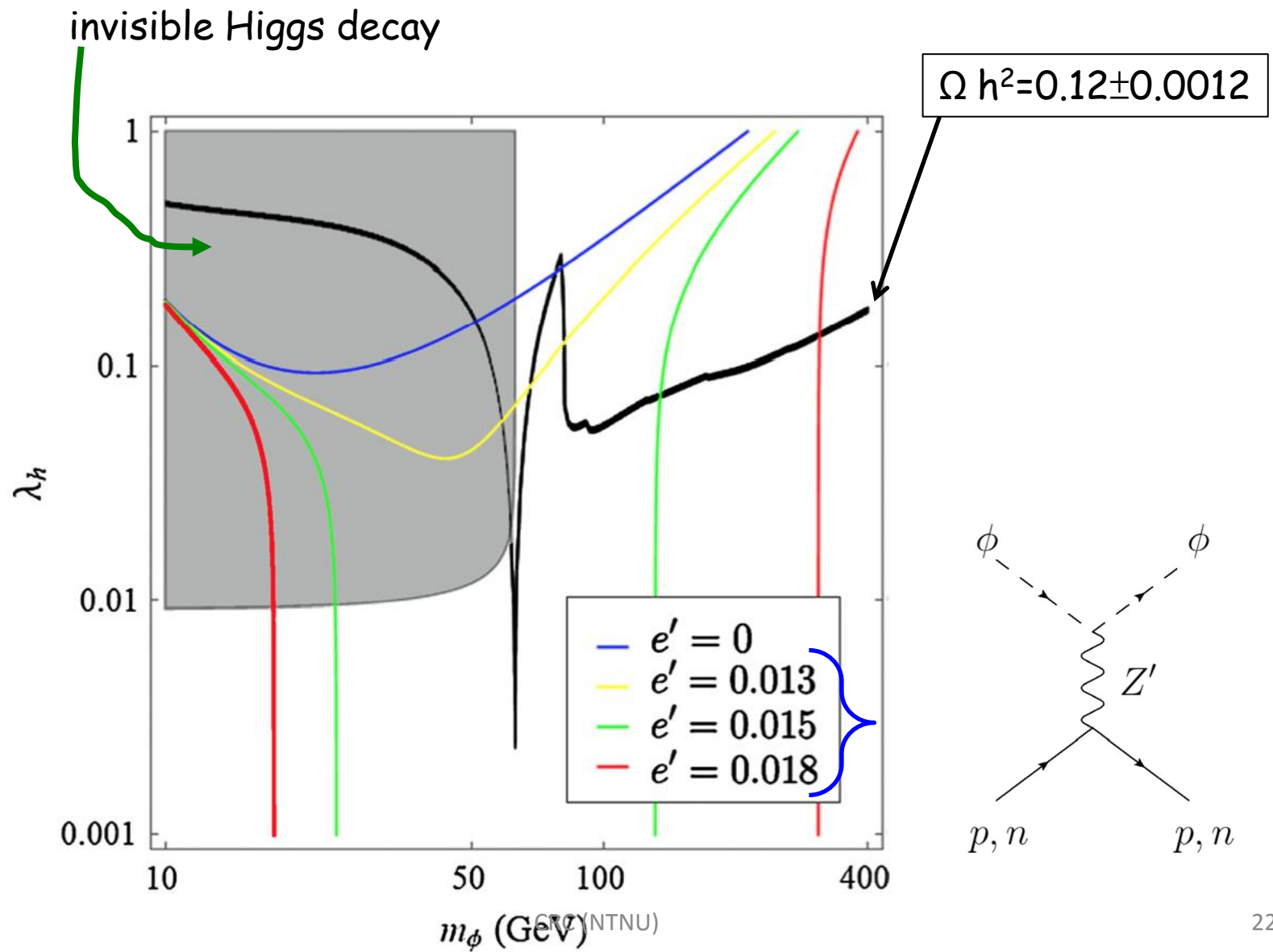
dark matter nucleon elastic scattering



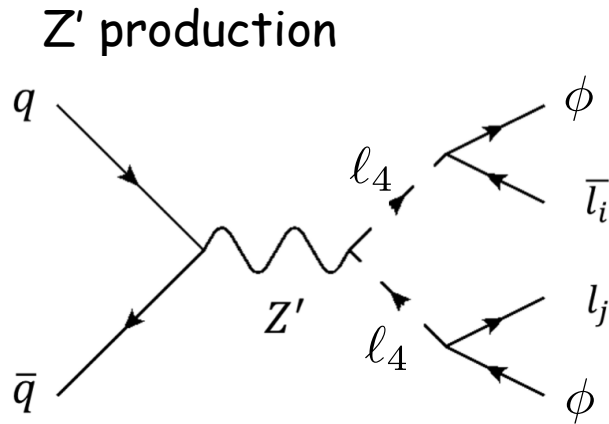
$$\sigma_{\phi p(n)}^{SI-h} = \frac{m_{p(n)}^2}{4\pi(m_\phi + m_{p(n)})^2} f_S^{p(n)2}$$

$$\sigma_{\phi p(n)}^{SI-Z'} = \frac{16e'^4 m_\phi^2 m_{p(n)}^2}{\pi(m_\phi + m_{p(n)})^2 m_{Z'}^4}$$

Dark Matter



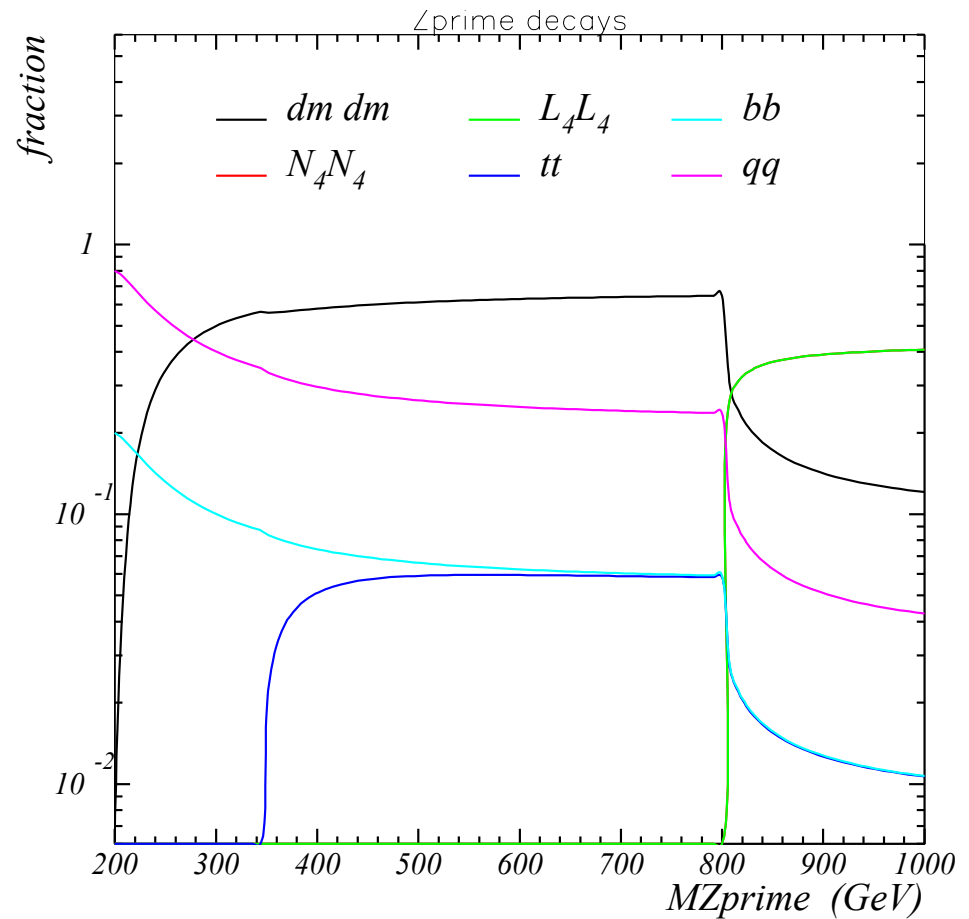
LHC Pheno



Signals:

flavor non-conserving lepton pair + missing ET

monjet+ missing ET



Summary

- * The existence of Dark Matter requires BSM
- * long-standing discrepancy between TH and EXP in muon $g-2$ may show the hints of BSM.
- * Fourth generation fermions in 2HDM is still possible!
- * With non-canonical charge assignment under SM and an additional $U(1)$, 4th generation lepton can provide a possible explanation for muon $g-2$ anomaly and dark matter.
- * LHC phenomenology is worth a detailed study!

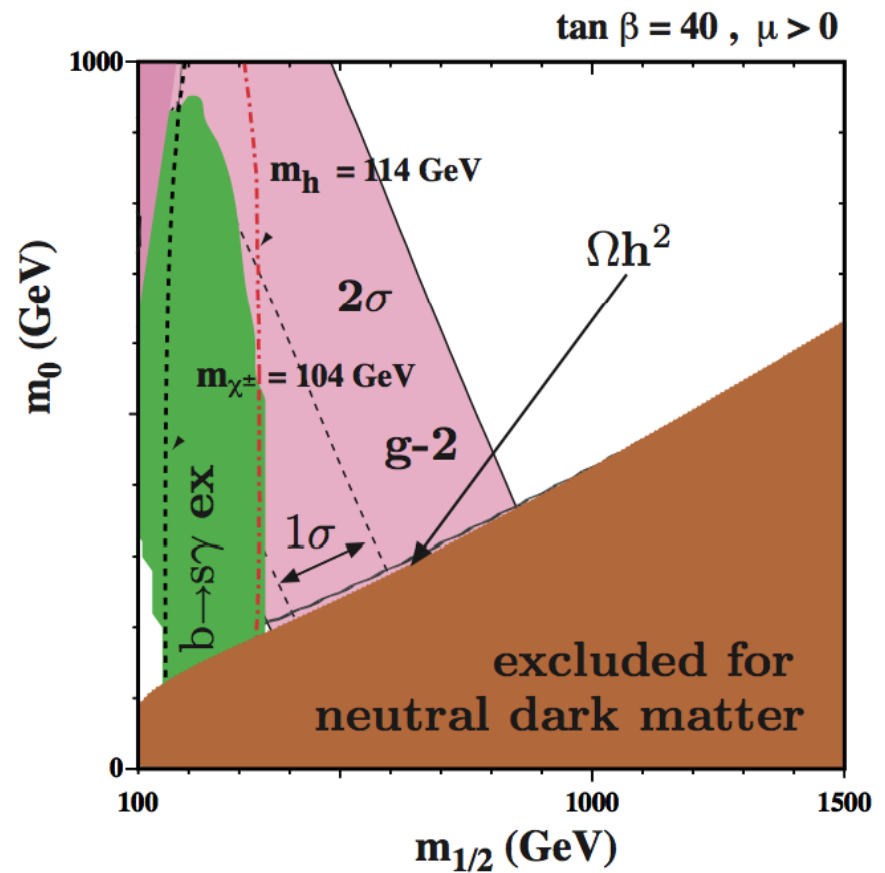
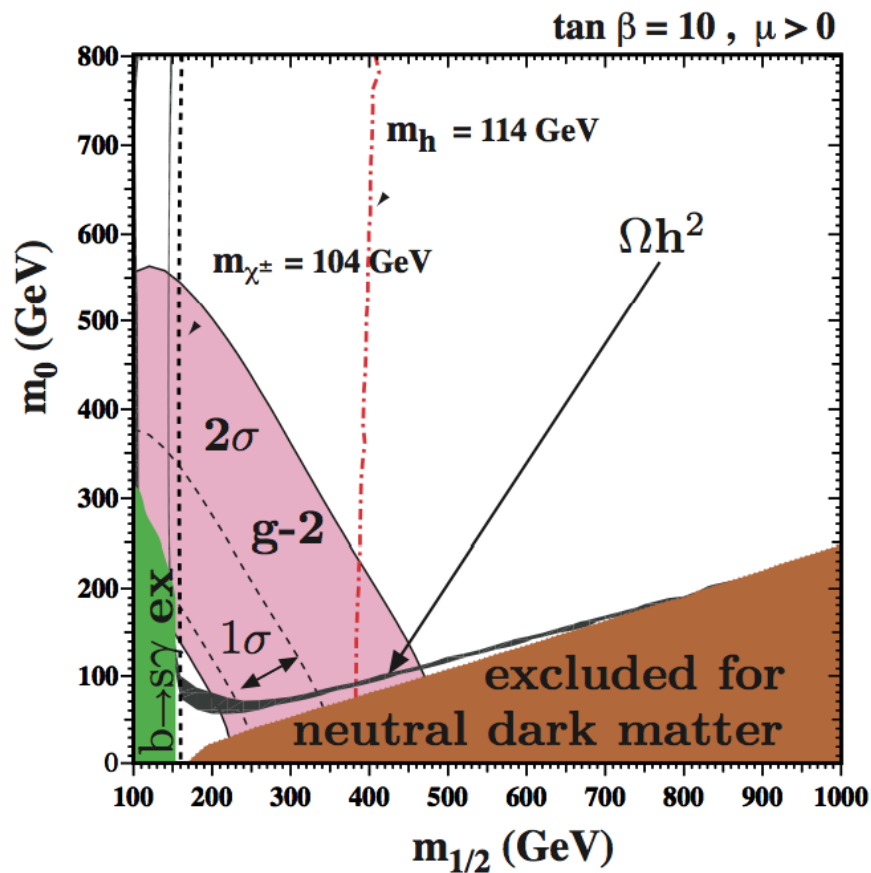
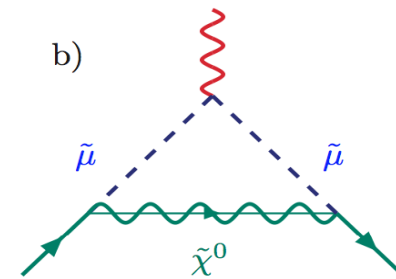
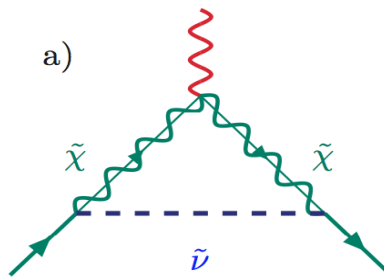


Backup



NP g_μ -2

SUSY (CMSSM)



Ellis, Olive, Santoso, Spanos, PLB 565(2003) 176
 Olive, Eur. Phys. J. C 59(2009) 269

General 2HDM

$$\begin{aligned}
 H f \bar{f}, \quad f = b, t & \quad -\frac{g}{2} \left(\frac{m_b}{M_W} \frac{\cos \alpha}{\cos \beta}, \frac{m_t}{M_W} \frac{\sin \alpha}{\sin \beta} \right) \\
 h f \bar{f}, \quad f = b, t & \quad -\frac{g}{2} \left(-\frac{m_b}{M_W} \frac{\sin \alpha}{\cos \beta}, \frac{m_t}{M_W} \frac{\cos \alpha}{\sin \beta} \right) \\
 A f \bar{f}, \quad f = b, t & \quad -\gamma_5 \frac{g}{2} \left(\frac{m_b}{M_W} \tan \beta, \frac{m_t}{M_W} \cot \beta \right) \\
 H^+ b \bar{t} & \quad \frac{g}{\sqrt{2}} \left(\frac{m_b}{M_W} \tan \beta \frac{1 + \gamma_5}{2} + \frac{m_t}{M_W} \cot \beta \frac{1 - \gamma_5}{2} \right) V_{tb}
 \end{aligned}$$



NP g_μ -2

Little Higgs

$$a_\mu^{\text{LH}} \sim 10 \times 10^{-11},$$

Park, Song, PRD 69(2004) 115010

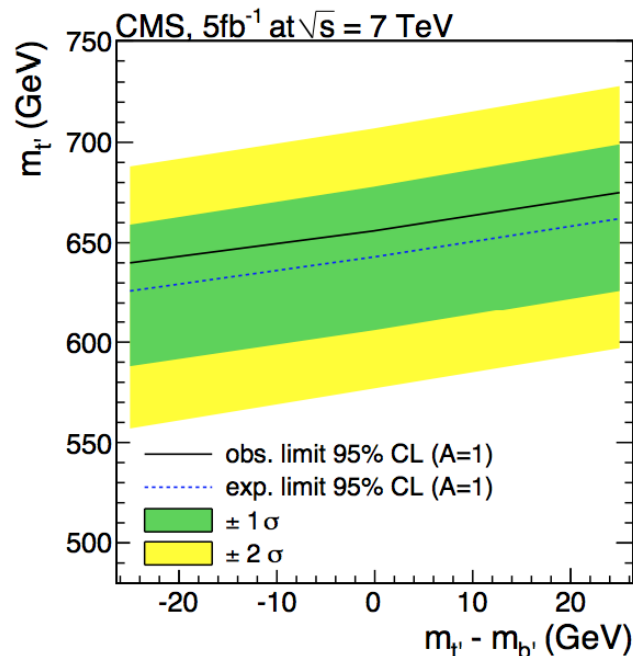
$$a_\mu^{\text{LHT}} < 12 \times 10^{-11}$$

Blanke et al., JHEP 0705(2007) 013

Sequential SM4

$$a_\mu^{\text{SM}}(W^+W^-N) \sim 233 \times 10^{-11} |V_{N\mu}|^2 F(x), \quad x = m_N^2/M_W^2$$

$|V_{N\mu}| > 0.7$ excluded by $Br(\mu \rightarrow e\gamma)$ Huo, Feng, hep-ph/0301153



The existence of 4th generation with mass below 685 GeV is excluded @ 95% CL.

CMS-PH-EP/2012-251, 1209.1062[hep-ex]

NP g_μ -2

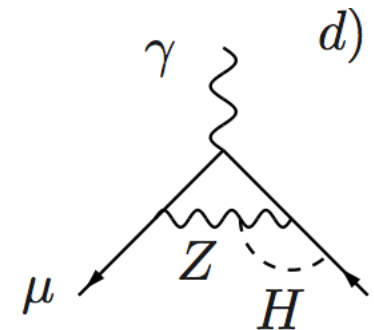
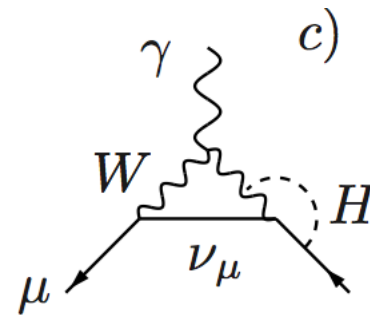
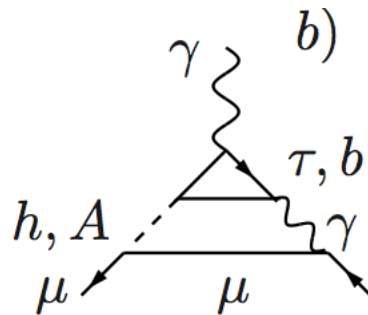
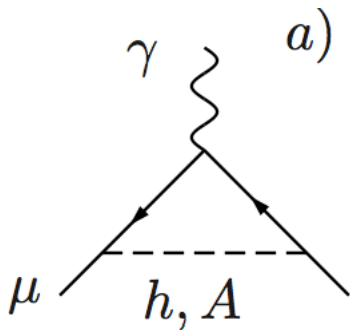
Krawczyk, hep-ph/0512371

Cheung, Kong, PRD68(2003) 053003

Wahab El Kaffas, Osland, Magne OGREID, PRD76(2007) 095001

Ellis, Hanh, Heinemeyer, Olive, Weiglein, JHEP 0710(2007) 092

general 2HDM



$(m_h, m_A, \tan \beta)$	$a_\mu^{(2)}(h)$	$a_\mu^{(2)}(A)$	$a_\mu^{(4)}(h)$	$a_\mu^{(4)}(A)$	sum
(100, 100, 10)	0.65	-0.62	-2.31	2.88	0.61
(100, 100, 40)	10.45	-9.89	-36.90	46.09	9.74
(100, 300, 10)	0.65	-0.08	-2.31	0.55	-1.18
(100, 300, 40)	10.45	-1.30	-36.90	8.85	-18.90

NOTE:

$$\Delta a_\mu(\text{E821} - \text{SM}) = (287 \pm 80) \times 10^{-11}$$