

# SUSY Inverse Seesaw gives Thermal Sneutrino Dark Matter

Hiroyuki Ishida (NCTS)

@ NCTS Annual Theory Meeting 2018: Particles, Cosmology and Strings  
2018/12/18

Collaborators: Jung Chang (Chonnam Natl. U.)

Kingman Cheung (NTHU)

Chih-Ting Lu (NTHU)

Martin Spinrath (NTHU)

Yue-Lin Sming Tsai (AS)

Refs: 1707.04374, 1806.04468

# Motivation

Why do we need to extend the SM?

- Neutrino masses
- Gauge hierarchy problem
- DM candidate
- Gauge coupling unification



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MSSM+type-I seesaw mechanism

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How small Majorana mass is possible?

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There are lots of alternative ideas

- Inverse seesaw (ISS) mechanism

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By using another gauge singlet

$$-\mathcal{L} \supset y_\nu \bar{L} H \nu_R + M_N \overline{\nu_R^C} \nu_R + M_S S S + \mu \nu_R S + \text{h.c.}$$

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Neutrino mass matrix

$$M_\nu = \begin{pmatrix} 0 & y_\nu v_{\text{EW}} & 0 \\ y_\nu^T v_{\text{EW}} & M_N & \mu \\ 0 & \mu & M_S \end{pmatrix} \Rightarrow m_\nu = -\frac{y_\nu v_{\text{EW}} M_S y_\nu^T v_{\text{EW}}}{\mu^2}$$

Small  $M_S$  (Lepton # violation) leads tiny  $m_\nu$



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Assumption in most of works  
technically naturalness

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when  $M_S \rightarrow 0$  lepton # sym. is recovered



smallness of  $M_S$  is technically natural



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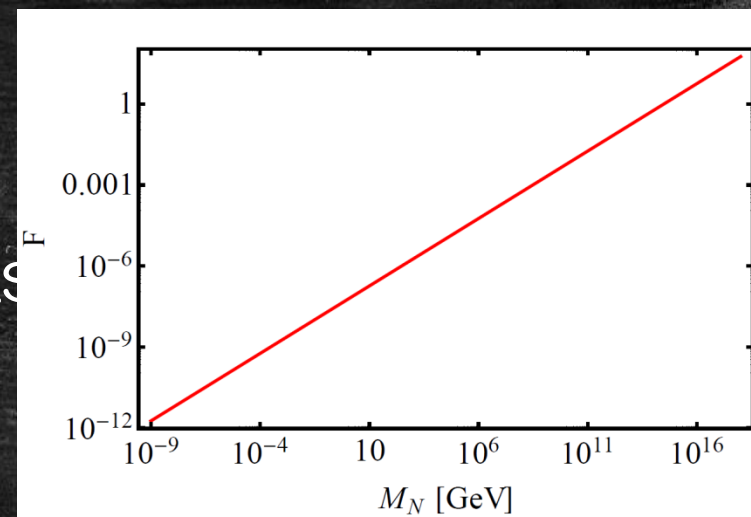
benefit of inverse seesaw

$$m_\nu = \left(\frac{y_\nu}{1}\right)^2 \left(\frac{v_{\text{EW}}}{10^2 \text{GeV}}\right)^2 \left(\frac{\text{TeV}}{\mu}\right)^2 \left(\frac{M_S}{10 \text{eV}}\right)$$

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extension at TeV scale with  $O(1)$  Yukawa



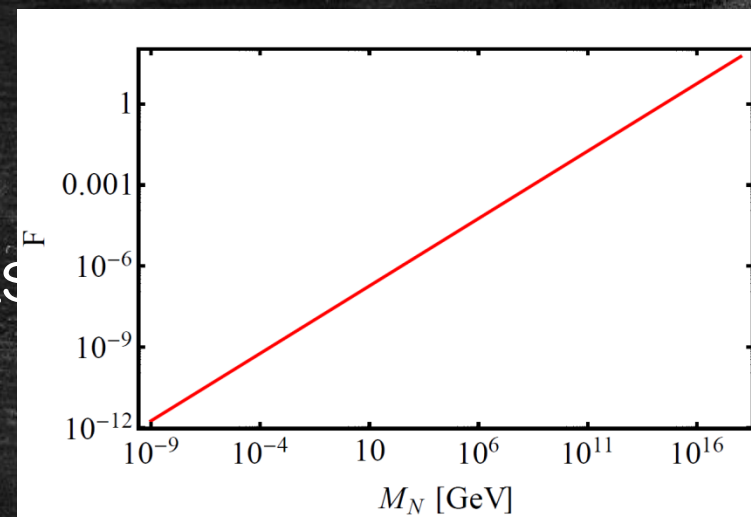
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Rich phenomenology at collider!

Dynamical origin of  $M_S$ ?

# Model (NCTS model)

Symmetry :  $\mathcal{G}_{\text{SM}} \times Z_6$

Superfield	$\hat{Q}_i$	$\hat{U}_i^c$	$\hat{E}_i^c$	$\hat{L}_i$	$\hat{D}_i^c$	$\hat{H}_u$	$\hat{H}_d$	$\hat{N}_\alpha^c$	$\hat{S}_\alpha$	$\hat{X}$
$Z_3$ charge	1	1	1	0	0	1	2	2	1	1
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$(\alpha = 1, 2)$



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New super potential in addition to MSSM

$$\mathcal{W}_\nu = Y_\nu \hat{L} \hat{H}_u \hat{N}^c + \mu_{\text{NS}} \hat{N}^c \hat{S} + \frac{\lambda}{2} \hat{X} \hat{S}^2 + \frac{\kappa}{3} \hat{X}^3$$



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related to neutrino

$$-\mathcal{L}_\nu = (Y_\nu)_{i\alpha} L_i N_\alpha^c H_u + (\mu_{\text{NS}})_{\alpha\beta} N_\alpha^c S_\beta + \frac{1}{2} \lambda_{\alpha\beta} S_\alpha S_\beta X + \text{H.c.}$$

# Model

## Phenomenological constraints?

### -LFV

1. Non-SUSY :  $\text{Br}(\mu \rightarrow e + \gamma) \simeq \mathcal{O}(10^{-20})$

2. SUSY : depends on sparticle mixing

### - $0\nu\beta\beta$ decay

1. Non-SUSY :  $m_{\text{eff}} \simeq 8 \times 10^{-9} \text{meV} \left( \frac{\mu_{NS}}{\text{TeV}} \right)$

2. SUSY : no contribution due to  
"R-parity" conservation



# DM estimation

## Boundary conditions

$$\begin{aligned} m_0^2 &= \frac{1}{9}m_{\tilde{Q}}^2 = \frac{1}{9}m_{\tilde{D}}^2 = \frac{1}{9}m_{\tilde{U}}^2 = m_{\tilde{L}}^2 = m_{\tilde{E}}^2 = m_{\tilde{N}}^2 = m_{\tilde{S}}^2 = m_{H_u}^2 = m_{H_d}^2 = b_{NS}, \\ M_{1/2} &= \frac{1}{3}M_3 = M_2 = M_1, \\ A_i &= A_0 Y_i, \quad A_\lambda = A_0 \lambda, \quad A_\kappa = \kappa A_0, \end{aligned}$$

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- Put arbitrary factor to make colored particles heavy enough
- $m_0$  and  $M_{1/2}$  are fixed at high scale
- $v_\chi$  and  $\kappa$  are fixed at low scale
- not to worry about running effect



# DM estimation

## Sneutrino mass matrix

$$m_{\tilde{\nu}_R}^2 \approx m_{\tilde{\nu}_I}^2 \approx \begin{pmatrix} m_0^2 + \frac{1}{2}M_Z^2 \cos(2\beta) & 0 & 0 \\ 0 & m_0^2 + \mu_{NS}^2 & m_0^2 \\ 0 & m_0^2 & m_0^2 + \mu_{NS}^2 \end{pmatrix}$$

-RG corrections to them is small enough

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-Physical states

$$\tilde{\nu}_{1,2} \approx \frac{1}{\sqrt{2}} \left( \tilde{N}_1^c \mp \tilde{S}_1 \right) \text{ and } \tilde{\nu}_3 \approx \tilde{L}_1$$

$$m_{\tilde{\nu}_1}^2 \approx \mu_{NS}^2$$

-Mass difference

$$m_{\tilde{\nu}_1^R}^2 - m_{\tilde{\nu}_1^I}^2 \approx \frac{1}{2} \lambda v_X \left( \sqrt{2} A_0 - 2\sqrt{2} \mu_{NS} + \kappa v_X \right)$$



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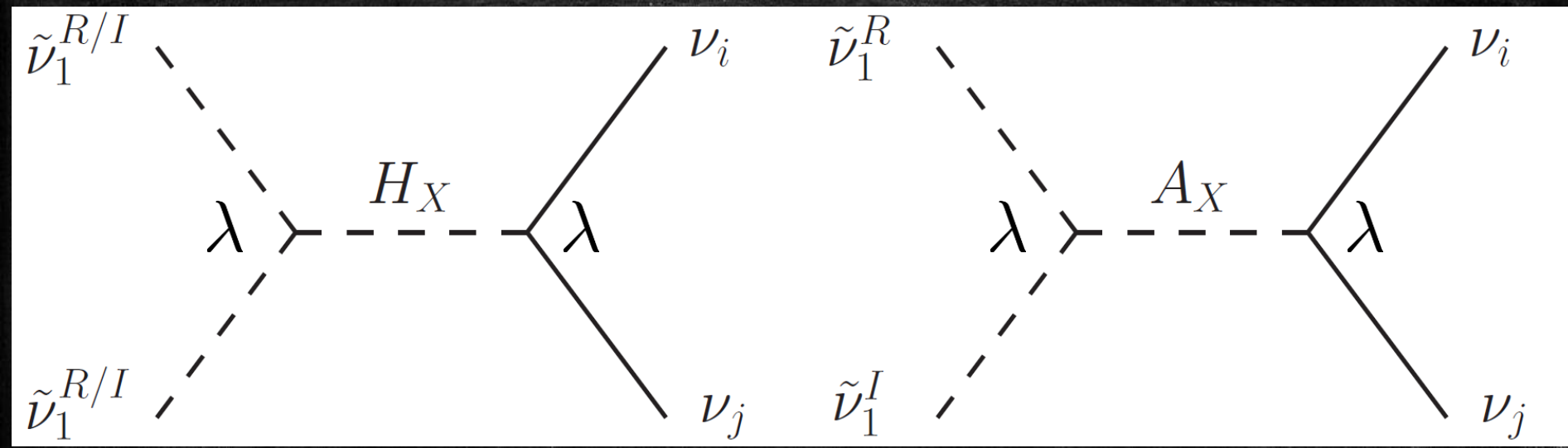
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Dominant (co-)annihilation channels



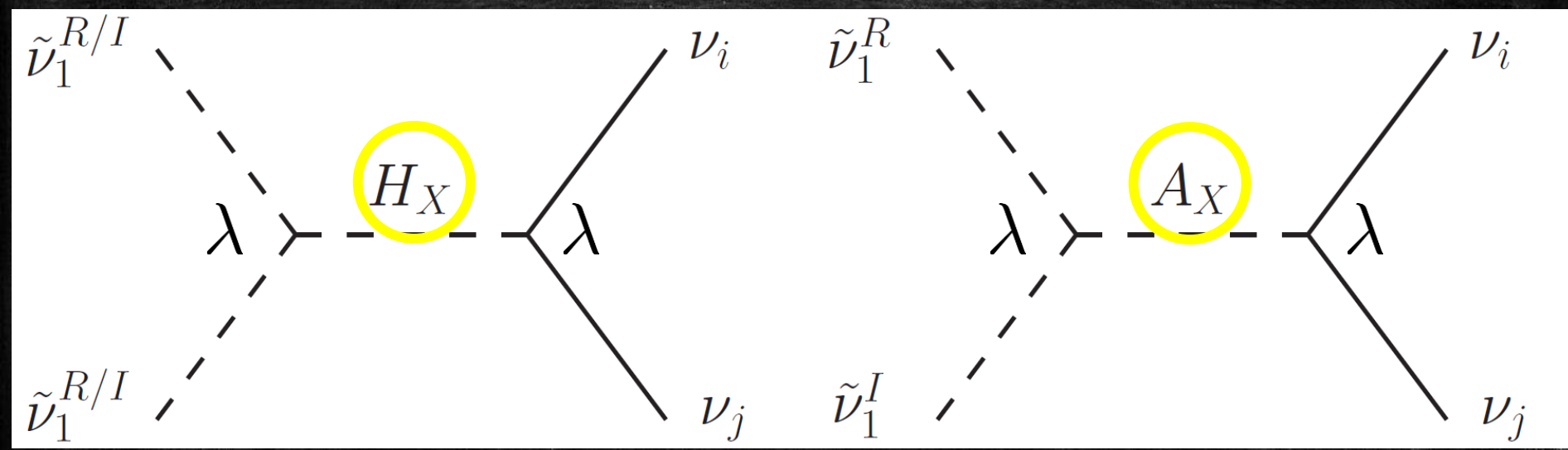
H-funnel

A-funnel



# DM estimation

## Dominant (co-)annihilation channels



H-funnel

A-funnel

Origin of  $\#L$  violation mediates  
between dark and visible sectors!

# DM estimation

## Features of our analysis

-Three exceptions of thermal relic calculation

[Griest and Seckel (1991)]

1. Co-annihilation
2. Annihilation into forbidden channel  
(near threshold)
3. Annihilation near pole (resonance)



# DM estimation

## Features of our analysis

-Three exceptions of thermal relic calculation  
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1. Co-annihilation
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We have to take into account 1 and 3!

$$m_{\tilde{\nu}_1^R} \simeq m_{\tilde{\nu}_1^I}, \quad m_{\tilde{\nu}_1^R} + m_{\tilde{\nu}_1^I} \simeq m_{A_X}$$

# DM estimation

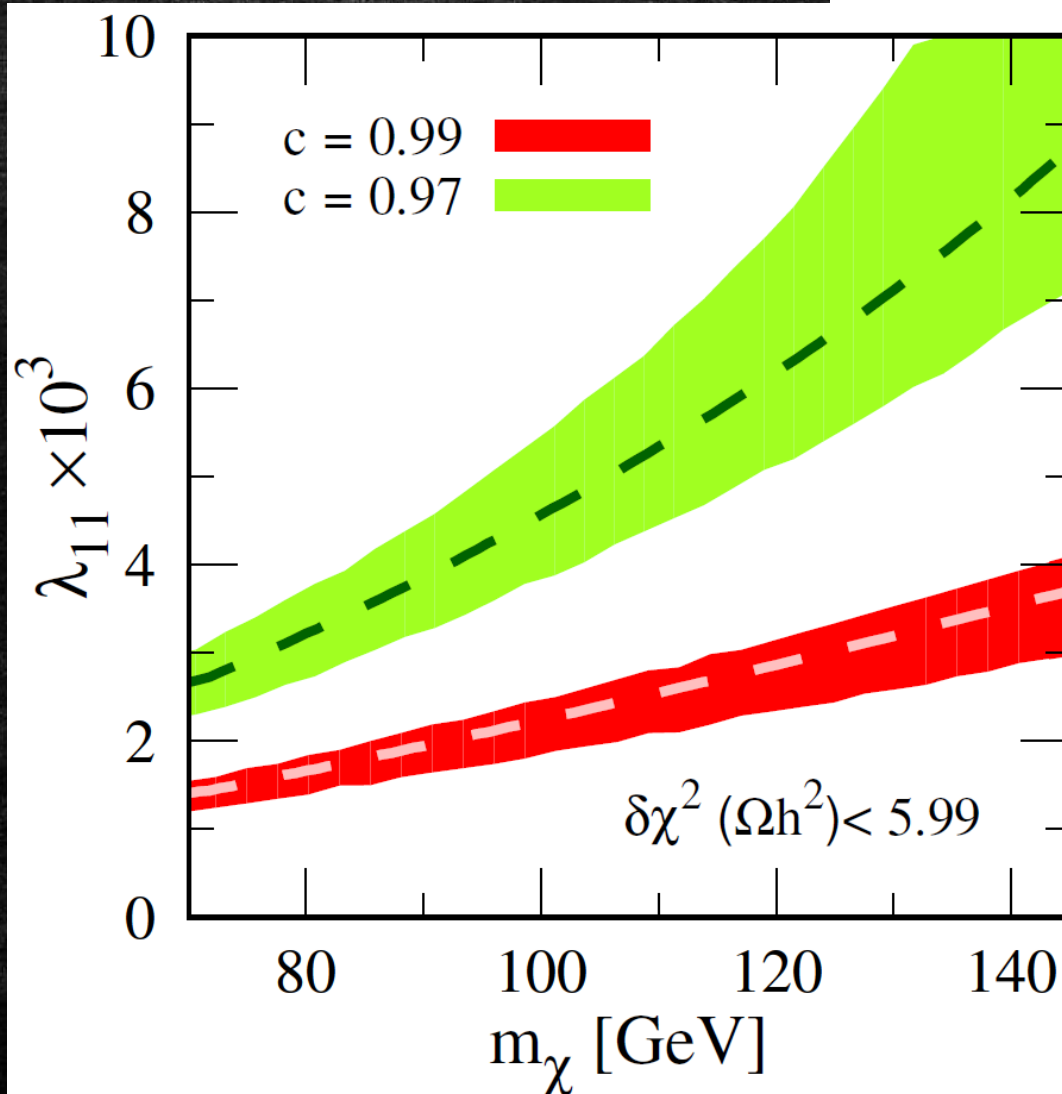
Results in  $A_x$ -funnel scenario



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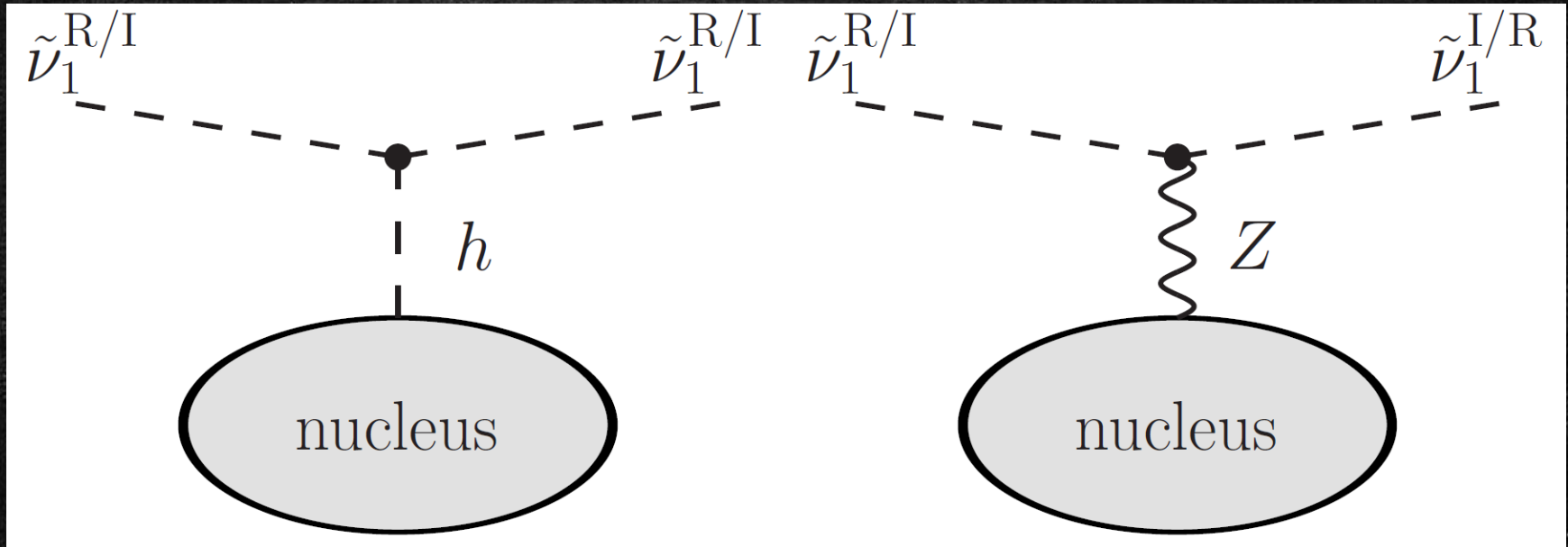
Results in  $A_X$ -funnel scenario

$$m_{\tilde{\nu}_1^R} + m_{\tilde{\nu}_1^I} = c m_{A_X}$$



# DM properties

## Direct detection

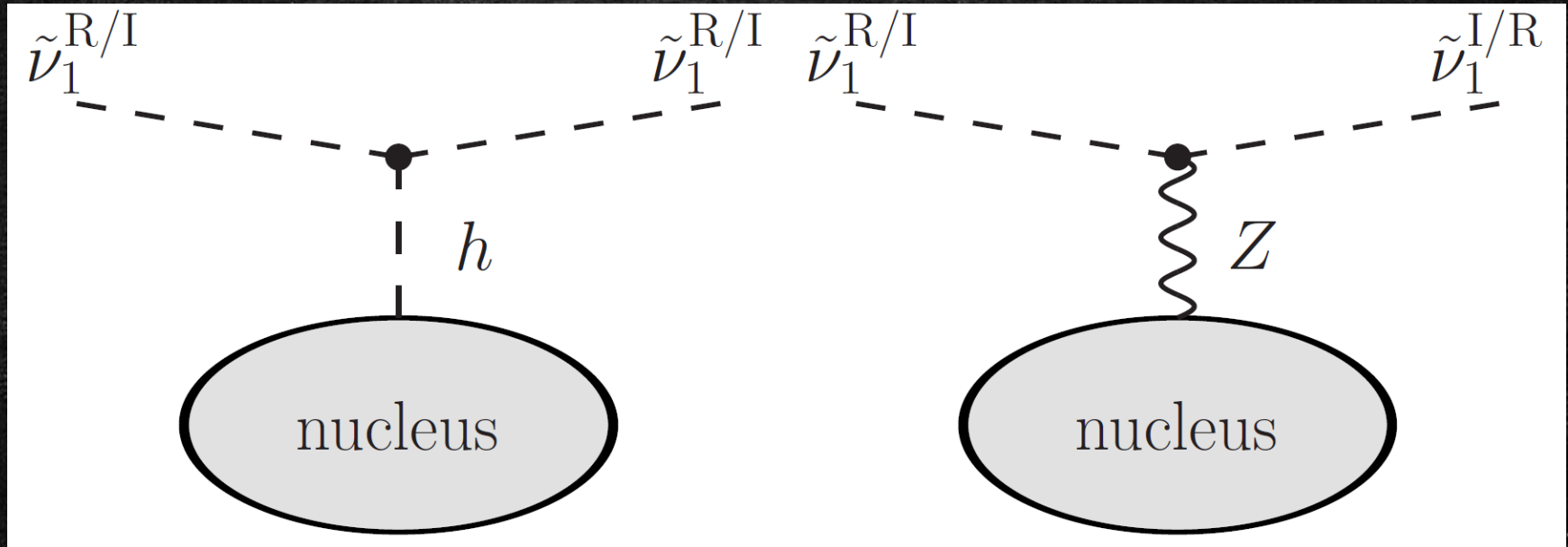


-Z exchange is more suppressed



# DM properties

## Direct detection



- Z exchange is more suppressed
- Using  $Y_{\nu} \sim 10^{-6}$  and  $M_{\text{SUSY}} = 1 \text{ TeV}$ , Higgs exchange cross section is given as  $O(10^{-29}) \text{ pb}$

DM p

Direct

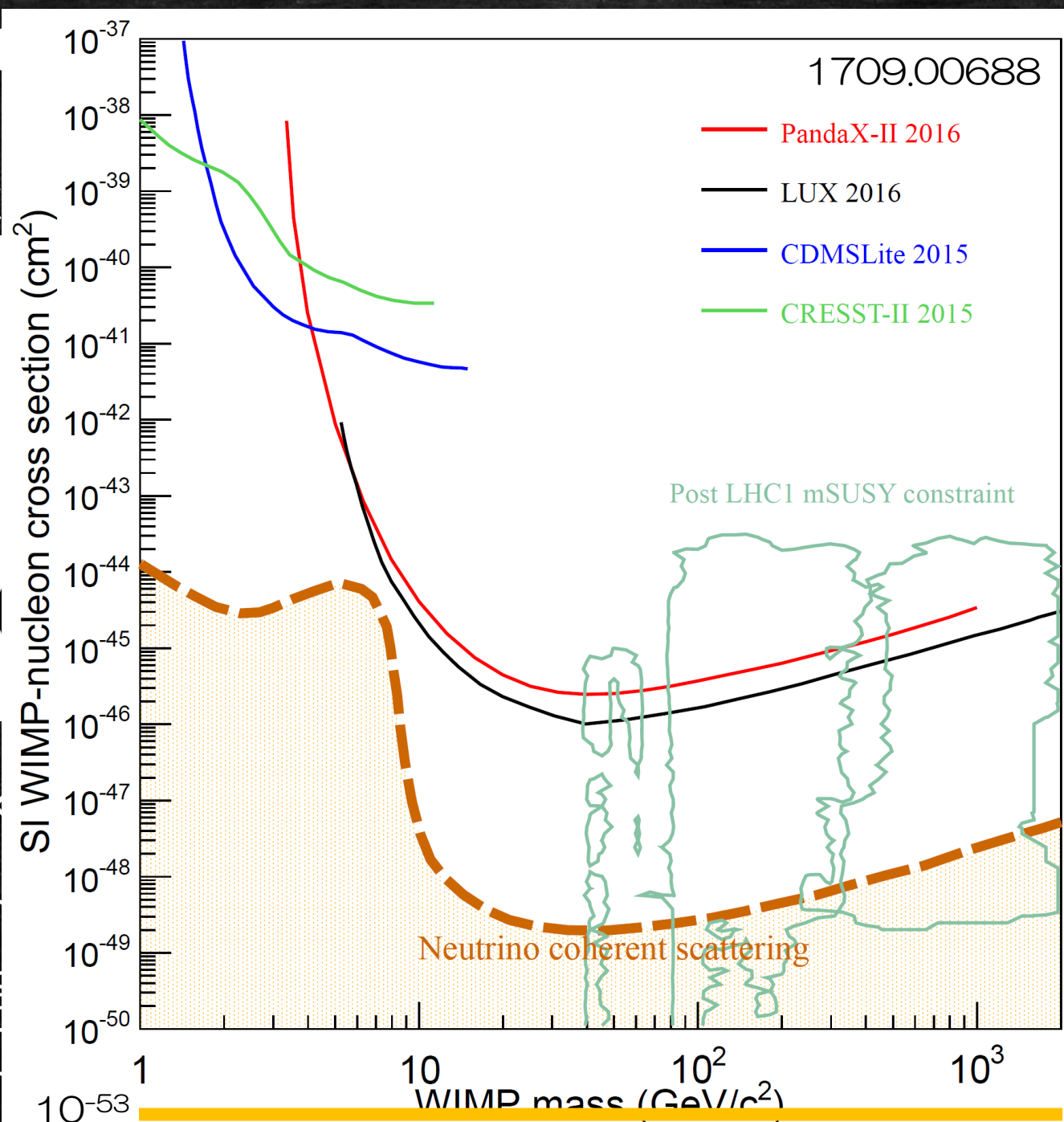
$\tilde{\nu}_1^{R/I}$

-Z ex

-Using

Higg

as C



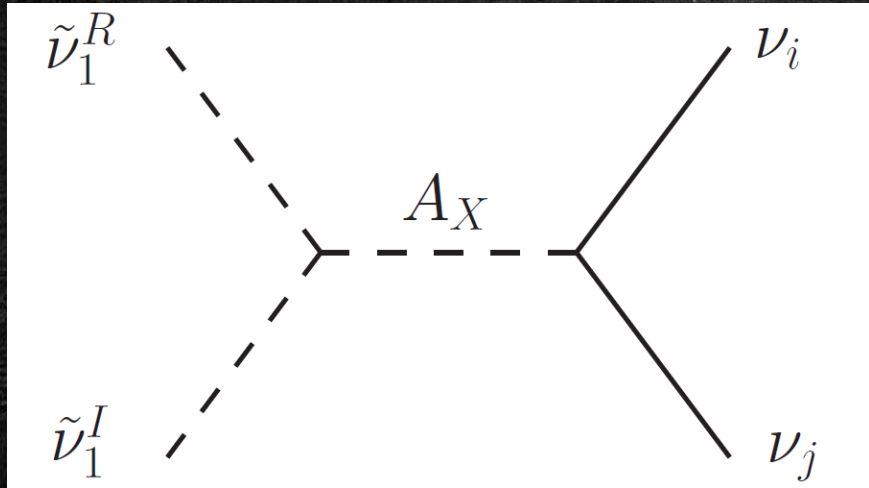
$\tilde{\nu}_1^{I/R}$

13



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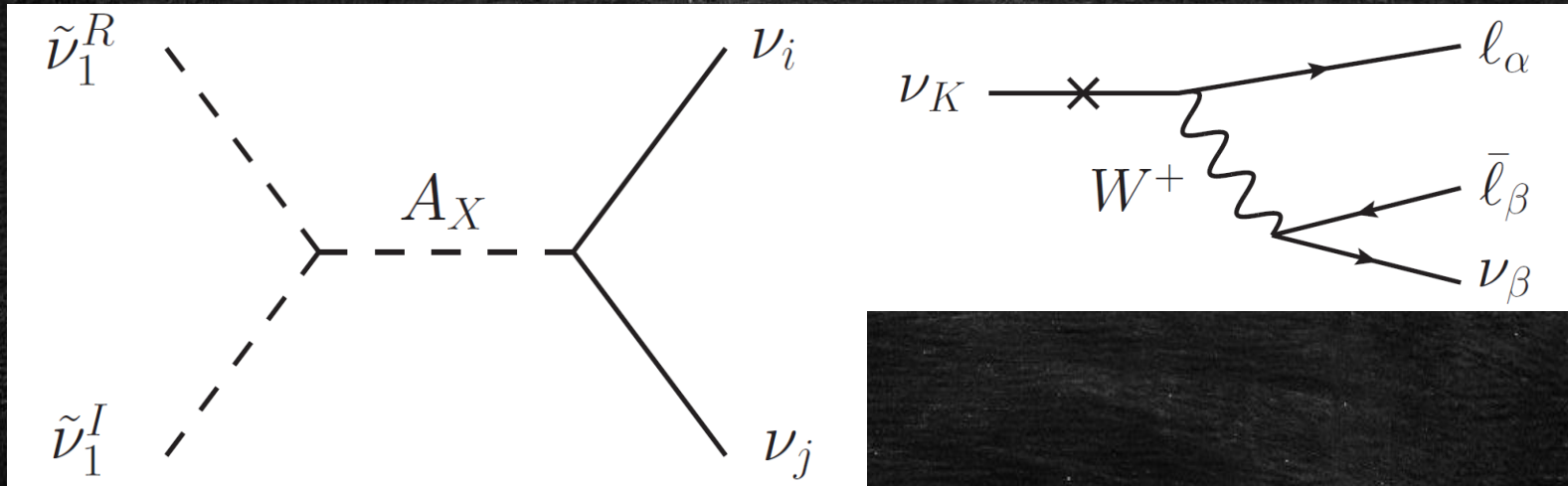
## Indirect detection



- If DM annihilate into two active neutrinos or one active and one heavy neutrino, we could see line signal of active  $\nu$  at IceCube
- Since annihilation cross section into two active neutrinos  $O(10^{-41})\text{cm}^3\text{s}^{-1}$ , this signal seems not to be so promising

# DM properties

## Indirect detection



- Since heavy  $\nu$  can decay into SM leptons, cascade decay could become important
- Cross section decaying into 2 heavy neutrinos is a few order of magnitude smaller, we could see signal in future



# Conclusions

- SUSY inverse seesaw model
  - Majorana mass term is dynamically induced
  - Low scale seesaw mechanism can be realized
  - Thermal relic sneutrino DM is possible thanks to existing the origin of  $\#L$  violation
  - Our extensions to MSSM is really hidden,

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  - Low scale seesaw mechanism can be realized
  - Thermal relic sneutrino DM is possible thanks to existing the origin of  $B-L$  violation
  - Our extensions to MSSM is really hidden,  
in other words,  
our model can be easily excluded by any other signals of DM!



Thank you  
for your attention

