

Axion-induced CMB B modes



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Axion-like DE and CDM

(too many references to list)

- Weak equivalence principle plus spin dictates a universal pseudoscalar (Ni 77)
- There exists at least one fundamental scalar – the Higgs boson !
- Axion monodromy – large-field inflation
- Peccei-Quinn symmetry breaking – QCD axion CDM
- Problems in small-scale structures – 10^{-22} eV scalar (maybe pseudoscalar) fuzzy CDM
- String axiverse – a plentitude of axions with a vast mass range 10^{-33} eV - 10^{-10} eV
- Extended string axiverse – axions as DE

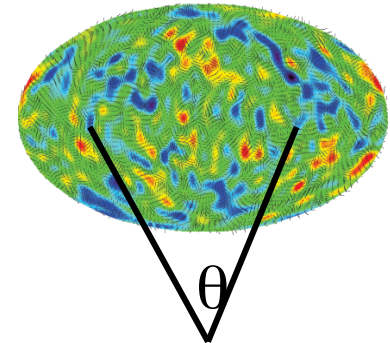
CMB Anisotropy and Polarization Angular Power Spectra

Decompose the CMB sky into a sum of spherical harmonics:

$$T(\theta, \varphi) = \sum_{lm} a_{lm} Y_{lm}(\theta, \varphi)$$

$$(Q - iU)(\theta, \varphi) = \sum_{lm} a_{2,lm} Y_{2,lm}(\theta, \varphi)$$

$$(Q + iU)(\theta, \varphi) = \sum_{lm} a_{-2,lm} Y_{-2,lm}(\theta, \varphi)$$

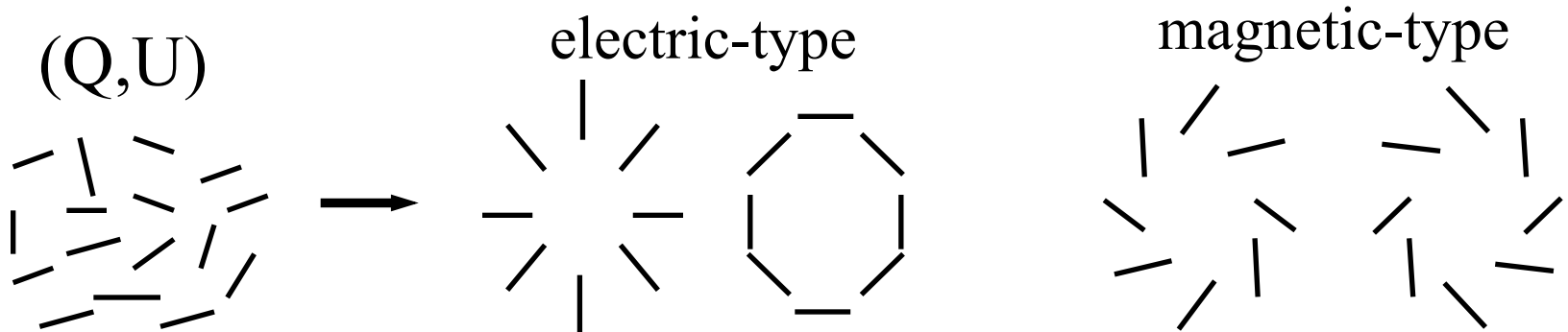


$$C_{l}^{TT} = \sum_m (a_{lm}^* a_{lm}) \quad \text{Anisotropy power spectrum} \quad l = 180 \text{ degrees} / \theta$$

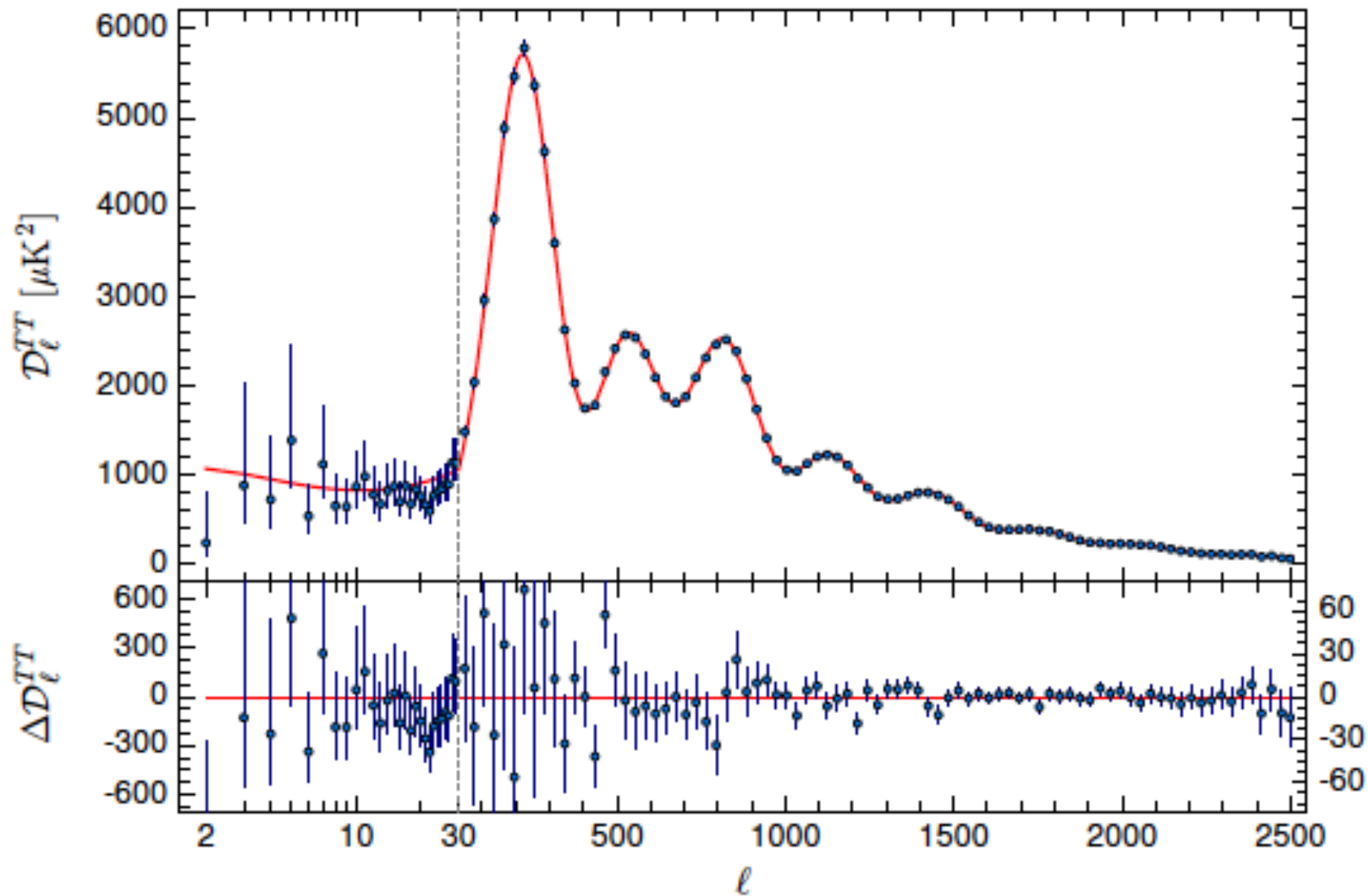
$$C_{l}^{EE} = \sum_m (a_{2,lm}^* a_{2,lm} + a_{2,lm}^* a_{-2,lm}) \quad \text{E-polarization power spectrum}$$

$$C_{l}^{BB} = \sum_m (a_{2,lm}^* a_{2,lm} - a_{2,lm}^* a_{-2,lm}) \quad \text{B-polarization power}$$

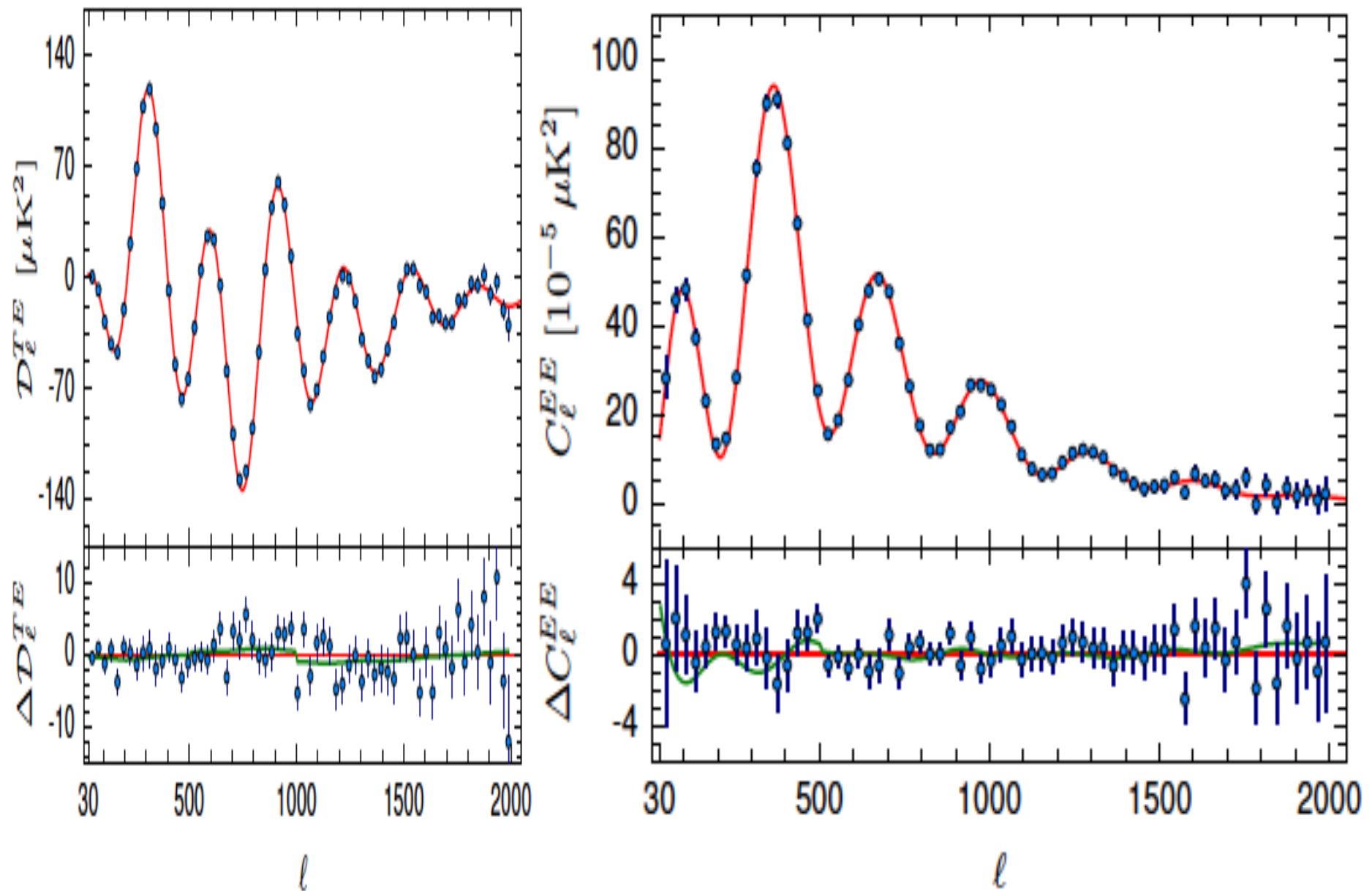
$$C_{l}^{TE} = - \sum_m (a_{lm}^* a_{2,lm}) \quad \text{TE correlation power spectrum}$$



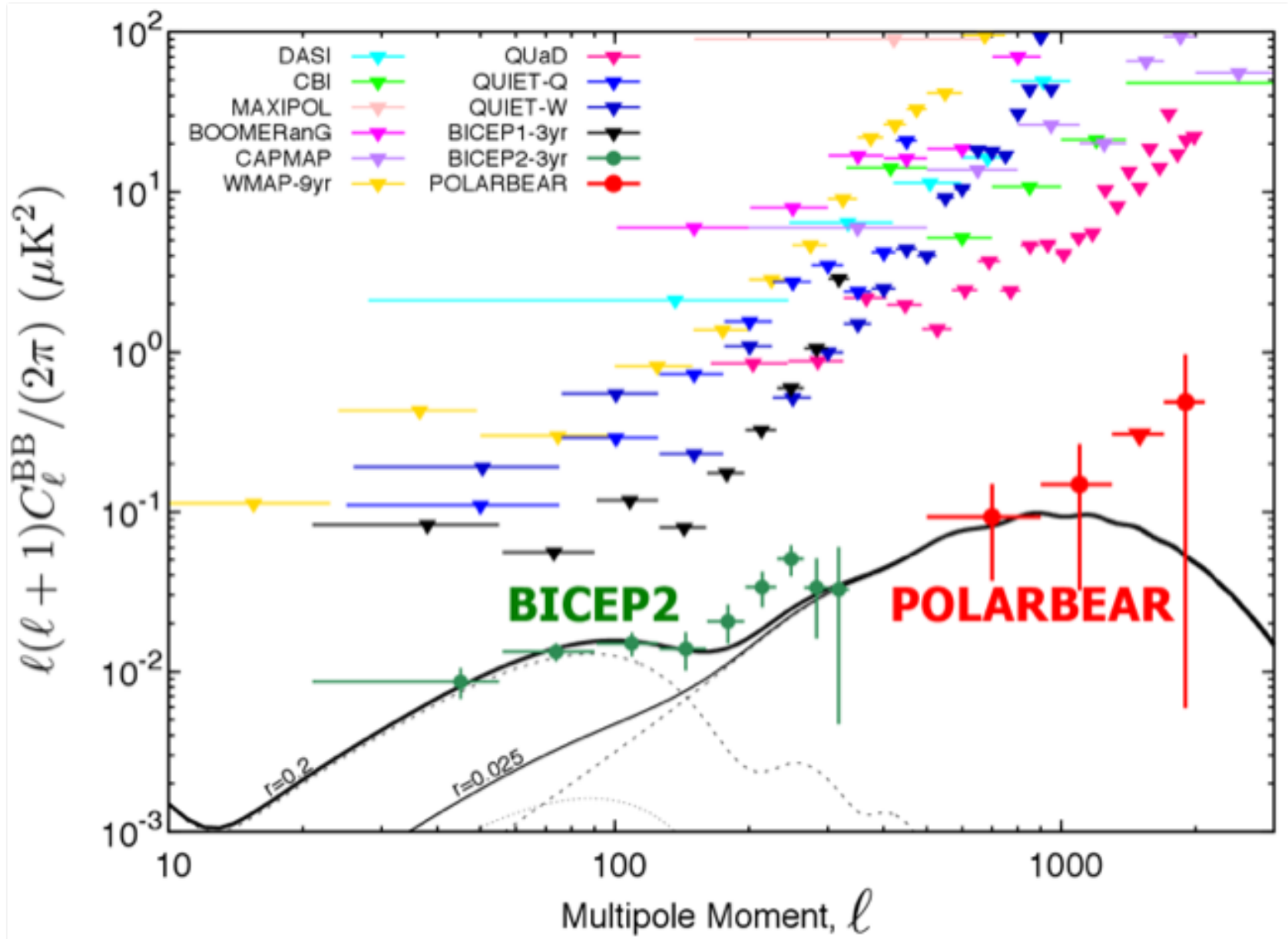
Planck CMB Anisotropy $D_{\ell}^{TT} = l(l+1) C_{\ell}^T$ 2015



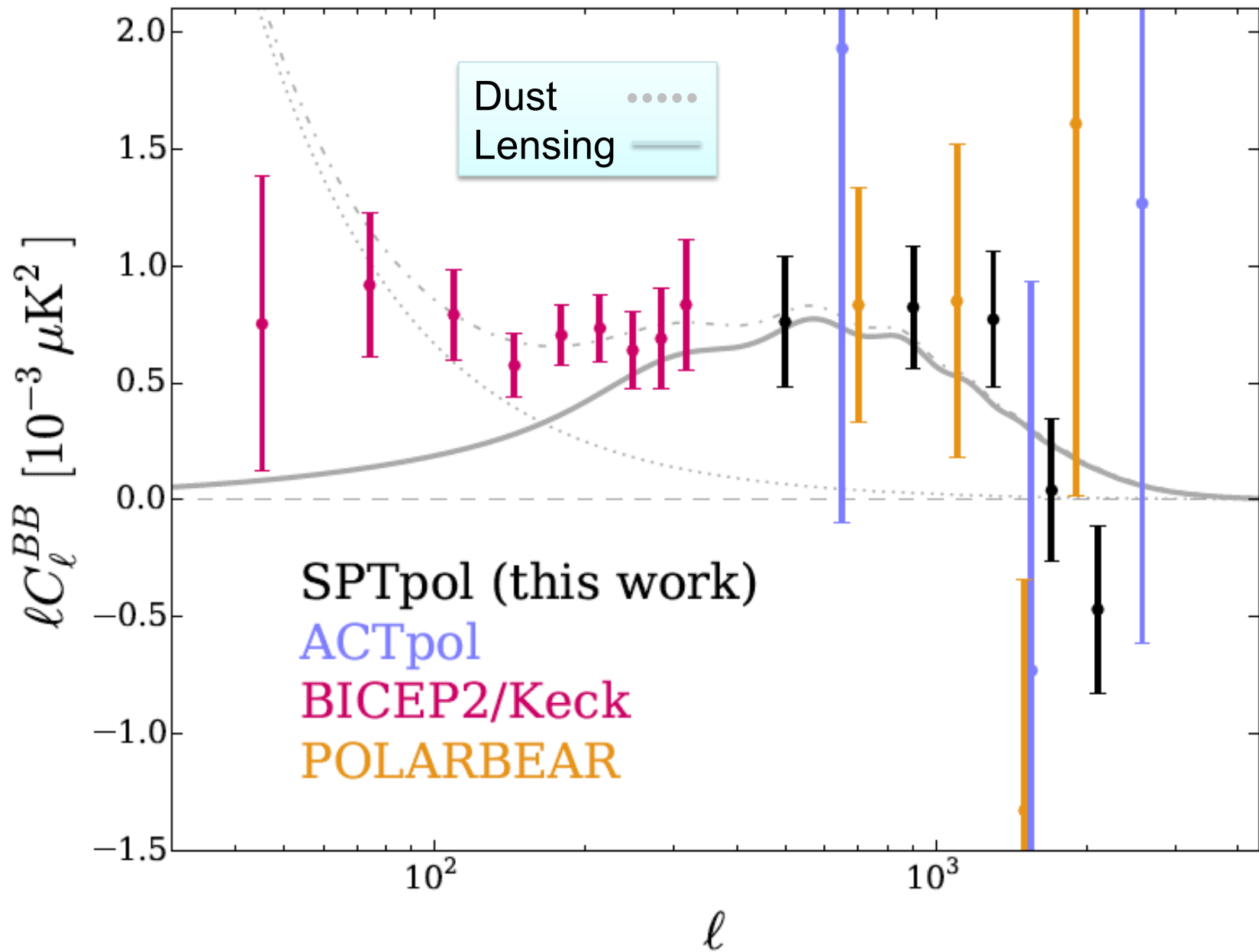
Planck CMB Polarization Power Spectra 2015



POLARBEAR+BICEP2 B-mode Detection



More B-mode detection



DE/DM Coupling to Electromagnetism

$$\mathcal{L}_N = -\frac{1}{4}\sqrt{-g}B_{F\tilde{F}}(\phi)F_{\mu\nu}\tilde{F}^{\mu\nu}, \quad \text{where } \phi \equiv \frac{\Phi}{M}, \quad M = M_{Pl}/\sqrt{8\pi}$$

This leads to photon dispersion relation Carroll,
Field,
Jackiw 90

$$n_{\pm} = \varepsilon \mp \frac{1}{2} \frac{\partial B_{F\tilde{F}}}{\partial \phi} \left(\frac{\partial \phi}{\partial \eta} + \vec{\nabla} \phi \cdot \hat{n} \right) \quad (\varepsilon, \vec{n}) \text{ is the photon four-momentum}$$

± left/right handed η conformal time

vacuum birefringence

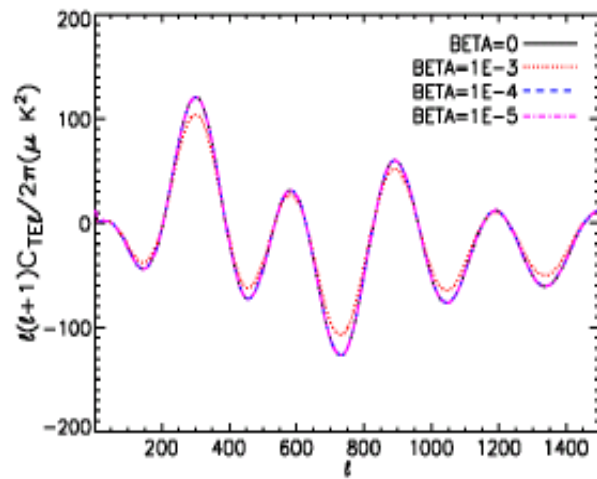
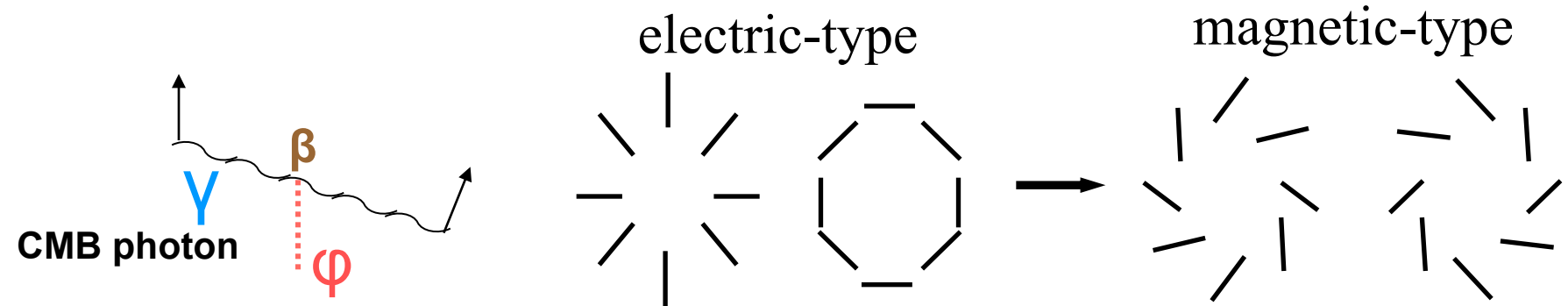
then, a rotational speed of polarization plane

$$\omega = \frac{1}{2}(n_+ - n_-) = -\frac{1}{2} \frac{\partial B_{F\tilde{F}}}{\partial \phi} \left(\frac{\partial \phi}{\partial \eta} + \vec{\nabla} \phi \cdot \hat{n} \right)$$

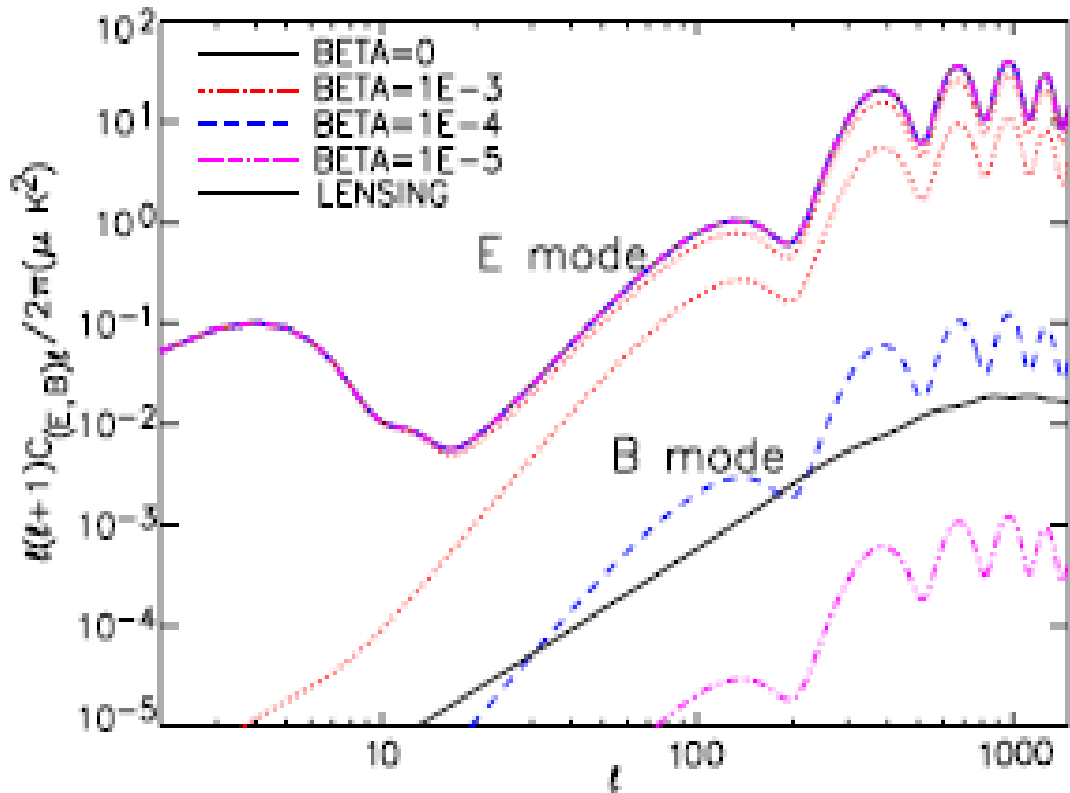
If $B=\beta\phi$, cooling of horizontal branch stars would imply $\beta < 10^7$

DE mean field induced vacuum birefringence – cosmic rotation of CMB polarization

Liu, Lee, Ng 06



TE spectrum



Radiative transfer equation

$$\dot{\Delta}_{Q\pm iU}(\vec{k}, \eta) + ik\mu\Delta_{Q\pm iU}(\vec{k}, \eta) = n_e\sigma_T a(\eta) \left[-\Delta_{Q\pm iU}(\vec{k}, \eta) \right. \\ \left. \sum_m \sqrt{\frac{6\pi}{5}} \pm_2 Y_2^m(\hat{n}) S_P^{(m)}(\vec{k}, \eta) \right] \mp i2\omega\Delta_{Q\mp iU}(\vec{k}, \eta),$$

$\mu = \hat{n} \cdot \vec{k}$,
 η : conformal time
 a : scale factor
 n_e : e density
 σ_T : Thomson cross section

Source term for polarization

$$S_P^{(m)}(\vec{k}, \eta) \equiv \Delta_{T2}^{(m)}(\vec{k}, \eta) + 12\sqrt{6}\Delta_{+,2}^{(m)}(\vec{k}, \eta) + 12\sqrt{6}\Delta_{-,2}^{(m)}(\vec{k}, \eta)$$

Cosmic rotation

$$\bar{\omega}(\eta) = -\frac{1}{2}\beta_{F\tilde{F}} \frac{d\bar{\phi}}{d\eta}.$$

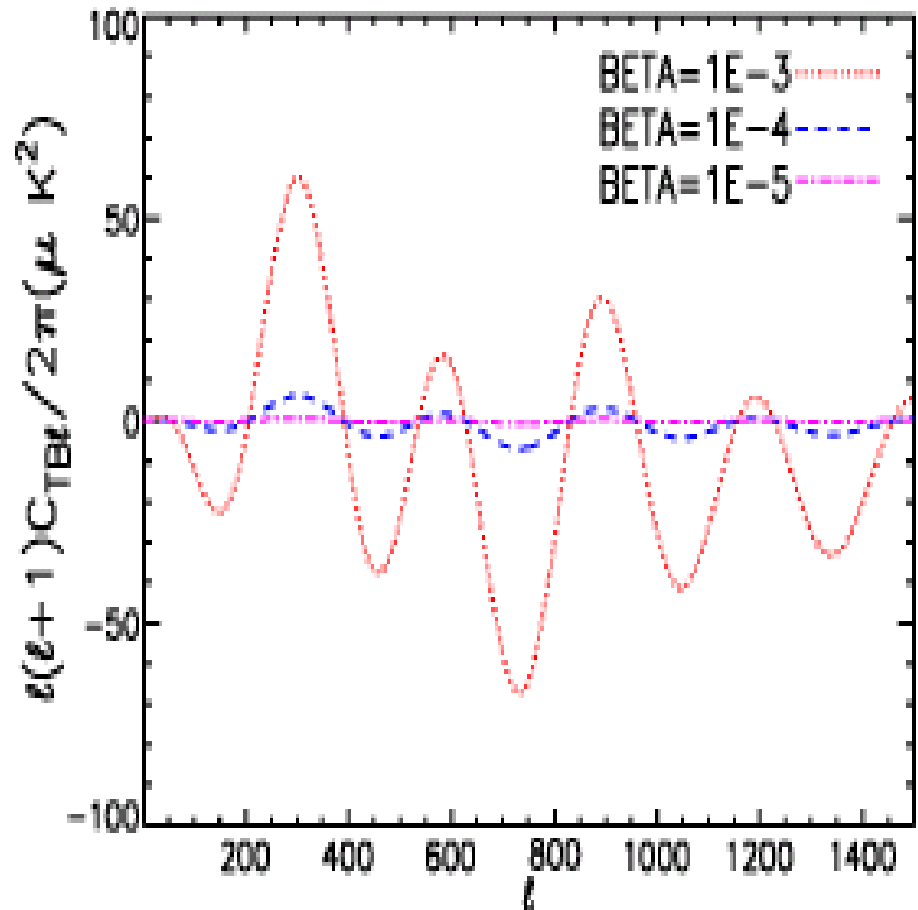
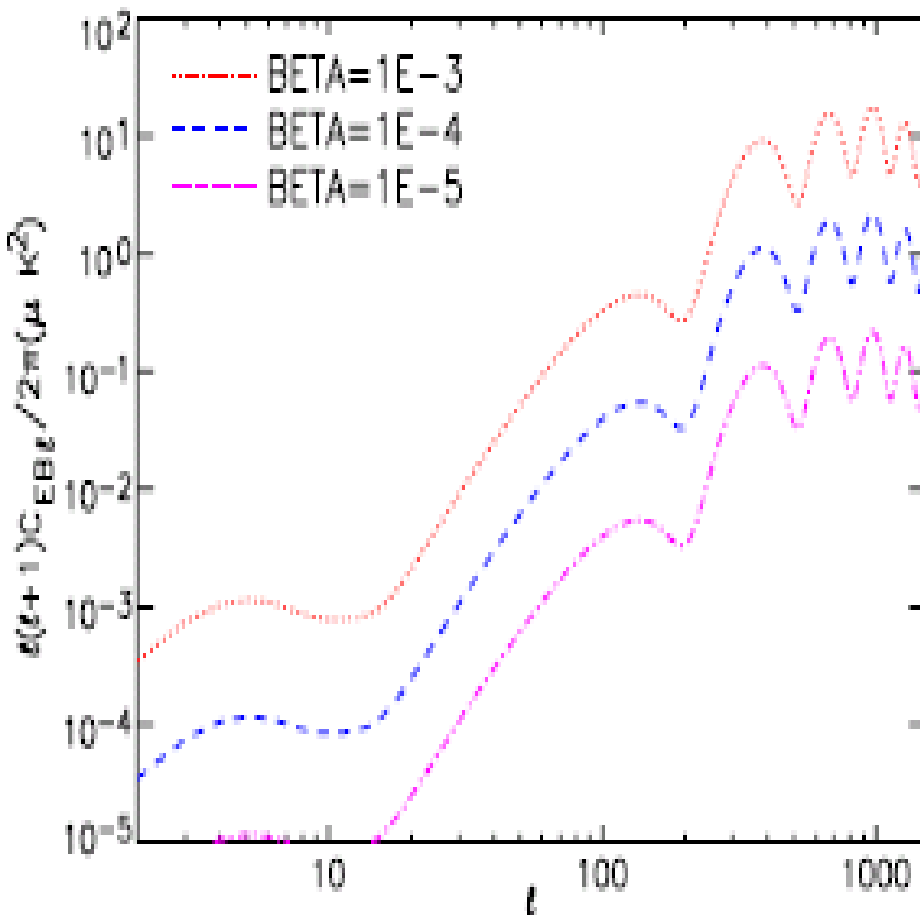
$$\mathcal{L}_N = -\frac{1}{4}\sqrt{-g}B_{F\tilde{F}}(\phi)F_{\mu\nu}\tilde{F}^{\mu\nu}$$

$$B_{F\tilde{F}} = \beta_{F\tilde{F}}\phi \quad \phi \equiv \frac{\Phi}{M}$$

Rotation angle

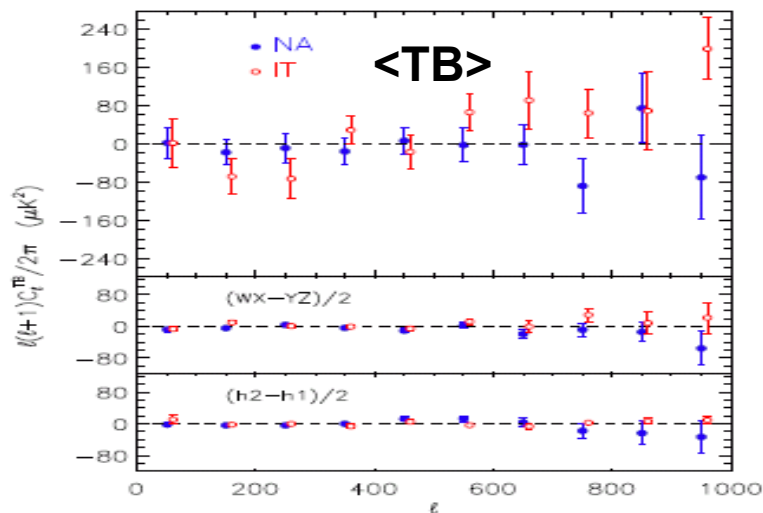
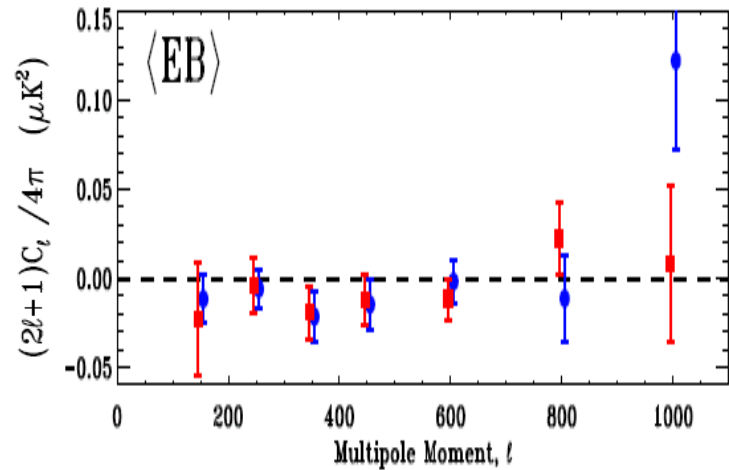
$$\alpha(\eta) = \int_{\eta}^{\eta_0} d\eta' \omega(\eta')$$

Parity violating EB,TB cross power spectra – cosmic parity violation



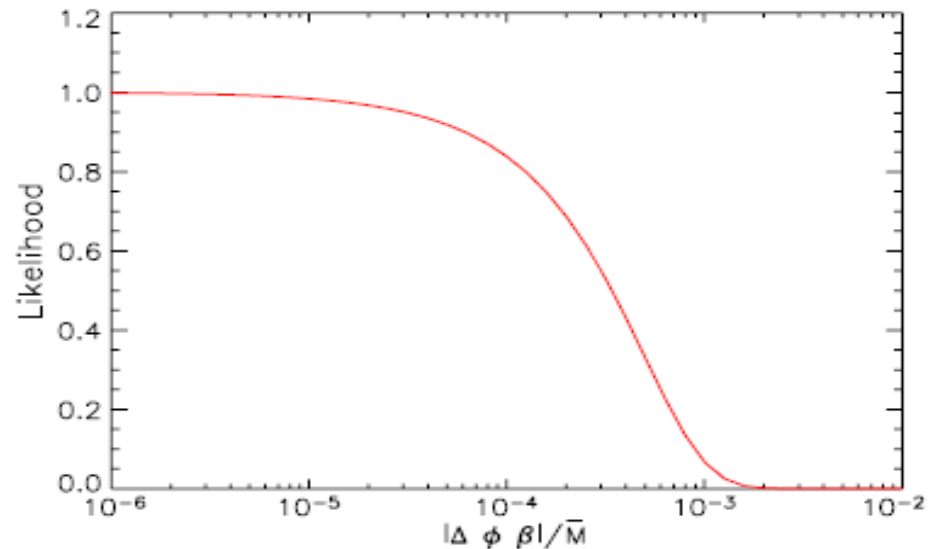
Constraining β by CMB polarization data

2003 Flight of BOOMERANG



Likelihood analysis assuming reasonable quintessence models

$$\bar{V}(\phi) = V_0 \exp(\lambda \phi^2 / 2\bar{M}^2) \quad \bar{V}(\phi) = V_0 \cosh(\lambda \phi / \bar{M})$$



$|\beta_{FF} \Delta \phi| / \bar{M} < 8.32 \times 10^{-4}$ at 95% c.l.
where $\Delta \phi$ is the total change of ϕ until today.

$\bar{M}$ reduced Planck mass

More stringent limits from
....Ni et al.

Including Dark Energy Perturbation

Dark energy
perturbation

$$\phi(\eta, \vec{x}) = \bar{\phi}(\eta) + \delta\phi(\eta, \vec{x}) \quad \delta\phi(\eta, \vec{x}) = \frac{1}{\sqrt{(2\pi)^3}} \int \delta\phi(\vec{k}', \eta) e^{i\vec{k}' \cdot \vec{x}} d^3k'$$

time and space
dependent rotation

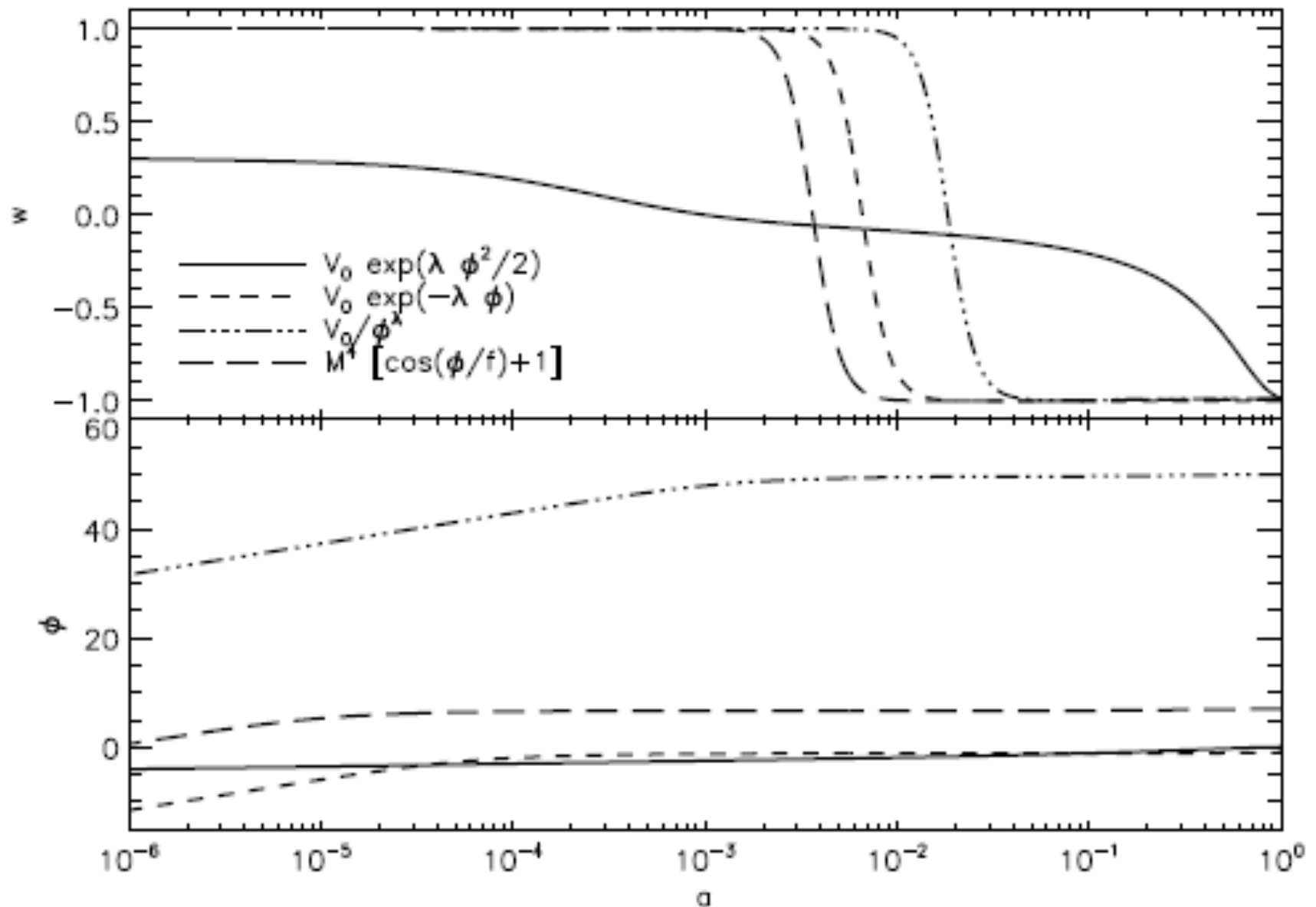
$$\omega = -\frac{1}{2} \frac{\partial B_{F\tilde{F}}}{\partial \phi} \left(\frac{\partial \phi}{\partial \eta} + \vec{\nabla} \phi \cdot \hat{n} \right)$$

$$\dot{\Delta}_{Q\pm iU}(\vec{k}, \eta) + ik\mu \Delta_{Q\pm iU}(\vec{k}, \eta) = n_e \sigma_T a(\eta) \left[-\Delta_{Q\pm iU}(\vec{k}, \eta) \times \right. \\ \left. \sum_m \sqrt{\frac{6\pi}{5}} {}_{\pm 2}Y_2^m(\hat{n}) S_P^{(m)}(\vec{k}, \eta) \right] \mp i2 \frac{1}{\sqrt{(2\pi)^3}} \int d\vec{k}' \tilde{\omega}(\vec{k} - \vec{k}', \eta) \Delta_{Q\pm iU}(\vec{k}', \eta)$$

$$\tilde{\omega}(\vec{k}, \eta) = -\frac{1}{2} \frac{\partial B_{F\tilde{F}}}{\partial \bar{\phi}} \left[\dot{\delta\phi}_{\vec{k}}(\eta) + i\vec{k} \cdot \hat{n} \delta\phi_{\vec{k}}(\eta) \right]$$

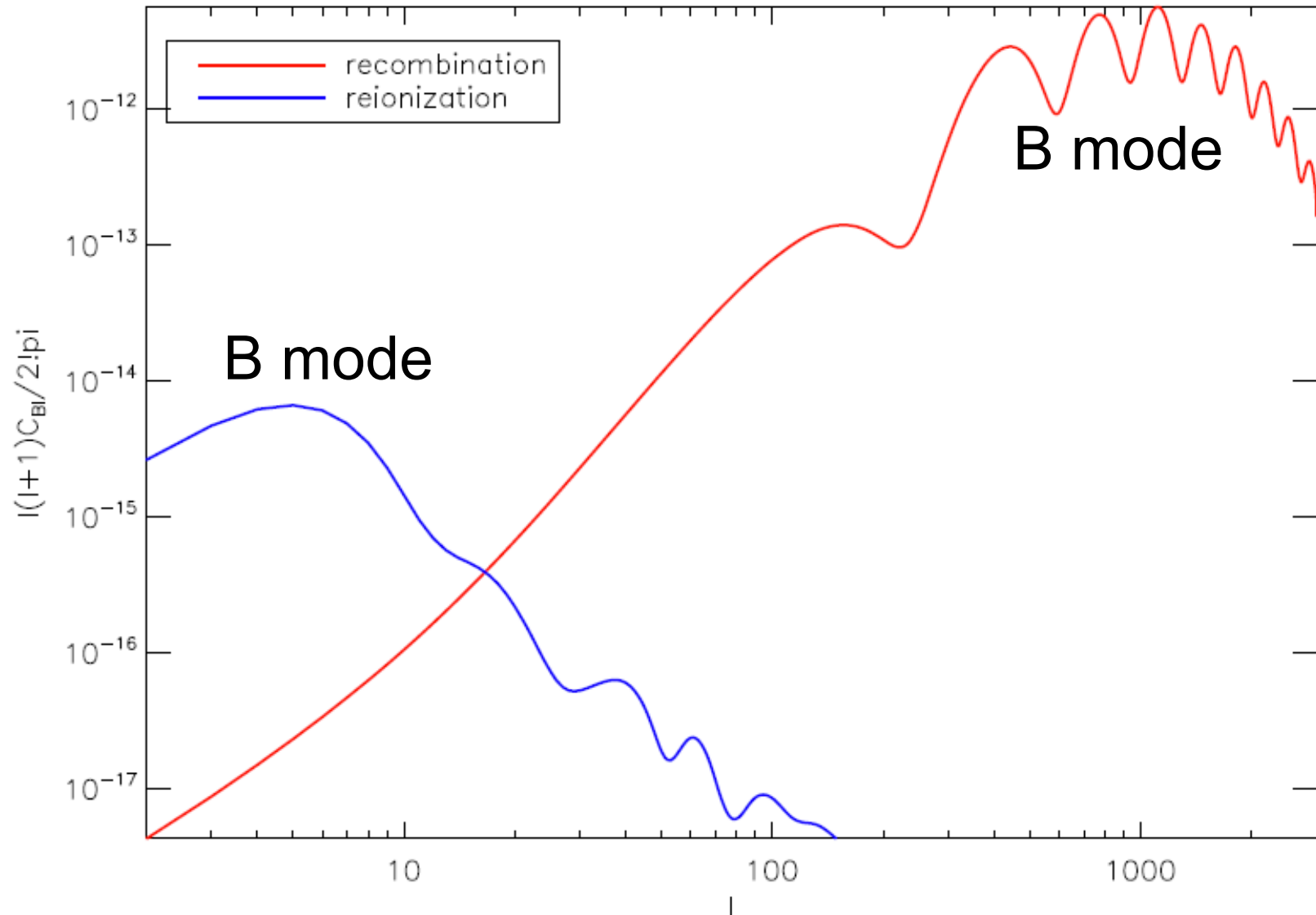
- Perturbation induced polarization power spectra in general quintessence models are small
- Interestingly, in nearly Λ CDM models (no time evolution of the mean field), birefringence generates $\langle BB \rangle$ while $\langle TB \rangle = \langle EB \rangle = 0$

We Tried Many Scalar Dark Energy Models



Dark energy perturbation with $w=-1$ Lee,Liu,Ng 14

Birefringence generates $\langle BB \rangle$ while $\langle TB \rangle = \langle EB \rangle = 0$



Cosmic Birefringence Fluctuations

Lee, Liu, Ng14

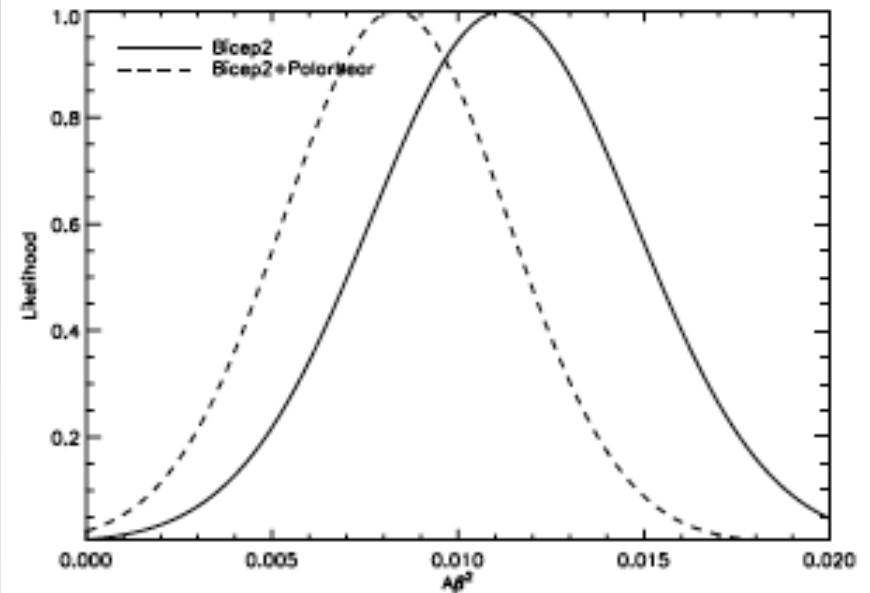
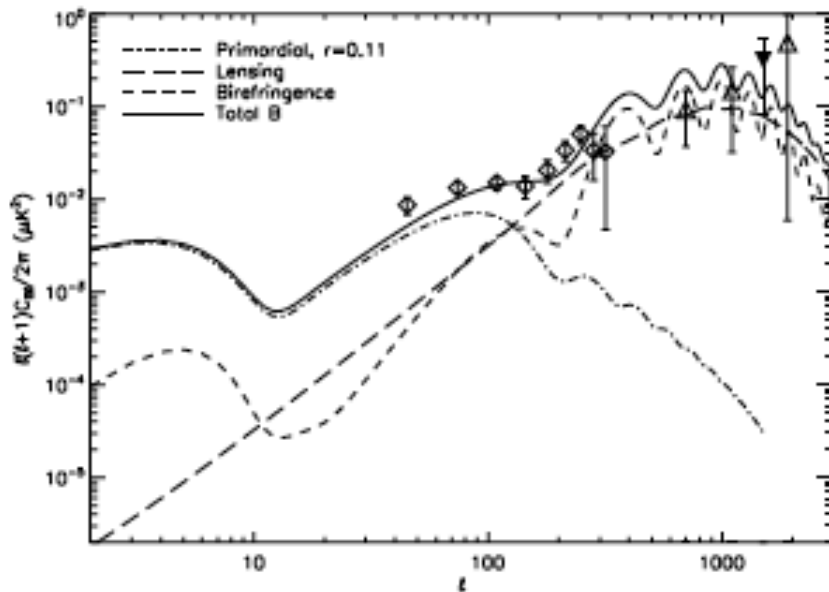
Nearly massless
pseudo scalar

$$\langle \delta\phi_{\vec{k},i} \delta\phi_{\vec{k}',i} \rangle = (2\pi^2/k^3) P_{\delta\phi}(k) \delta(\vec{k} - \vec{k}')$$

$$P_{\delta\phi}(k) = A k^{n-1}$$

Lensed-LCDM+r=0.11+CB

Lee, Liu & Ng arXiv:1403.5585



$$A\beta^2 = 0.0112 \pm 0.032 \text{ BICEP2}$$

$$A\beta^2 = 0.0084 \pm 0.029 \text{ BICEP2+POLARBEAR}$$

Planck mission has put an upper limit on $A < 3.4 \times 10^{-11}$

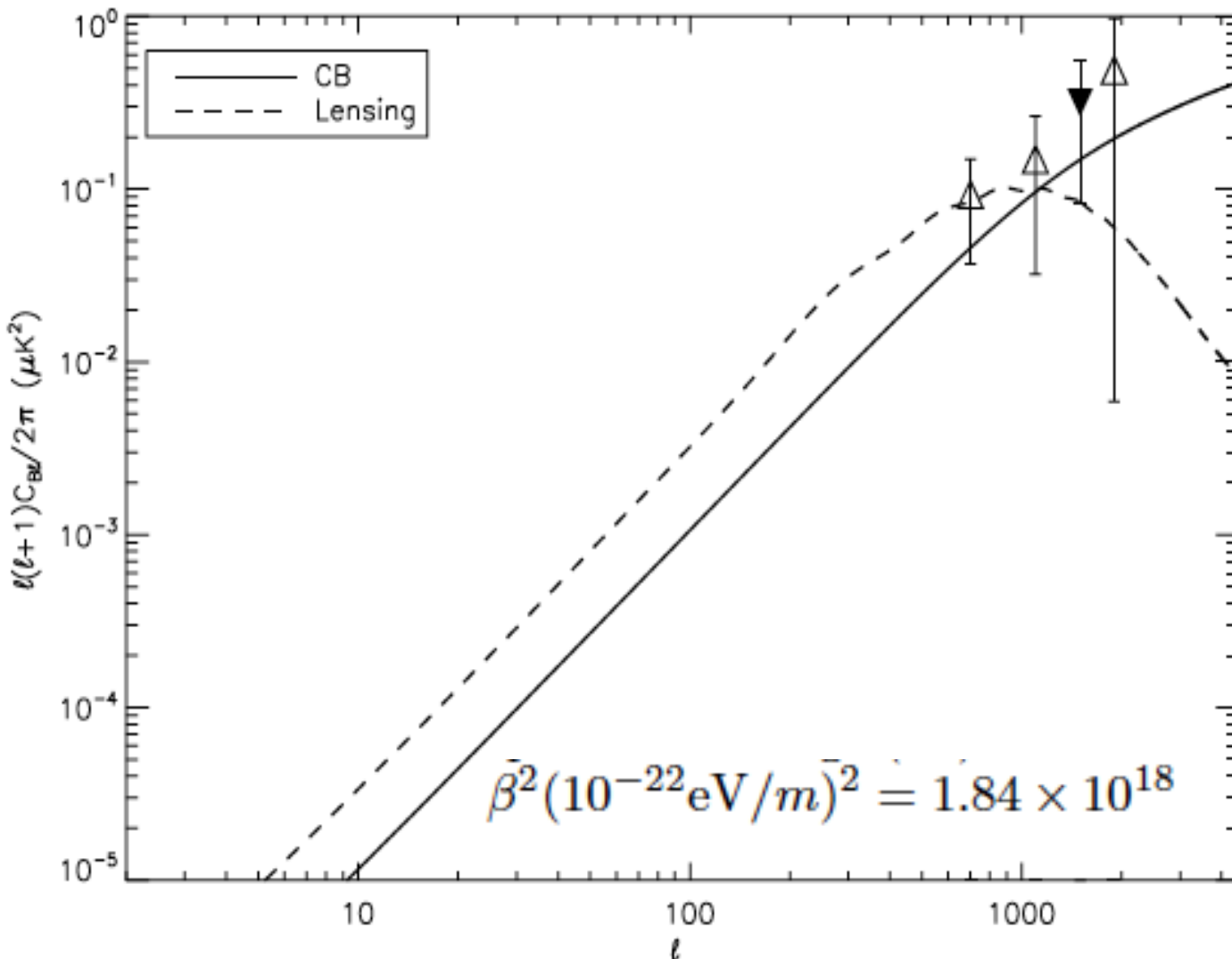
$$\chi^2(r=0.2+\text{lensing}) - \chi^2(\text{CB}+r=0.11+\text{lensing}) = -3.01$$

Only use BICEP2+Polarbear data

Axion ($m \sim 10^{-22} \text{eV}$) CDM curvature perturbation

(preliminary !)

$$\delta\rho_\phi/\rho_\phi = \delta\rho/\rho$$



$$\rho_\phi = m_\phi^2 \phi^2$$

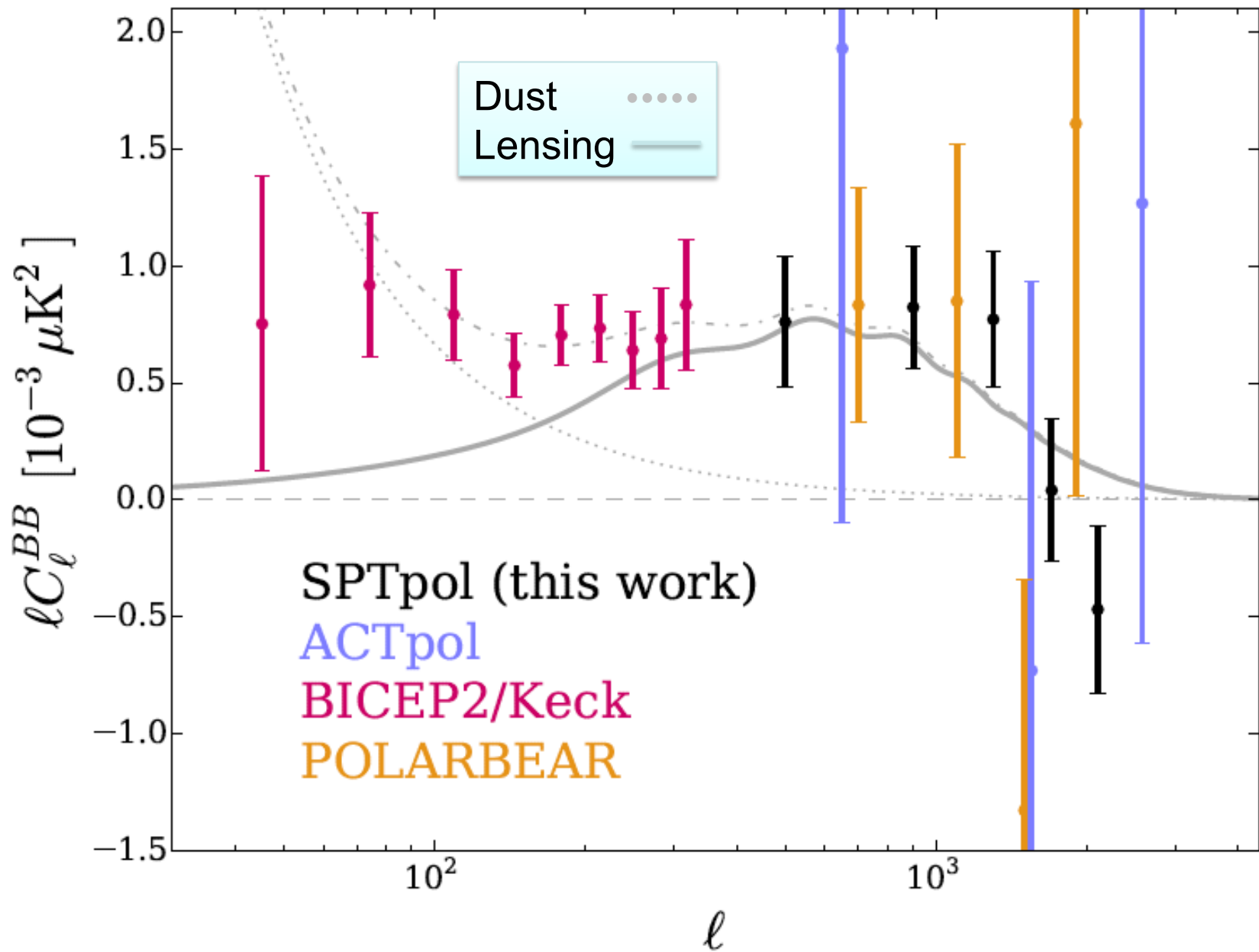
$$\frac{\delta\rho_\phi}{\rho_\phi} = 2 \frac{\delta\phi}{\phi}$$

$$\frac{\delta\phi}{M} = \frac{\delta\phi}{\phi} \frac{\phi}{M}$$

$$\phi = \phi_m \left(\frac{a_m}{a} \right)^{\frac{3}{2}}$$

$$H(a_m) = m$$

More B-mode detection



Summary

- Future observations such as SNe, lensing, galaxy survey, CMB, etc. to measure dark energy $w(z)$ at high- z
- Using CMB B-mode polarization to search for dark energy induced **vacuum birefringence**
 - Mean field time evolution $\rightarrow \langle BB \rangle, \langle TB \rangle, \langle EB \rangle$
 - Include DE perturbation $\rightarrow \langle BB \rangle, \langle TB \rangle = \langle EB \rangle = 0$
- Axion cold matter matter curvature perturbation $\rightarrow \langle BB \rangle, \langle TB \rangle = \langle EB \rangle = 0$; isocurvature perturbation?
- This may confuse the searching for genuine B modes induced by gravitational lensing or primordial gravitational waves, so de-rotation is needed to remove vacuum birefringence effects [Kamionkowski 09](#), [Ng 10](#)