

# Vacuum (meta?)stability, Higgs inflation and physics beyond the Standard Model

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**NCTS Annual Theory Meeting 2015:  
Particles, Strings and Cosmology**

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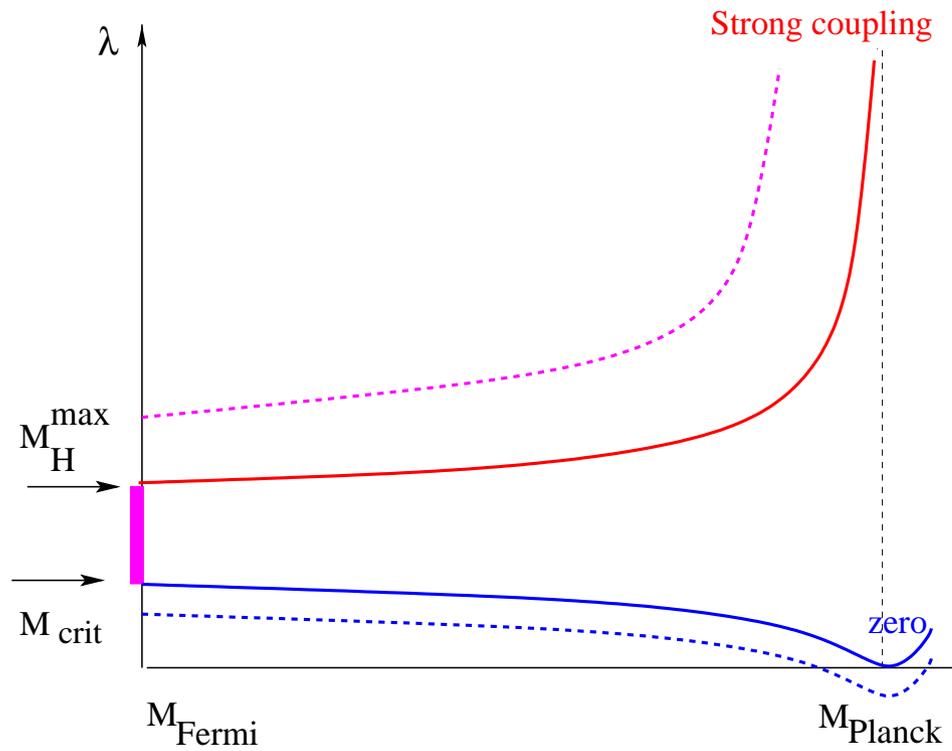
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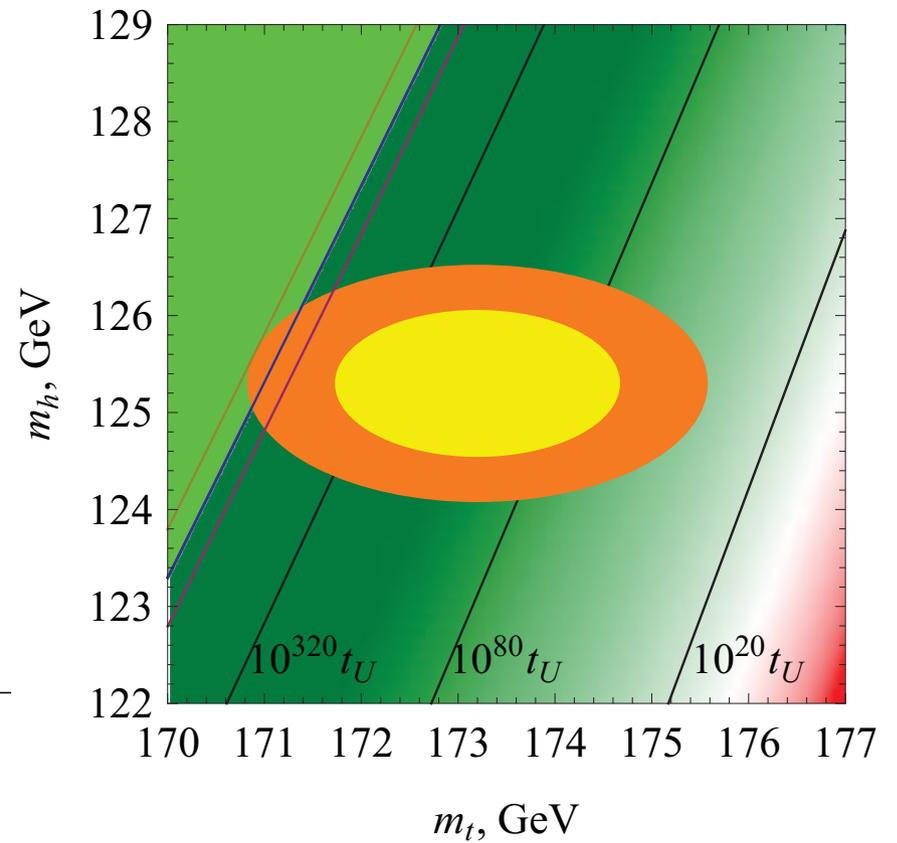
- The Standard Model is now complete: the last particle - Higgs boson, predicted by the SM, has been found
- No deviations from the SM have been observed
- The masses of the top quark and of the Higgs boson, the Nature has chosen, make the SM a self-consistent effective field theory all the way up to the Planck scale

$$114 \text{ GeV} < m_H < 175 \text{ GeV}$$

# Behaviour of the scalar self-coupling

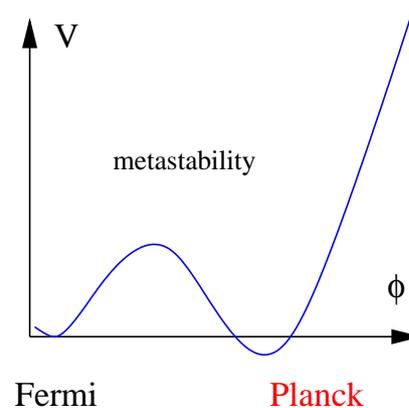
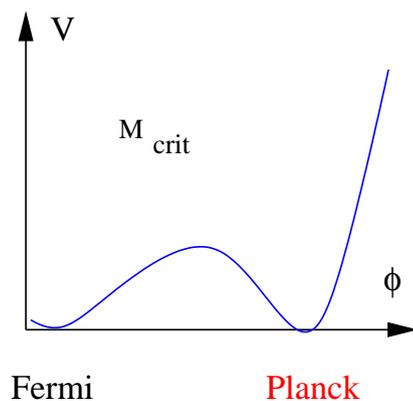
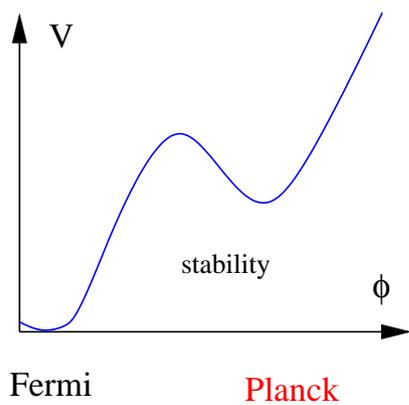


# vacuum lifetime

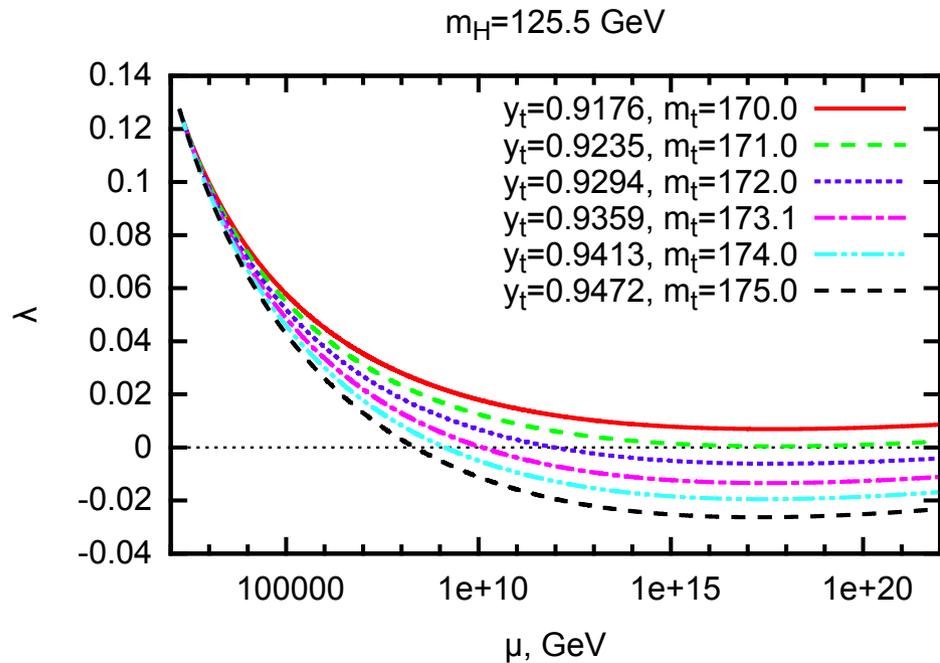


# Vacuum (meta?)stability

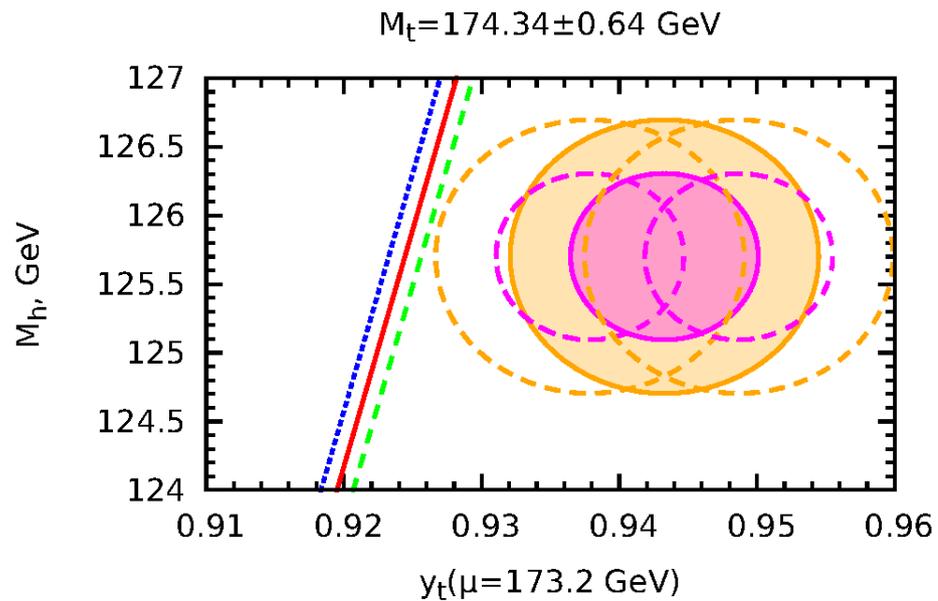
**Important fact:** The combination of top-quark and Higgs boson masses is very close to the **stability** bound of the SM vacuum\* (95'), to the **Higgs inflation bound**\*\* (08'), and to **asymptotic safety** values for  $M_H$  and  $M_t$  \*\*\* (09'):



- \* Froggatt, Nielsen
- \*\* Bezrukov, MS  
De Simone, Hertzberg,  
Wilczek
- \*\*\* Wetterich, MS

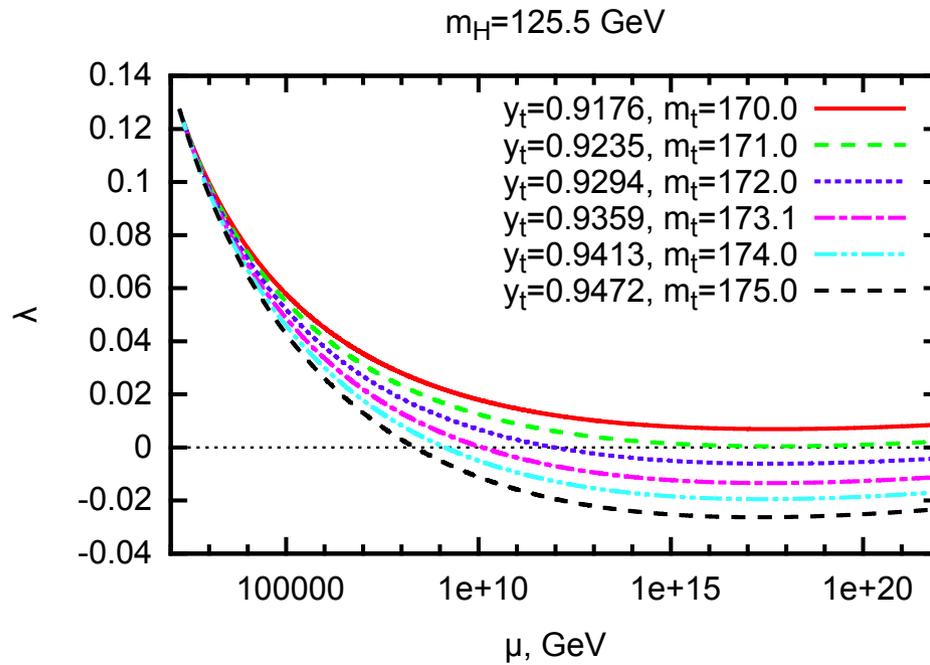


Absolute stability

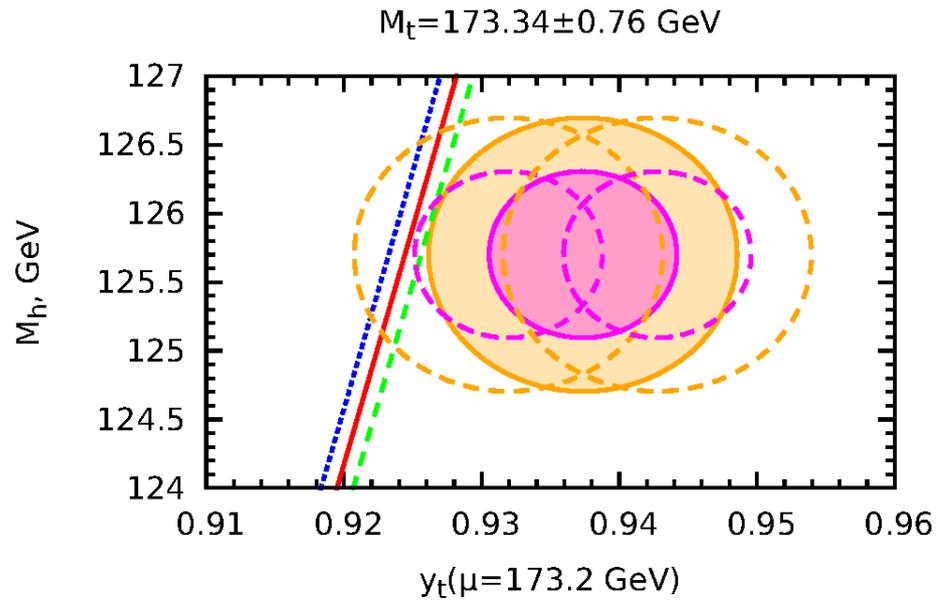


Metastability

TEVATRON 2014:  $m_t = 174.34 \pm 0.37 \pm 0.52$  GeV

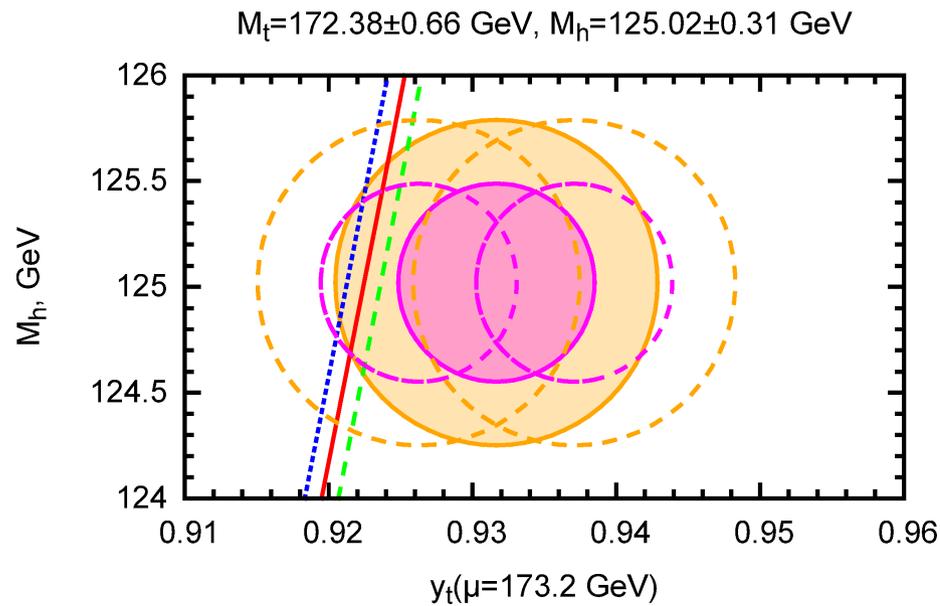
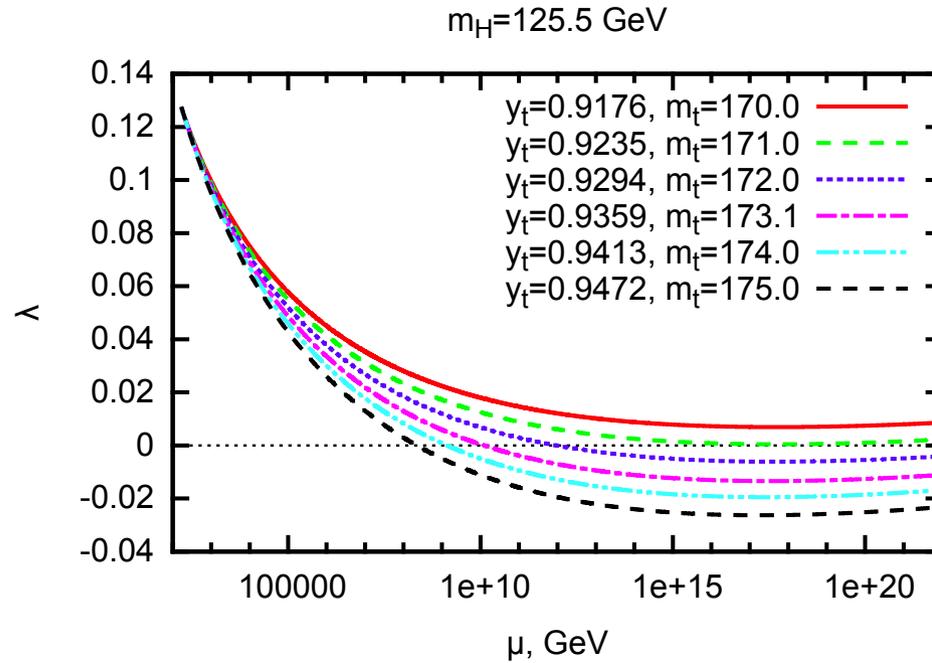


Absolute stability



Metastability

PDG 2014:  $m_t = 173.34 \pm 0.27 \pm 0.71 \text{ GeV}$

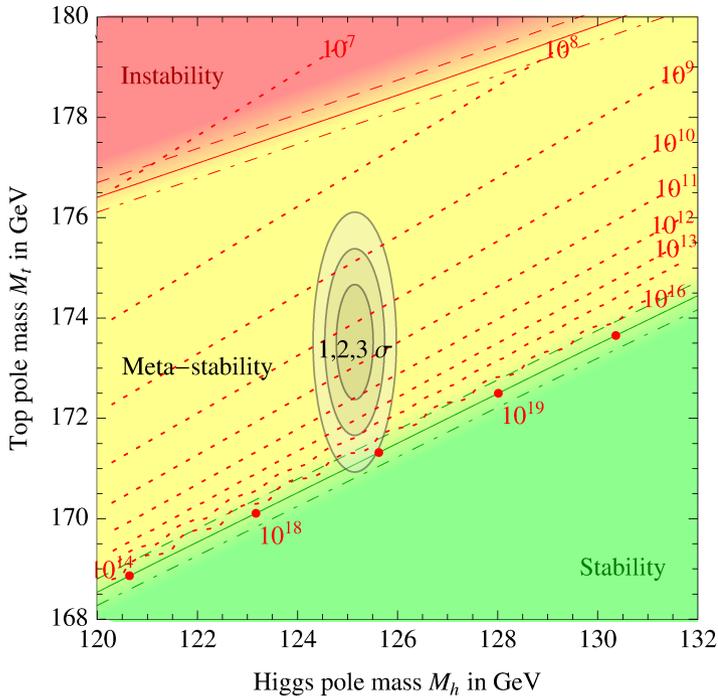


Absolute stability

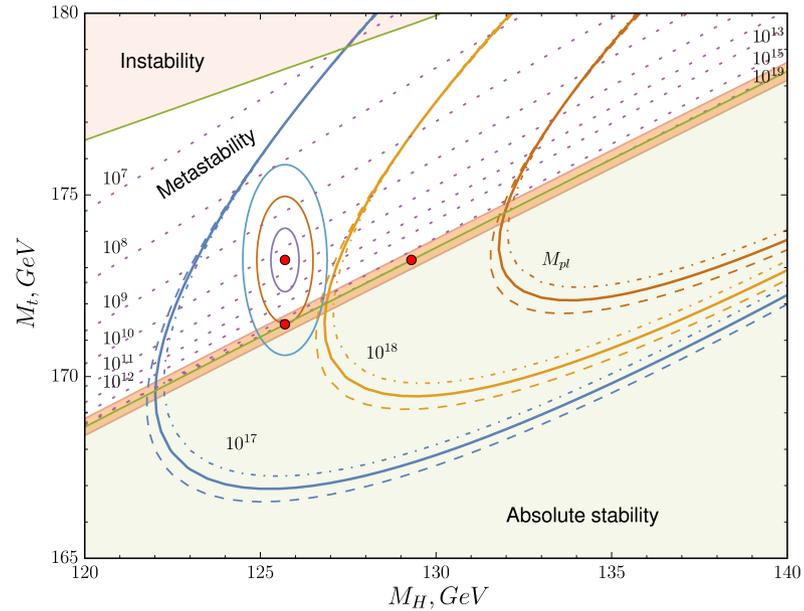
Metastability

**CMS 2014:  $m_t = 172.38 \pm 0.10 \pm 0.65 \text{ GeV}$**

## Buttazzo et al, '13, '14



## Bednyakov et al, '15

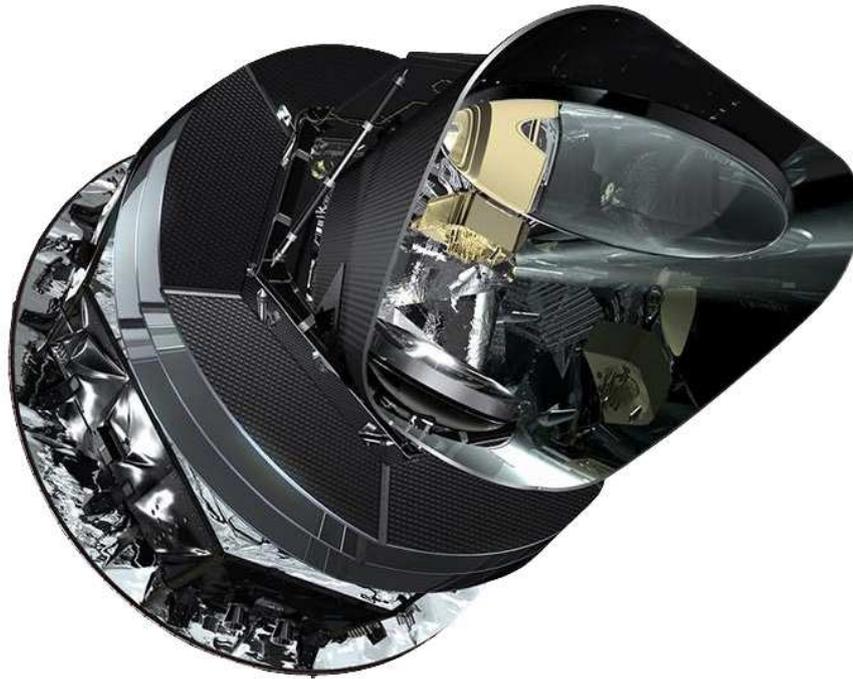


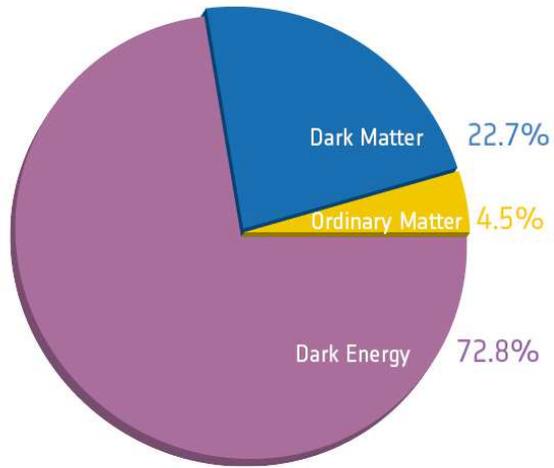
Vacuum is unstable at  $2.8\sigma$

Vacuum is unstable at  $1.3\sigma$

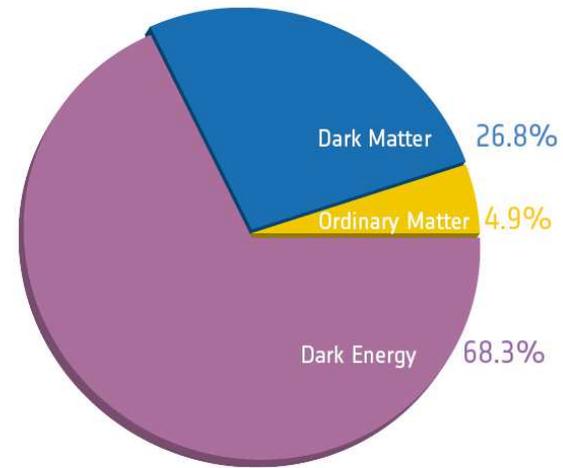
Main uncertainty: top Yukawa coupling, relation between the MC mass and the top Yukawa coupling allows for  $\pm 1$  GeV in  $M_{top}$ . Alekhin et al, Frixione et al.

# Planck results

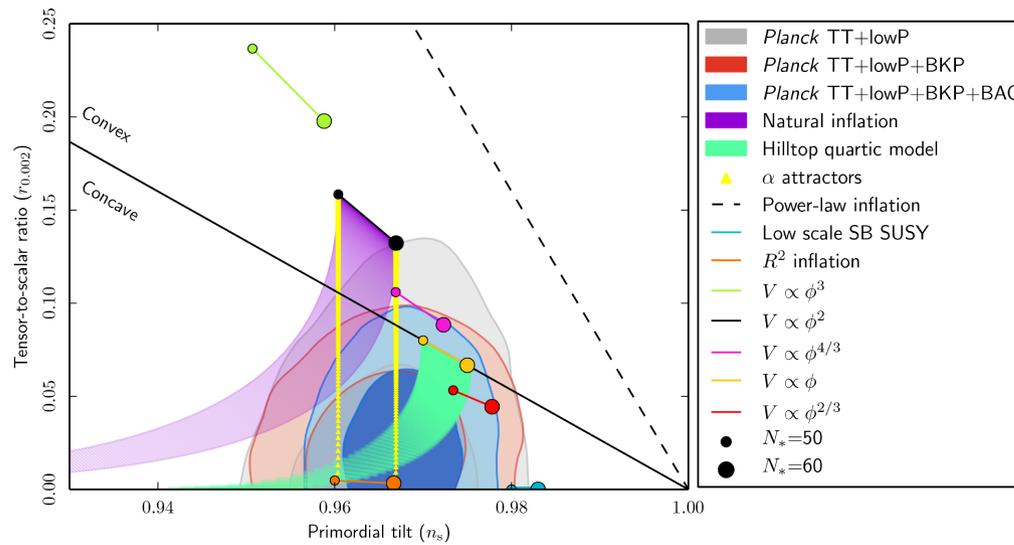




Before Planck



After Planck



# The message from Planck: The Standard $\Lambda$ CDM model is in a very good agreement with the data

- No primordial non-Gaussianities are observed
- One-field inflationary models agree well with Planck
- No physics beyond Standard  $\Lambda$ CDM is observed

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- The Universe is asymmetric: it contains baryons, but there is no antimatter in amounts comparable with matter. **This cannot be explained in the SM.**
- The Universe expansion at present is accelerating. **Is this simply a tiny cosmological constant or something more complicated?**

How to reconcile the evidence for  
new physics without spoiling the  
success of the Standard Model  
and Standard  $\Lambda$ CDM?

Many suggestions, inspired by “naturalness”: how to protect the Higgs boson mass from large corrections coming from unification of the three forces

- Low energy supersymmetry: WIMP as a dark matter candidate, electroweak baryogenesis
- Composite Higgs boson
- Large extra dimensions

Generically, this requires the existence of many new particles at the reach of LHC.

Accelerated expansion of the Universe: Dynamical dark energy?

Modification of gravity at very large scales? New super-light fields?

# A proposal for **minimal** new physics:

Standard Model with non-minimal coupling of the Higgs field to  
gravitational Ricci scalar : Higgs inflation

+

3 right-handed neutrinos with masses in KeV-GeV region: neutrino  
masses, dark matter, and baryogenesis

+

cosmological constant: no clue why so small, but fits the data

# Higgs inflation near the critical line

# Higgs Inflation, no loops

Higgs field in general must have **non-minimal** coupling to gravity:

$$S_G = \int d^4x \sqrt{-g} \left\{ -\frac{M_P^2}{2} R - \frac{\xi h^2}{2} R \right\}$$

Jordan, Feynman, Brans, Dicke,...

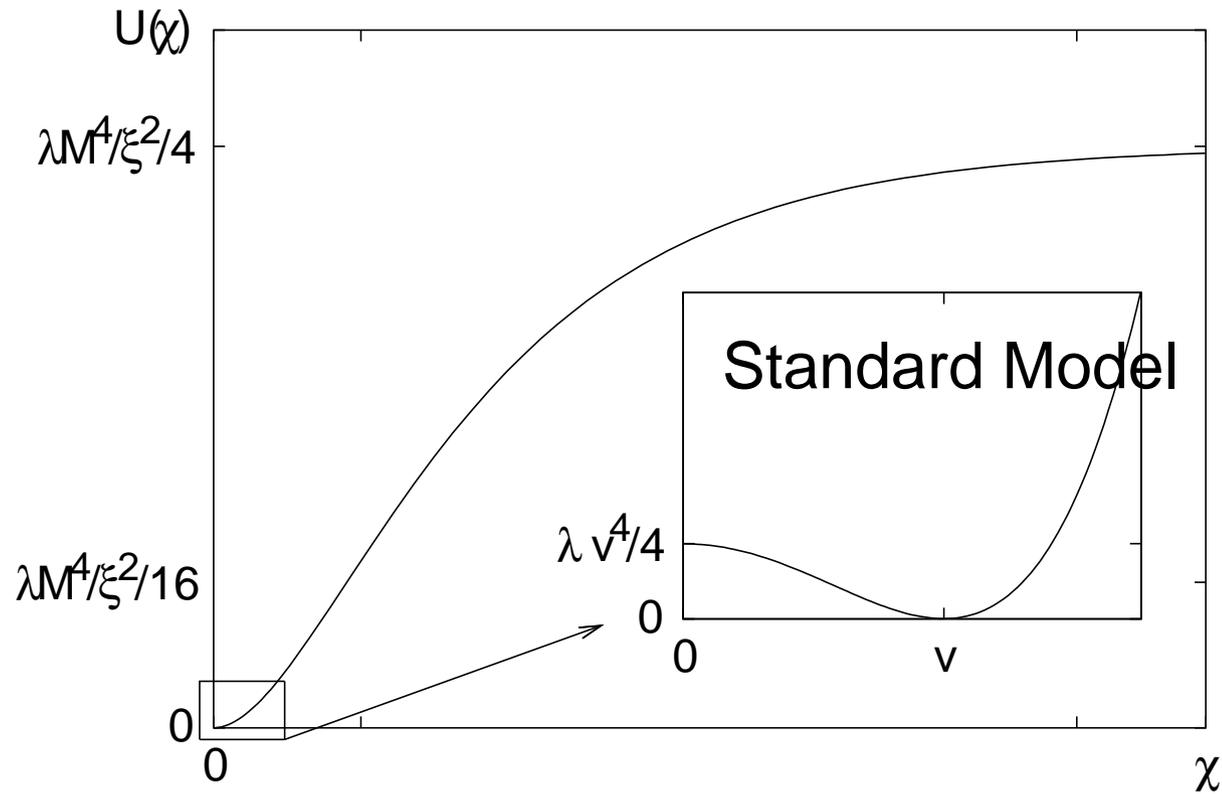
Consider large Higgs fields  $h > M_P/\sqrt{\xi}$ , which may have existed in the early Universe

The Higgs field not only gives particles their masses  $\propto h$ , but also determines the gravity interaction strength:

$$M_P^{\text{eff}} = \sqrt{M_P^2 + \xi h^2} \propto h$$

For  $h > \frac{M_P}{\sqrt{\xi}}$  (classical) physics is the same ( $M_W/M_P^{\text{eff}}$  does not depend on  $h$ )!

# Potential in Einstein frame



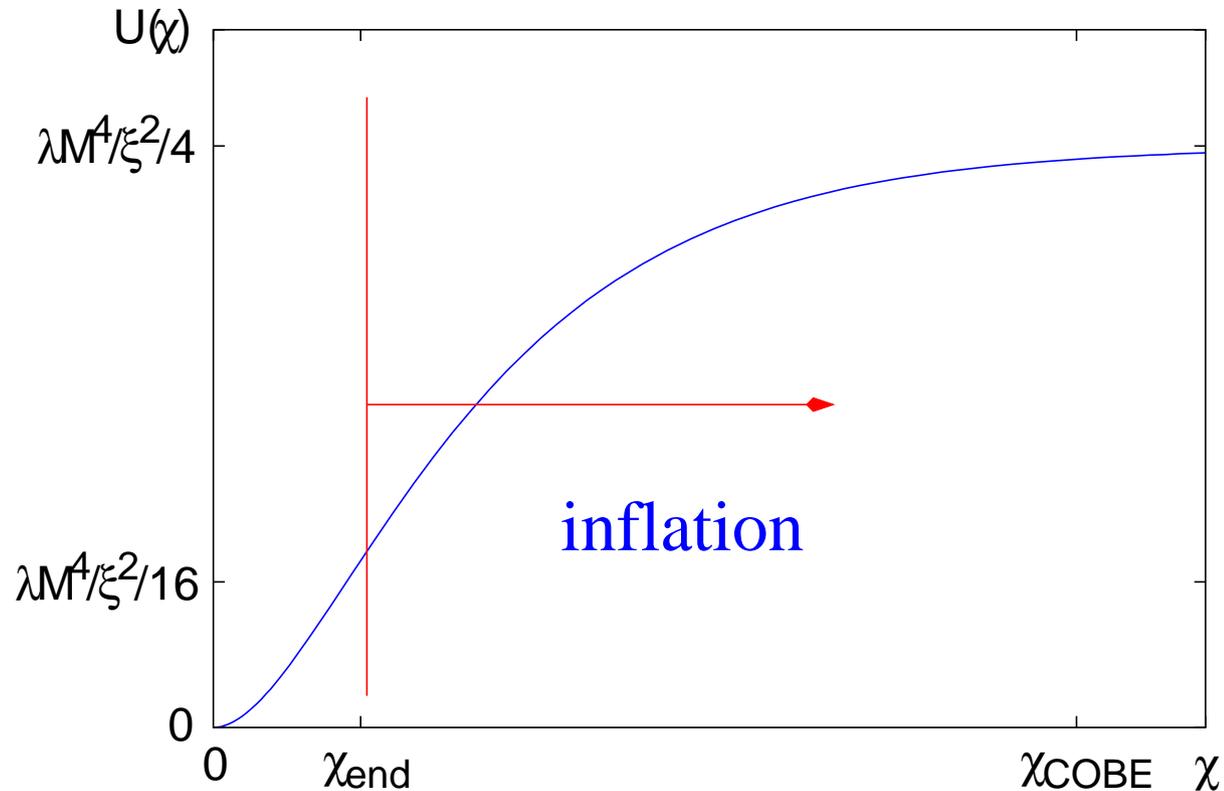
$\chi$  - canonically normalized scalar field in Einstein frame.

Potential for the Higgs field may be flat at large values of  $h$ : Linde chaotic inflation

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Inflation, Big Bang - all in the framework of the Standard Model

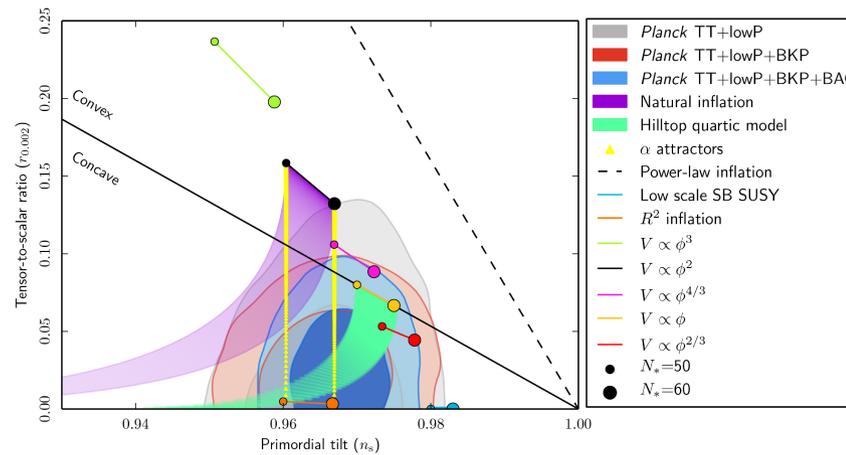
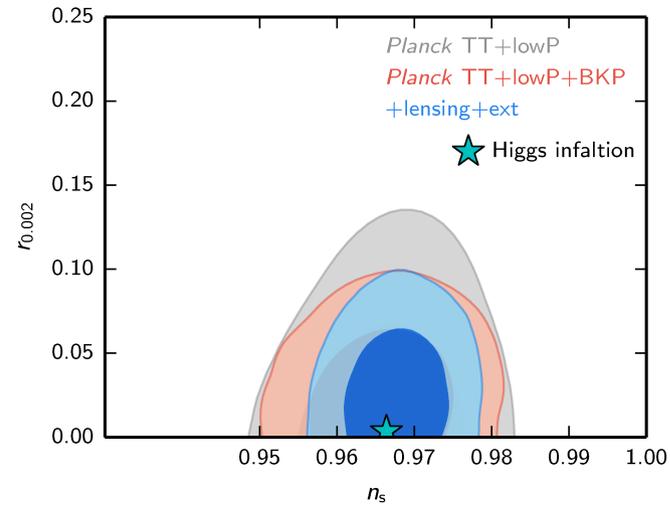
Stage 1: Higgs inflation,  $h > \frac{M_P}{\sqrt{\xi}}$ , slow roll of the Higgs field



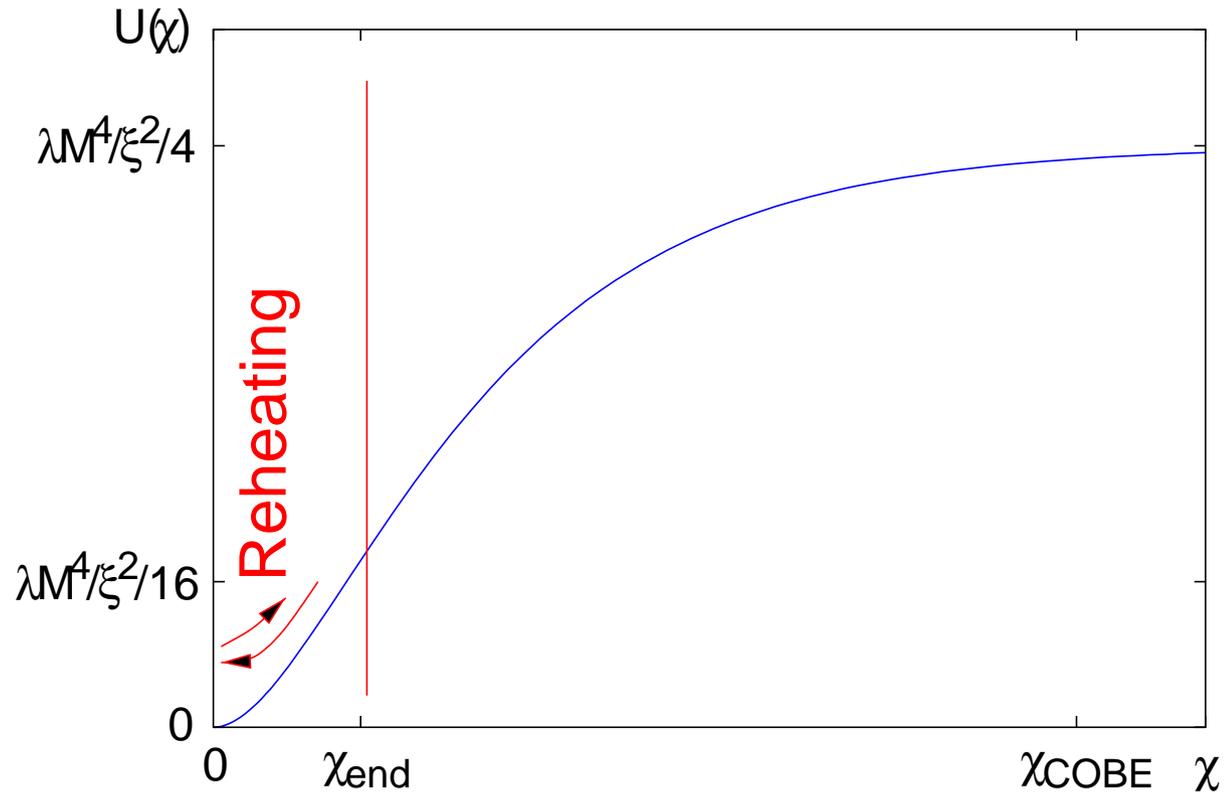
- Makes the Universe flat, homogeneous and isotropic
- Produces fluctuations leading to structure formation: clusters of galaxies, etc

# CMB parameters - spectrum and tensor modes, $\xi \gtrsim 1000$

$$n_s = 0.97, \quad r = 0.003$$



## Stage 2: Big Bang, $\frac{M_P}{\xi} < h < \frac{M_P}{\sqrt{\xi}}$ , Higgs field oscillations



- All particles of the Standard Model are produced
- Coherent Higgs field disappears
- The Universe is heated up to  $T \propto M_P/\xi \sim 10^{14}$  GeV

Any theory of inflation is non-renormalisable, as it includes gravity!

How to account for this fact in general, and for the Higgs inflation in particular? Higher dimensional operators? Radiative corrections?

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(ii) Self-consistent approach to Higgs inflation: compute the onset of strong coupling  $\Lambda$  (“UV cutoff”) by considering tree high energy scattering amplitudes Burgess, Lee, Trott ; Barbon and Espinosa in the Higgs-dependent background Bezrukov, Magnin, M.S., Sibiryakov; Ferrara, Kallosh, Linde, A. Marrani, Van Proeyen and add higher-dimensional operators suppressed by this cutoff.

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- (iii) **The most minimal setup**: add to Lagrangian **all** counter-terms necessary to make the theory finite with **all** constant parts having the same structure as counter-terms.  
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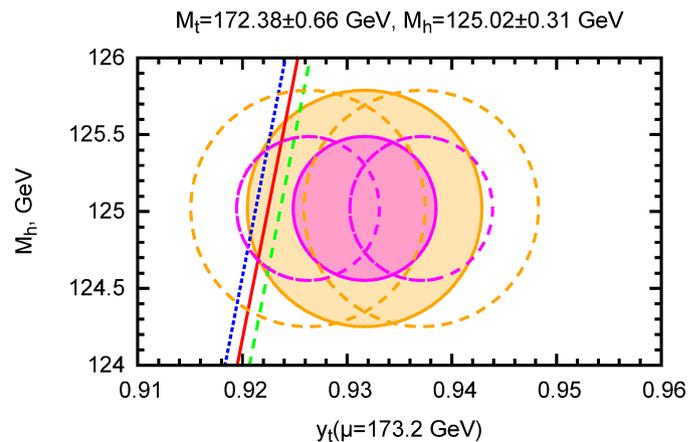
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Radiative corrections, different approaches: Barvinsky, Kamenshchik, Starobinsky; Bezrukov, MS; De Simone, Hertzberg, Wilczek; George, Mooij, Postma,...

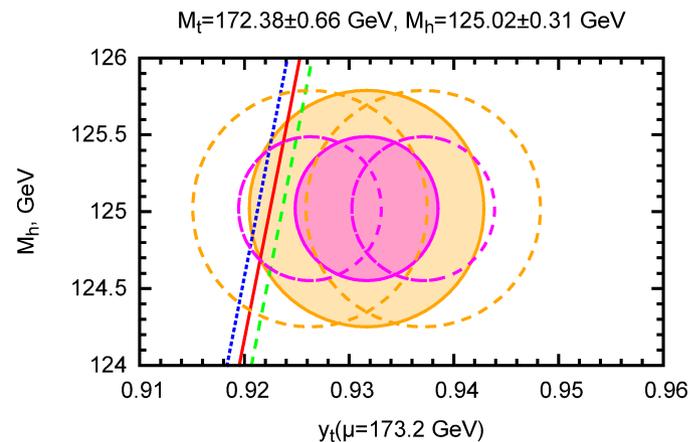
Higgs inflation:  $y_t < y_t^{\text{crit}}$



The same story as the Higgs inflation at the tree level.

# Critical Higgs inflation: $y_t \approx y_t^{\text{crit}}$

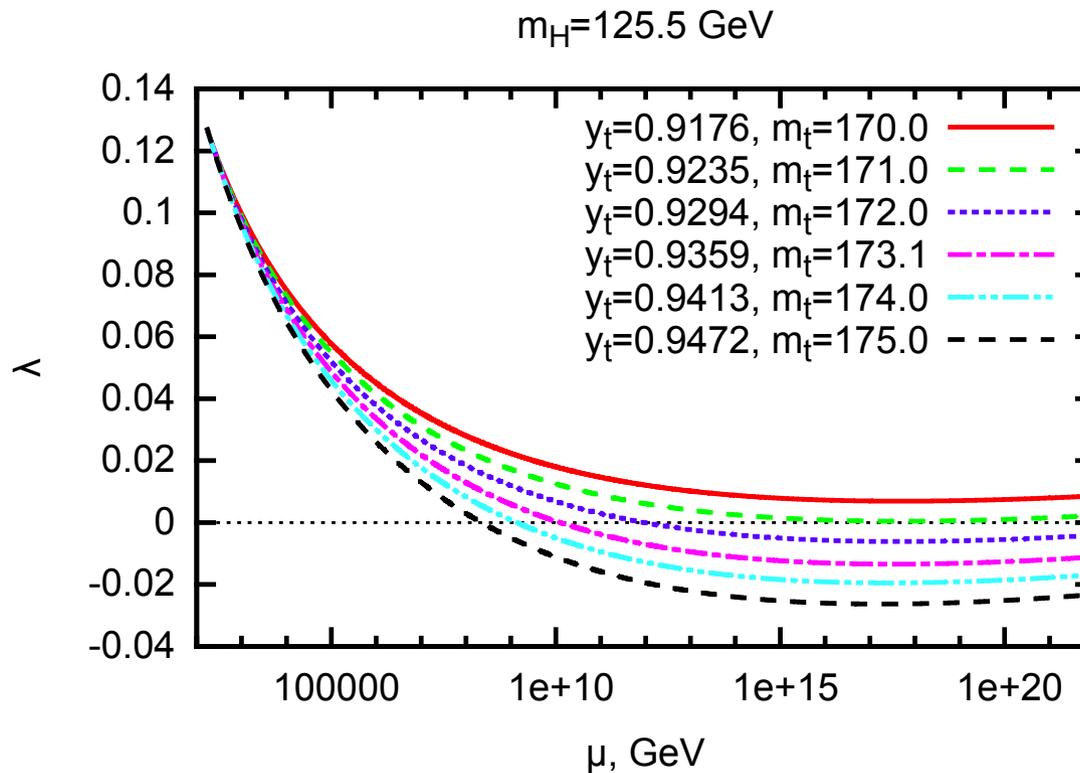
Extreme fine tuning of the Higgs and top quark masses



## Bezrukov, MS

For  $y_t$  very close to  $y_t^{\text{crit}}$  : critical Higgs inflation - tensor-to-scalar ratio can be large,  $\xi \sim 10$

Behaviour of  $\lambda$ :



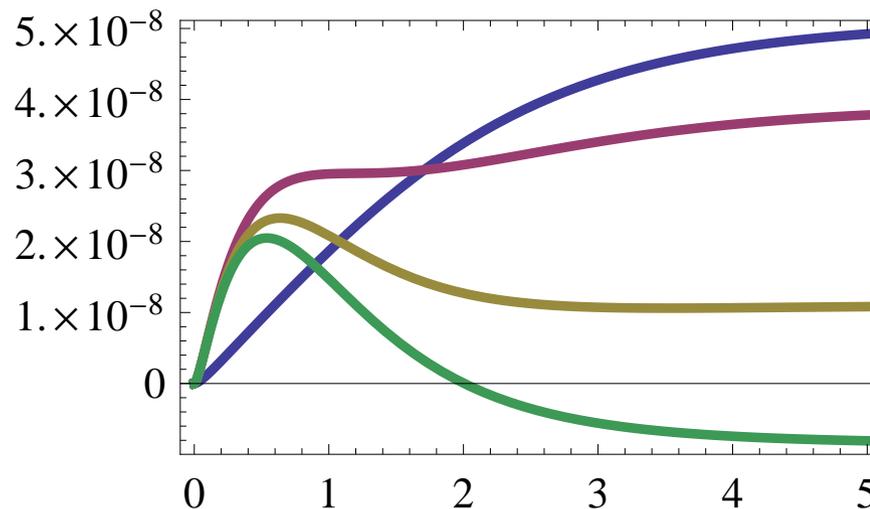
# Effective potential

$$U(\chi) \simeq \frac{\lambda(z')}{4\xi^2} \bar{\mu}^4, \quad z' = \frac{\bar{\mu}}{\kappa M_P}, \quad \bar{\mu}^2 = M_P^2 \left( 1 - e^{-\frac{2\chi}{\sqrt{6}M_P}} \right)$$

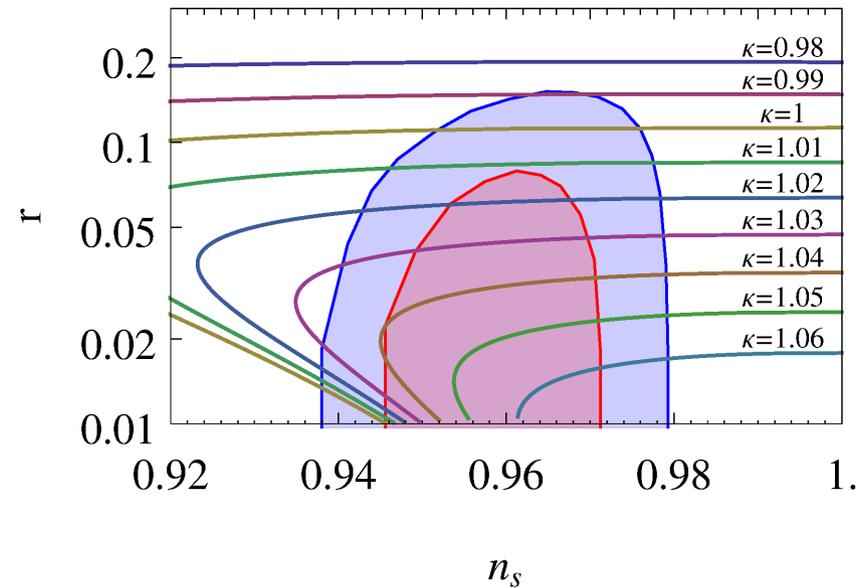
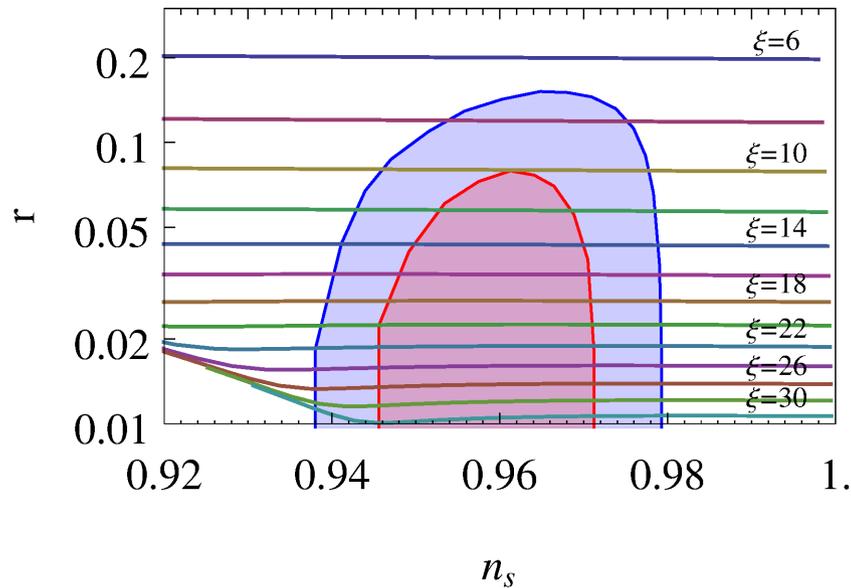
The parameter  $\mu$  that optimises the convergence of the perturbation theory is related to  $\bar{\mu}$  as

$$\mu^2 = \alpha^2 \frac{y_t(\mu)^2}{2} \frac{\bar{\mu}^2}{\xi(\mu)}, \quad \alpha \simeq 0.6$$

Behaviour of effective potential for  $\lambda_0 \simeq b/16$ :



# The inflationary indexes

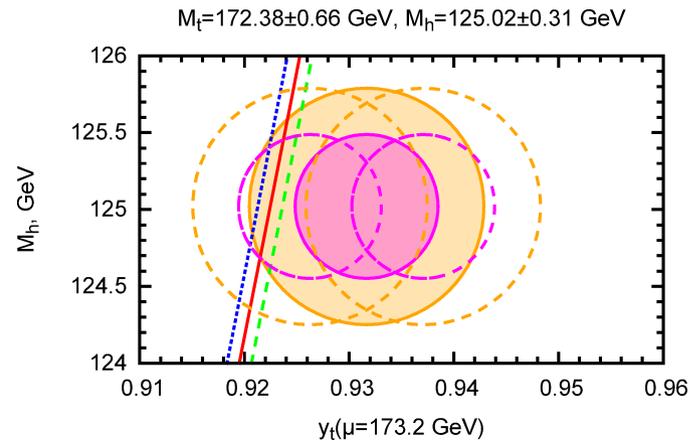


$r$  can be large!

see also [Hamada, Kawai, Oda and Park](#)

Critical Higgs inflation only works if **both** Higgs and top quark masses are close to their experimental values.

# Living beyond the edge: Higgs inflation and vacuum metastability, $y_t > y_t^{\text{crit}}$

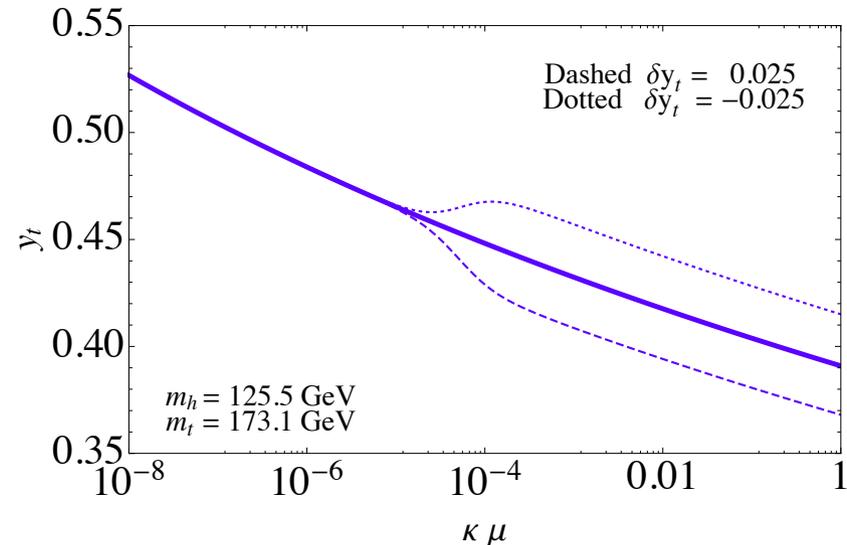
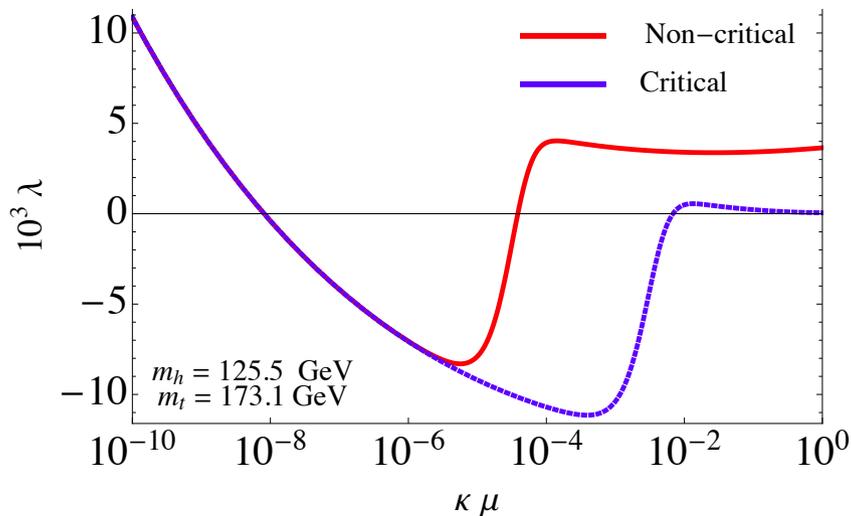


## Bezrukov, Rubio, MS

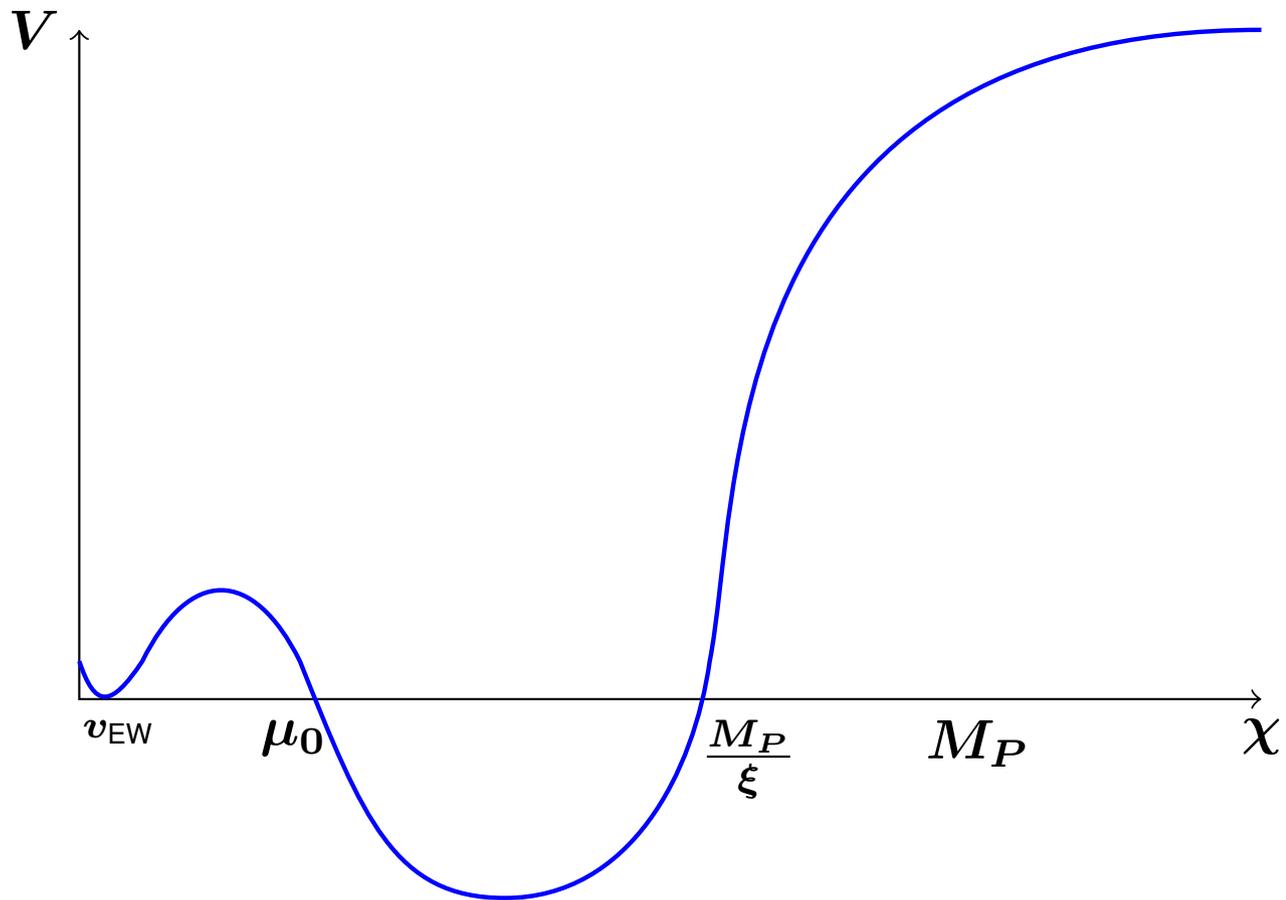
Renormalisation of the SM coupling constants at the scale  $M_P/\xi$ :  
“jumps” of  $\lambda$  and  $y_t$  controlled by UV completion of the SM, which  
cannot be found from low-energy observables of the SM

## Bezrukov, Magnin, MS., Sibiryakov

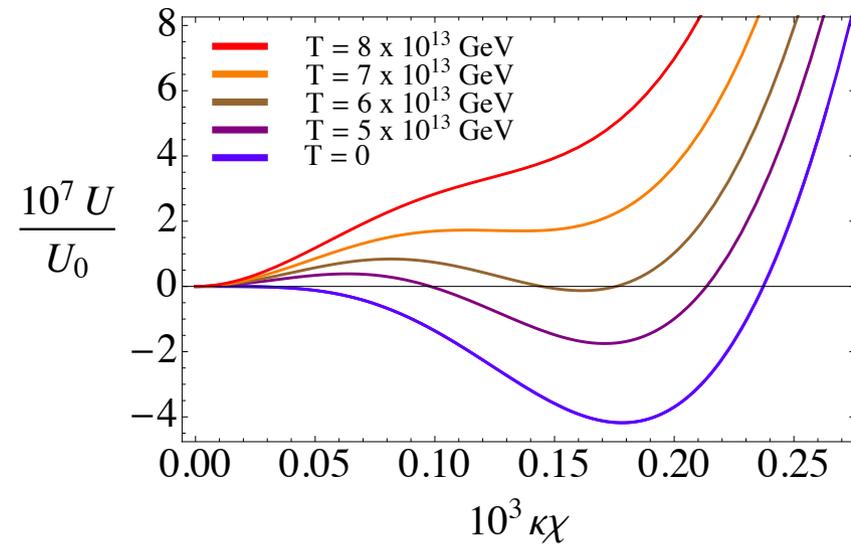
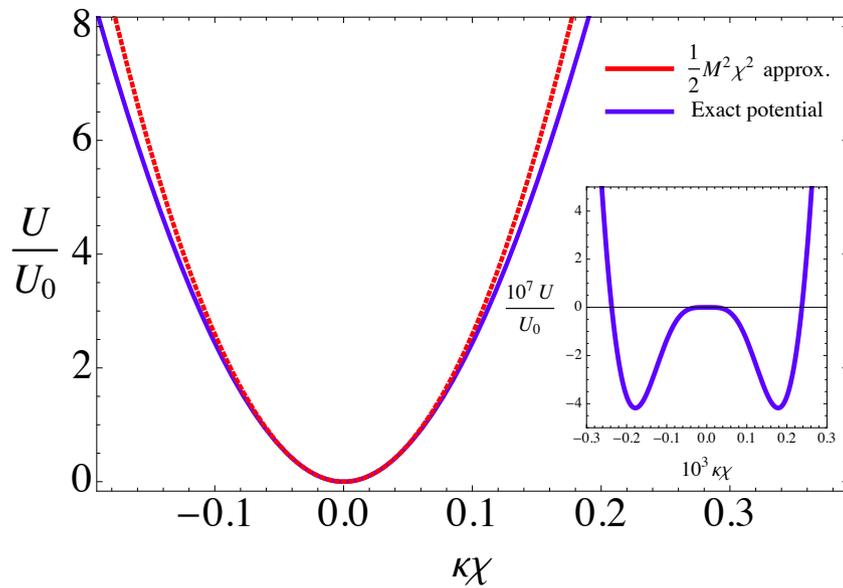
$\lambda(M_P/\xi)$  is small due to cancellations between fermionic and bosonic  
loops:  $\delta\lambda$  can be of the order of  $\lambda$



# Higgs potential



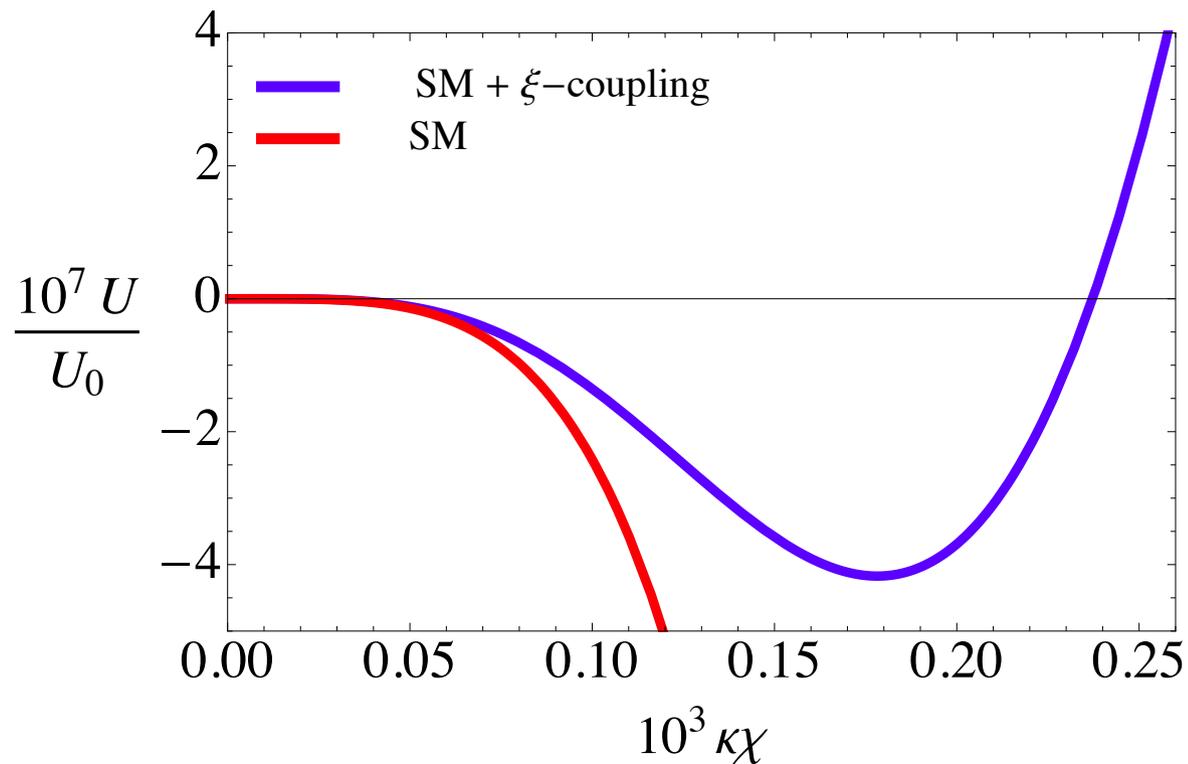
# Symmetry restoration



Reheating temperature  $T_R \simeq 2 \times 10^{14}$  GeV  $>$   $T_+ \simeq 7 \times 10^{13}$  GeV,  
 $T_c = 6 \times 10^{13}$  GeV

# (Meta) stability of false vacuum

Computation for SM: Espinosa, Giudice, Riotto



Predictions for critical indexes  $n_s$  and  $r$  are the same as for non-critical Higgs inflation

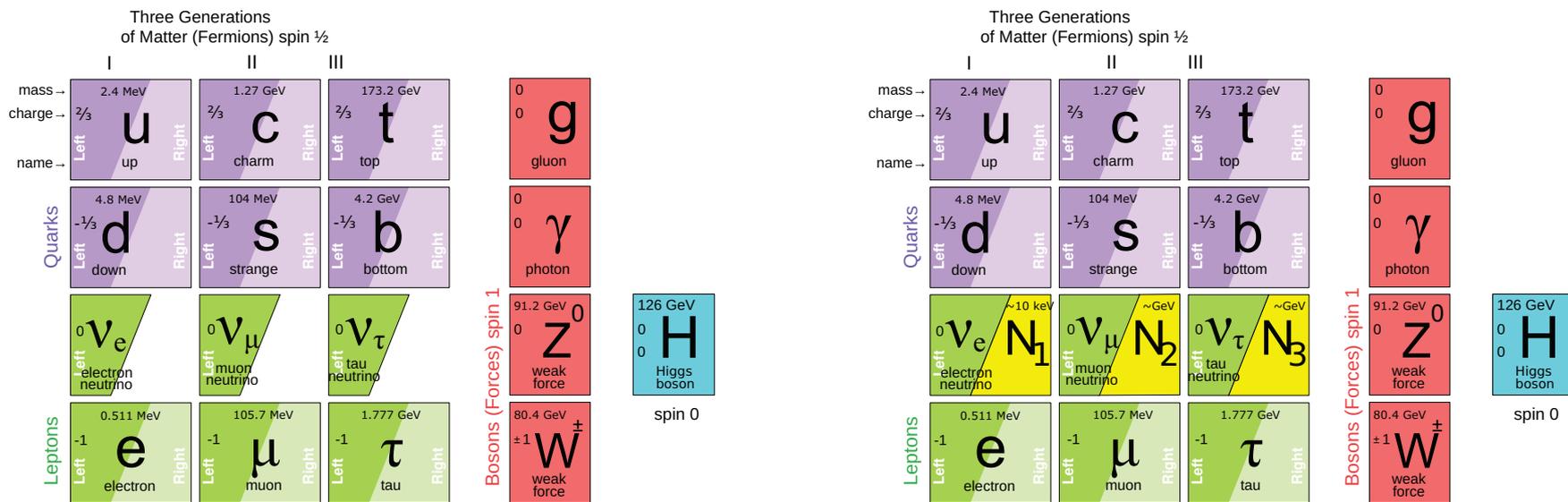
$$n_s = 0.97, \quad r = 0.003$$

Critical Higgs inflation at  $y_t > y_t^{\text{crit}}$ ?

Critical Higgs inflation : small  $\xi \sim 10$  - the depth of the large Higgs value vacuum is comparable with the energy stored in the Higgs after inflation: the required reheating temperature is too large,  $T_+ \simeq 10^{16}$  GeV and cannot be achieved.

# Neutrino masses, dark matter and baryon asymmetry

## $\nu$ MSM - the neutrino minimal Standard Model



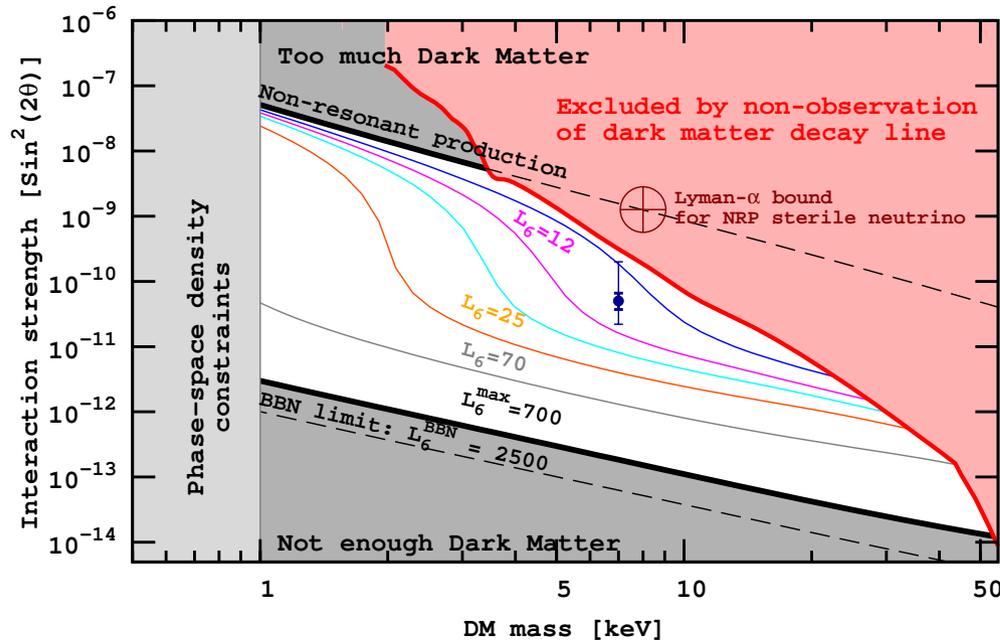
**N = Heavy Neutral Lepton - HNL**

Role of  $N_1$  with mass in keV region: dark matter

Role of  $N_2, N_3$  with mass in 100 MeV – 80 GeV region: “give” masses to neutrinos and produce baryon asymmetry of the Universe (BAU)

# How to find DM HNL?

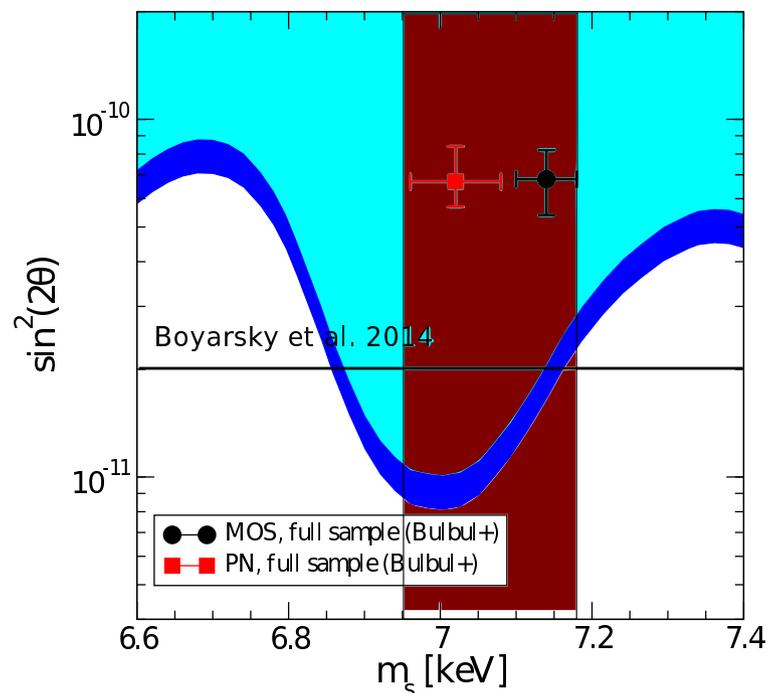
Strategy: Use X-ray telescopes (such as Chandra and XMM Newton) to look for a narrow  $\gamma$  line coming from decays  $N \rightarrow \nu\gamma$



Detection of An Unidentified Emission Line in the Stacked X-ray spectrum of Galaxy Clusters. E. Bulbul et al., e-Print: arXiv:1402.2301

An unidentified line in X-ray spectra of the Andromeda galaxy and Perseus galaxy cluster. A. Boyarsky et al., e-Print: arXiv:1402.4119

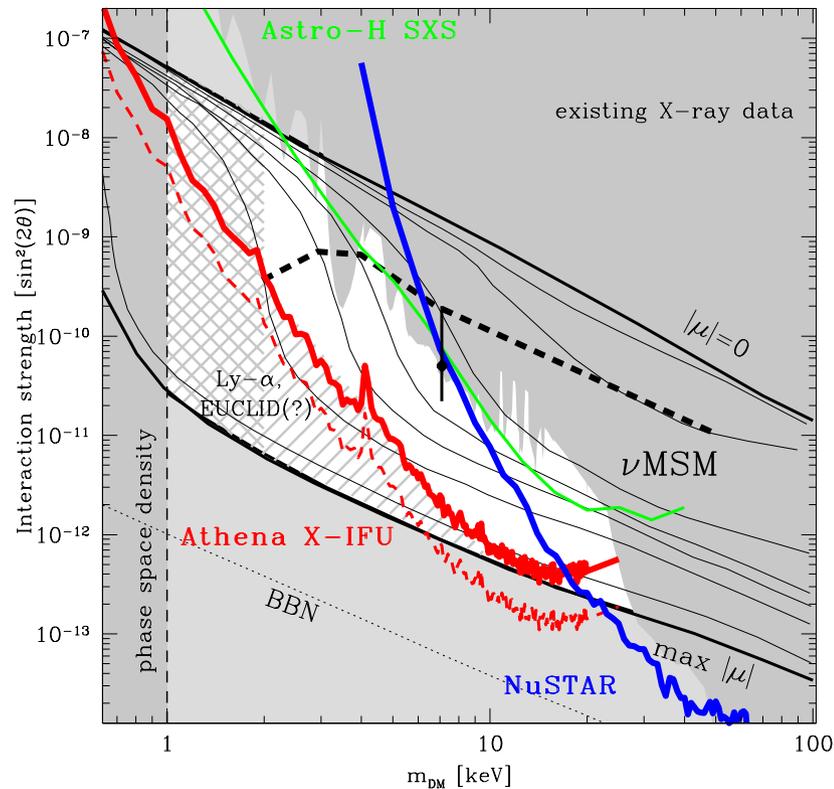
# XMM observations of dwarf spheroidal galaxy Draco (1.6 Msec, PI Boyarsky)



From: Jeltema, Profumo, arXiv:1512.01239

- Statistical fluctuation?
- Non-DM origin of 3.5 keV line?
- Larger uncertainties in DM distribution?

# Future projections

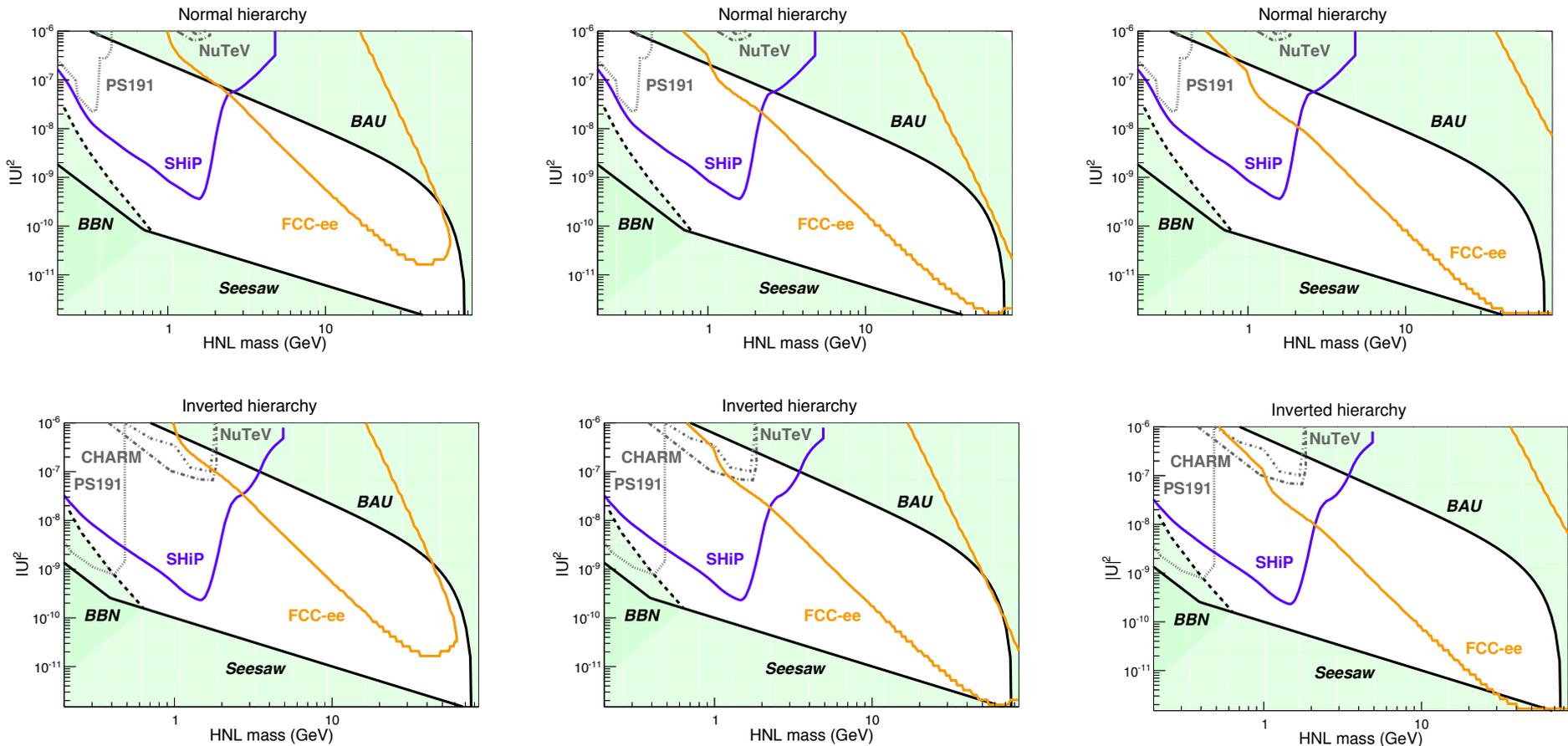


Parameter space of sterile neutrino DM in the  $\nu$ MSM, from arXiv:1509.02758, Neronov et al.

Red line - Athena (launch 2028). Left corner, shaded region "Lyman-alpha"/Euclid : projection for future observations.

# How to find **HNL** responsible for $\nu$ masses and **BAU**?

Strategy: search for decays of HNL such as  $N \rightarrow \pi\mu$  with  $N$  created in fixed target experiments (new proposal at CERN SPS - SHiP) or with  $N$  created in Z-boson decays (new project FCC - ee)



# Conclusions

- The SM is in a great shape and may be valid up to the Planck scale
- The Higgs inflation can take place both for absolutely stable and metastable vacuum, with universal predictions  
 $n_s = 0.97$ ,  $r = 0.003$  for a wide range of parameters
- For critical Higgs inflation corresponding to  $y_t \approx y_t^{\text{crit}}$   $n_s$  and  $r$  can be substantially different from these values
- The BSM physics related to neutrino masses, dark matter and baryon asymmetry of the Universe can be light and can be searched at a number of new experiments (SHiP, FCC) and cosmic missions